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## Quantitative analysis of SO<sub>2</sub>, NO<sub>2</sub> and NO mixed gases based on ultraviolet absorption spectrum

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SO<sub>2</sub>, NO<sub>2</sub> and NO are the main atmospheric pollutants produced by the combustion of fossil fuel. Detecting these gases is of great significance for atmospheric protection and the online concentration detection of pollutants. In this study, the concentration retrieval methods of NO, NO<sub>2</sub> and SO<sub>2</sub> and their mutual effects were studied in the wavelength range of 192.3–254.4 nm. In this band, NO, NO<sub>2</sub> and SO<sub>2</sub> have large absorption cross-sections; however, their spectrum superpositions were serious. A novel method was proposed to separate the superposed absorption spectra of NO and SO<sub>2</sub> or NO<sub>2</sub>. The advantage of this method is that it can remove the influence of SO<sub>2</sub> and NO<sub>2</sub> on NO concentration retrieval. The fast Fourier transform (FFT) amplitude method was used to calculate the concentrations of SO<sub>2</sub> and NO<sub>2</sub>, and the direct absorption spectroscopy method was used to calculate NO concentration. Via these methods, the gas concentrations of SO<sub>2</sub>, NO<sub>2</sub> and NO can be calculated in ternary-gas mixtures. The experimental results show that these methods can effectively remove the mutual interferences between the concentration retrieval of NO, NO<sub>2</sub> and SO<sub>2</sub>. The maximum absolute values of the relative deviations for the concentration retrieval of SO<sub>2</sub>, NO<sub>2</sub> and NO in ternary-gas mixtures are 3.868%, 4.740% and 5.008%, respectively. These methods have high detection precision and good adaptability and are suitable for online flue detection equipment.

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### 1. Introduction

Sulfur dioxide (SO<sub>2</sub>) is one of the main atmospheric pollutants produced by fossil fuel combustion and volcanic eruption.<sup>1,2</sup> When the SO<sub>2</sub> concentration in the surrounding environment exceeds 0.21 ppm, it can harm human health, such as causing respiratory diseases.<sup>2,3</sup> The SO<sub>2</sub> in the air returns to the ground with rainwater, thereby corroding buildings and equipment and damaging water and forest ecosystems.<sup>1,4</sup> Nitrogen oxides (NO<sub>x</sub>, which mainly includes NO and NO<sub>2</sub>) mainly come from the combustion of fossil fuel and biomass, lightning and microbial activity.<sup>5</sup> The NO<sub>x</sub> in the air can combine with water, ammonia, and other organic gases to form smog and acid rain, damaging the ecological environment.<sup>2,6,7</sup> With the rapid development of economy, the use of fossil fuel is increasing to generate power to meet the energy needs of human activities. This will cause an increase in SO<sub>2</sub> and NO<sub>x</sub> emissions and further exacerbate environmental pollution. In order to ensure a healthy living environment and achieve sustainable development of human beings, the Chinese govern-

ment has issued regulations requiring the concentrations of SO<sub>2</sub> and NO<sub>x</sub> emitted by thermal power plants to be lower than 35 ppm and 48.7 ppm, respectively.<sup>8</sup> Because detecting pollutant gas concentrations is an essential prerequisite for controlling emissions, it is of great significance to study methods for detecting SO<sub>2</sub> and NO<sub>x</sub> concentrations.

At present, the main methods for gas detection include the metal oxide sensor method and optical methods.<sup>9</sup> Metal oxide sensors are widely applied in detecting the concentrations of SO<sub>2</sub> and NO due to their low cost. However, the performance of metal oxide sensors deteriorates with increasing working hours and is susceptible to temperature and humidity changes.<sup>9,10</sup> Although some metal oxide sensors can operate at room temperature, their poor stability and repeatability limit their widespread application in the field of high-precision and real-time detection.<sup>9</sup> Optical methods mainly include photoacoustic spectroscopy (PAS), tunable diode laser absorption spectroscopy (TDLAS), non-dispersive infrared spectroscopy (NDIR), differential optical absorption spectroscopy (DOAS), *etc.*<sup>11</sup> Due to the good collimation of lasers, TDLAS easily achieves a considerable optical path, so it can achieve high-precision detection. However, the equipment for TDLAS is relatively expensive and can only detect one kind of gas at a time with poor scalability.<sup>12,13</sup> NDIR uses infrared light as the detection system's light source. It can detect NO<sub>2</sub> and NO in a large concentration range, but is susceptible to interference from

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water vapor and has poor anti-interference ability and large measurement deviations.<sup>14</sup> Moreover, when measuring multiple gases, it requires multiple measurement channels, increasing hardware costs.<sup>13,14</sup> DOAS has good scalability, high selectivity, high economy, and high accuracy and can simultaneously detect multiple gases. Therefore, it has been widely applied in the field of multiple gas detection.<sup>5,14</sup> However, DOAS also faces the following challenge: under extremely low concentration conditions, the spectral signal received by the traditional detection systems is easily affected by noise, making it difficult to achieve high-precision detection.<sup>14,15</sup>

There are two main solutions to the current problem of using DOAS technology to detect gas concentrations: the first method is to use an absorption cell with a long optical path to improve the signal-to-noise ratio of the detection system, as shown in ref. 2; the second method is to select the gas absorption band with the larger absorption cross-section as the gas retrieval wavelength band. However, deuterium lamps, which are often used as the light source in the DOAS detection systems, have a large divergence angle and are difficult to achieve good collimation like lasers, making it difficult to achieve a long optical path in detection systems. NO, SO<sub>2</sub> and NO<sub>2</sub> have large absorption cross-sections in the wavelength range of 192–255 nm, but their absorption cross-sections are mixed with each other, as shown in Fig. 1,<sup>16</sup> bringing difficulties to gas concentration retrieval. In the field of low concentration and high-precision mixed gas detection, research on separation methods for superposed absorption spectra has great application potential. For example, ref. 14 studied the absorption spectra of mixtures of SO<sub>2</sub> and NO and achieved SO<sub>2</sub> measurement deviations from –4% to 1.19%.

In this paper, DOAS and direct absorption spectroscopy are used to separate the superposed absorption spectra of NO<sub>2</sub>, SO<sub>2</sub> and NO mixed gases in the wavelength range of 192.3–254.4 nm. This method makes full use of the advantage of the large absorption cross-section in this wavelength range to improve the concentration retrieval precision of the gases in SO<sub>2</sub>, NO<sub>2</sub> and NO mixtures.

## 2. Theory

### 2.1 Lambert–Beer law

The propagation of a monochromatic beam with wavelength  $\lambda$  in a specific gas is expressed by the Lambert–Beer law<sup>2,10,17,18</sup> as shown in eqn (1), where  $I_0(\lambda)$  is the light intensity of the monochromatic beam with wavelength  $\lambda$  which isn't absorbed by the gas to be measured,  $I(\lambda)$  is the remaining light intensity after being absorbed by the gas,  $\sigma(\lambda)$  is the absorption cross-section of the gas to be measured at wavelength  $\lambda$  (cm<sup>2</sup> per molecule),  $L$  is the optical path of the beam propagating in the gas (cm) and  $C$  is the gas concentration (molecule per cm<sup>3</sup>).

$$I(\lambda) = I_0(\lambda) \times \exp[-\sigma(\lambda)CL] \quad (1)$$

The Rayleigh scattering  $\varepsilon_R(\lambda)$  and Mie scattering  $\varepsilon_M(\lambda)$  of the gas molecules also play a role in reducing the light intensity of the beam propagating in the gas, so eqn (1) can be revised as eqn (2). The meanings of the other parameters in eqn (2) are the same as in eqn (1).

$$I(\lambda) = I_0(\lambda) \times \exp[-\sigma(\lambda)CL - \varepsilon_R(\lambda) - \varepsilon_M(\lambda)] \quad (2)$$

Because nitrogen is hardly absorbed in the wavelength range of 192.3–254.4 nm, there is only Rayleigh scattering and Mie scattering. Therefore, the Rayleigh scattering and Mie scattering in eqn (2) can be replaced by measuring high-purity nitrogen, as shown in eqn (3). In eqn (3),  $I'_0(\lambda)$  is the light intensity when the gas to be measured is high-purity nitrogen, and the meanings of the other parameters are the same as in eqn (2).

$$I'_0(\lambda) = I_0(\lambda) \times \exp[-\varepsilon_R(\lambda) - \varepsilon_M(\lambda)] \quad (3)$$

Substituting eqn (3) into eqn (2), the result is eqn (4). Taking the logarithm of eqn (4), the result is eqn (5).  $A(\lambda)$  is the gas absorbance in eqn (5). According to eqn (5), there is a linear relationship between the concentration of a specific gas

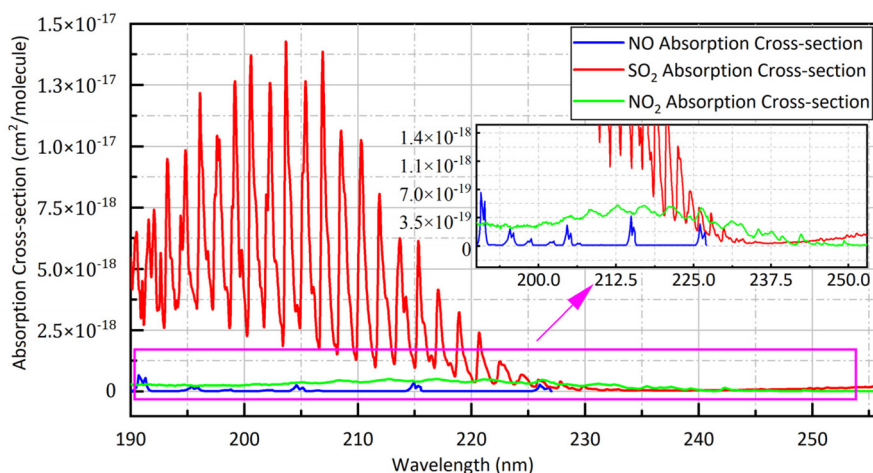


Fig. 1 Absorption cross-sections of NO, NO<sub>2</sub> and SO<sub>2</sub> at 190–256 nm.<sup>16,24</sup>

and its absorbance, which is the theoretical basis for gas measurement based on the absorption spectroscopy method.<sup>18</sup>

$$I(\lambda) = I_0(\lambda) \times \exp[-\sigma(\lambda)CL] \quad (4)$$

$$A(\lambda) = \ln\left(\frac{I_0(\lambda)}{I(\lambda)}\right) = \sigma(\lambda)CL \quad (5)$$

## 2.2 Differential optical absorption spectroscopy

In the DOAS theory, a gas absorption cross-section can be divided into two parts, as shown in eqn (6): one part is the slow-varying part which varies slowly with wavelength, and the other is the fast-varying part which varies rapidly with the wavelength. In eqn (6),  $\sigma^f(\lambda)$  and  $\sigma^s(\lambda)$  are the fast-varying part and the slow-varying part respectively, and the meanings of the other parameters are the same as in eqn (2).<sup>2,19,20</sup>

$$I(\lambda) = I_0(\lambda) \times \exp[-(\sigma^f(\lambda) + \sigma^s(\lambda))CL - \varepsilon_R(\lambda) - \varepsilon_M(\lambda)] \quad (6)$$

Just like in the previous section, the Rayleigh scattering and Mie scattering in eqn (6) are replaced by measuring high-purity nitrogen. Taking the logarithm of eqn (6), the result is shown as eqn (7). In eqn (7),  $A'(\lambda)$  is the absorbance of the gas to be measured. As shown in eqn (8), the fast-varying part can represent the concentration information of the gas, and DOD( $\lambda$ ) is the differential absorbance of the gas. It is known from eqn (8) that the DOD( $\lambda$ ) of a specific gas is linearly related to the gas concentration. Therefore, DOD( $\lambda$ ) can be used to retrieve the gas concentration.

$$A'(\lambda) = \ln\left(\frac{I_0(\lambda)}{I(\lambda)}\right) = (\sigma^f(\lambda) + \sigma^s(\lambda))CL \quad (7)$$

$$\text{DOD}(\lambda) = \sigma^f(\lambda)CL \quad (8)$$

However, when using eqn (8) for gas measurement, the gas to be measured must be a single component gas and eqn (8) cannot be used when the gas to be measured is a mixture of multiple gases. When measuring mixtures of multiple gases, eqn (6) is adjusted to eqn (9),<sup>2,21,22</sup> where  $\sigma_i^f(\lambda)$  and  $\sigma_i^s(\lambda)$  are the fast-varying part and the slow-varying part, respectively, of the absorption cross-section of the  $i$ -th gas. The meanings of the other parameters in eqn (9) are the same as in eqn (6).

$$I(\lambda) = I_0(\lambda) \times \exp\left[-\sum_{i=1}^n (\sigma_i^f(\lambda) + \sigma_i^s(\lambda))C_iL - \varepsilon_R(\lambda) - \varepsilon_M(\lambda)\right] \quad (9)$$

Just like in the measurement of a single gas, the Rayleigh scattering and Mie scattering in eqn (9) are replaced by measuring high-purity nitrogen and then taking the logarithm of eqn (9). The result is shown as eqn (10), where  $A''(\lambda)$  is the absorbance of the multiple gases. Using a mathematical method to filter out the slow-varying parts of multiple gases, the differential absorbance of multiple gases can be obtained, as shown in eqn (11).<sup>1,14</sup>

$$A''(\lambda) = \ln\left(\frac{I_0(\lambda)}{I(\lambda)}\right) = \sum_{i=1}^n (\sigma_i^f(\lambda) + \sigma_i^s(\lambda))C_iL \quad (10)$$

$$\text{DOD}'(\lambda) = \sum_{i=1}^n \sigma_i^f(\lambda)C_iL \quad (11)$$

When using DOAS to measure multiple gases, it is necessary to filter out the slow-varying parts of different gases and obtain a differential absorbance that can represent the concentration information of multiple gases. However, the slow-varying parts of different gases have different characteristics, making it difficult to find a suitable method to simultaneously filter out the slow-varying part of different gases.

## 3. Experimental system setup

The schematic diagram of the measurement system is shown in Fig. 2. A deuterium lamp (Hamamatsu L6301, Japan) which has a strong and continuous emission spectrum in the ultraviolet band is used as the light source of the measurement system. The broad band ultraviolet light emitted by the deuterium lamp is coupled into an anti-ultraviolet (anti-UV) optical fiber whose numerical aperture is 0.22, and the outgoing light of the anti-UV optical fiber is collimated by a parabolic reflector (Thorlabs MPD01M9-F01, USA) and then enters a gas absorption cell. The optical path of the absorption cell is 700 mm.

When the ultraviolet light passes through the gas absorption cell with fused silica window glass, the photons of a specific wave band are absorbed by the gas to be measured. The parabolic reflector and the fused silica window glass absorb little in the ultraviolet band. Photons that aren't absorbed by the gas are focused by another parabolic reflector (Thorlabs MPD01M9-F01, USA) and then coupled into another anti-UV optical fiber. The output end of the optical fiber is connected to an ultraviolet spectrometer (GanWei GW-5040, China) which works in the wavelength range of 180–400 nm with a sampling interval of 0.1 nm.

The gases used in the experiment are from Dalian Special Gases Co., Ltd. The uncertainties of SO<sub>2</sub>, NO<sub>2</sub> and NO are all 2%. The gases in the cylinders pass through pressure reducing

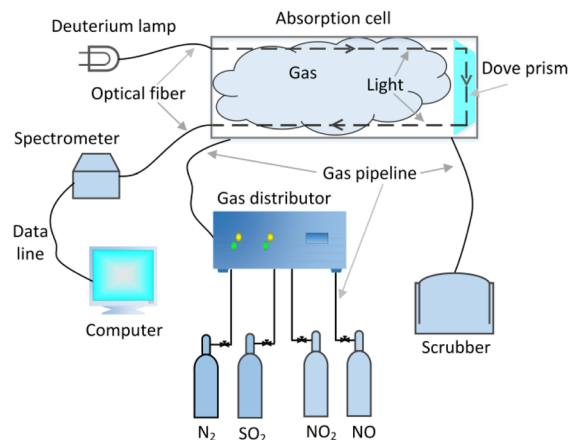


Fig. 2 Schematic diagram of measurement system.<sup>24</sup>

valves and then flow along a gas pipeline to a gas distribution instrument (SWISSGAS Sonimix7100, Switzerland) with an accuracy error of 0.5%. The gas mixed by the gas distributor enters the gas absorption cell. The measured gas is discharged into the atmosphere after tail gas treatment.

The whole experimental process was conducted at room temperature and atmospheric pressure, and the influence of temperature and pressure on the experimental results was relatively small and could be ignored.<sup>1,14</sup>

At the beginning of the experiment, the experimental equipment was turned on to preheat for 30 minutes, and the pressure reducing valves were adjusted to maintain 0.3–0.5 MPa, meeting the input pressure requirement of the gas distributor. During the whole measurement process, the flow rate of the gas flowing into the absorption cell remained unchanged at 350 ml min<sup>-1</sup>.

Then, nitrogen flowed into the gas absorption cell at a flow rate of 350 ml min<sup>-1</sup> for 200 s to ensure that the absorption cell was completely filled with pure nitrogen. Spectral data were collected with the ultraviolet spectrometer. The integration time of the spectrometer was 19 ms to ensure that the spectral signal had a high signal-to-noise ratio and didn't exceed the maximum code value of the spectrometer detector. The spectral signal received at this time by the spectrometer was denoted as  $I_0(\lambda)$ . Then, the absorption spectral signals of the mixed gases were collected, and the operation processes of filling the mixed gases were the same as that of filling nitrogen. The spectral signals of the mixed gases were recorded as  $I(\lambda)$ . 50 groups of spectral data were collected for each measurement.

## 4. Method and results

### 4.1 Signal-gas retrieval express

**4.1.1 NO.** The experiment collected 14 groups of NO gas with concentrations ranging from 42 ppm to 92 ppm. Fig. 3 and 4 show the spectral signals and the absorbances of partial NO concentrations. It can be seen from Fig. 4 that there are obvious absorption peaks for NO at 192.3 nm, 205.5 nm, 215.4 nm, and 226.5 nm. However, the peak value of the NO absorption peak at 192.3 nm was higher than the others.

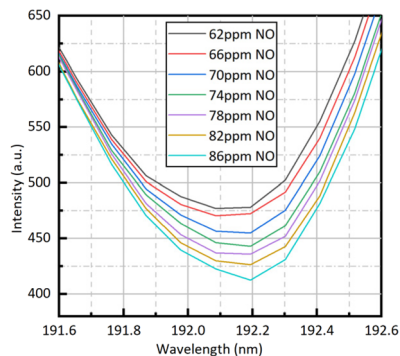


Fig. 3 Absorption spectra of NO with different concentrations.

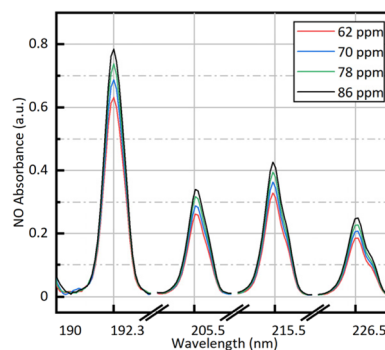


Fig. 4 Absorbance of NO with different concentrations.

Although the deuterium lamp has weak emission intensity at 192.3 nm, the signal-to-noise ratio of its light intensity at 192.3 nm meets the requirement of the gas spectral signal process for signal-to-noise ratio. Since the absorption peaks of NO are discontinuous, the direct absorption spectroscopy method was used to retrieve NO concentrations. The mathematical expression of the direct absorption spectroscopy method is shown in eqn (7). The absorbances at 192.3 nm of different concentrations of NO were fitted with the NO concentrations, and the fitting results are shown in Fig. 5 and eqn (12), where  $A_{\text{NO}}$  is the NO absorbance at 192.3 nm, and  $C_{\text{NO}}$  is the retrieval concentration of NO. The goodness of fit between the NO absorbances at 192.3 nm and the NO concentrations reaches 0.9944. According to the fitting results in Fig. 5 and eqn (12), the NO absorbances at 192.3 nm has a good linear relationship with NO concentrations and the high-precision concentration retrieval of NO can be achieved based on the relationship between the NO absorbances at 192.3 nm and the NO concentrations.

$$C_{\text{NO}} = 143.269 \times A_{\text{NO}} - 27.353 \quad (12)$$

**4.1.2 SO<sub>2</sub>.** As shown in Fig. 1, SO<sub>2</sub> has a large absorption cross-section at 193–225 nm and 275–313 nm, but the SO<sub>2</sub> absorption cross-section at 193–223 nm changes more quickly with wavelength and is larger than that at 275–313 nm.<sup>23</sup> In order to achieve detection under low concentration conditions,

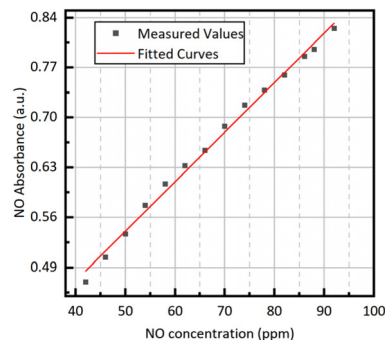


Fig. 5 Relationship between NO concentration and the absorbance at 192.3 nm.



the wavelength range of 193–223 nm with the large SO<sub>2</sub> absorption cross-section is selected as the retrieval wavelength band of SO<sub>2</sub>. The experiment collected 20 groups of SO<sub>2</sub> with different concentrations ranging from 26 ppm to 102 ppm. Fig. 6 shows the absorbances of SO<sub>2</sub> at concentrations of 30 ppm, 50 ppm, and 70 ppm. It can be seen from Fig. 6 that the absorbance increases with increasing SO<sub>2</sub> concentration and changes sharply with wavelength. These provide conditions for the concentration retrieval of SO<sub>2</sub> based on the FFT amplitude method. As shown in Fig. 7, the FFT amplitude at 0.628 nm<sup>-1</sup> of the SO<sub>2</sub> absorbance increases with increasing SO<sub>2</sub> concentration. Therefore, the SO<sub>2</sub> absorbances at 193–223 nm were transformed by FFT and then the FFT amplitudes at 0.628 nm<sup>-1</sup> were fitted with the SO<sub>2</sub> concentrations.<sup>24</sup> The fitting relationship between the FFT amplitudes at 0.628 nm<sup>-1</sup> of SO<sub>2</sub> absorbances and the SO<sub>2</sub> concentrations is shown in Fig. 8 and eqn (13) and their goodness of fit reaches 0.9998. In eqn (13), AMP<sub>SO<sub>2</sub></sub> is the SO<sub>2</sub> FFT amplitude at 0.628 nm<sup>-1</sup>, and C<sub>SO<sub>2</sub></sub> is the retrieval concentration of SO<sub>2</sub>. From the above analysis, it can be concluded that the FFT amplitude at 0.628 nm<sup>-1</sup> of SO<sub>2</sub> absorbance can accurately retrieve SO<sub>2</sub> concentration.

$$C_{\text{SO}_2} = 573.252 \times \text{AMP}_{\text{SO}_2} - 27.561 \quad (13)$$

**4.1.3 NO<sub>2</sub>.** In this paper, the wavelength range of 229.1–254.4 nm was selected as the retrieval wavelength band

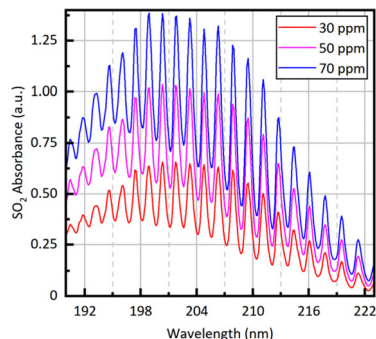


Fig. 6 SO<sub>2</sub> absorbance with different concentrations.

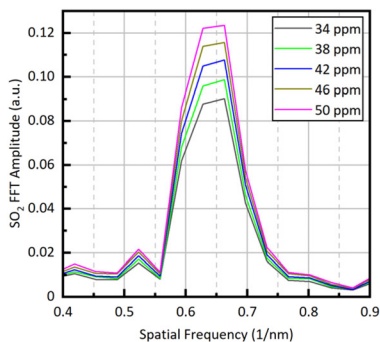


Fig. 7 FFT amplitude of the absorbance at 193–223 nm of SO<sub>2</sub> with different concentrations.

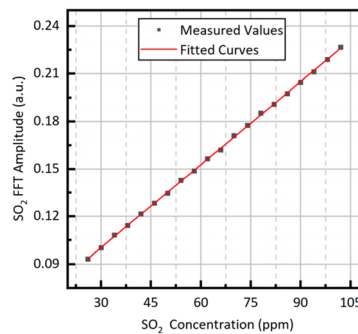


Fig. 8 Relationship between SO<sub>2</sub> concentration and the FFT amplitude at 0.628 nm<sup>-1</sup>.

of NO<sub>2</sub>. As shown in Fig. 1, although NO<sub>2</sub> has a small absorption cross-section at 229.1–254.4 nm, the absorption cross-section of SO<sub>2</sub> in this band is smaller than that of NO<sub>2</sub>, so NO<sub>2</sub> concentration retrieval is less affected by SO<sub>2</sub>. Also, at 229.1–254.4 nm, the deuterium lamp is bright, so the absorption spectral signal of NO<sub>2</sub> has a high signal-to-noise ratio. Due to the continuous absorption cross-section of NO<sub>2</sub>, the FFT amplitude method was used to retrieve NO<sub>2</sub> concentration. The experiment collected 13 groups of NO<sub>2</sub> with different concentrations ranging from 40 ppm to 88 ppm. Fig. 9 and 10 show the absorbances and FFT amplitudes of

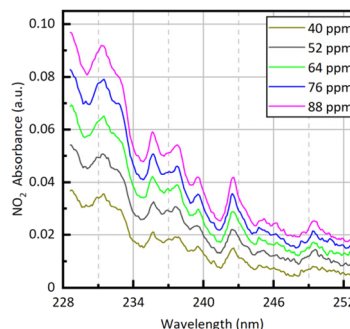


Fig. 9 NO<sub>2</sub> absorbance with different concentrations.

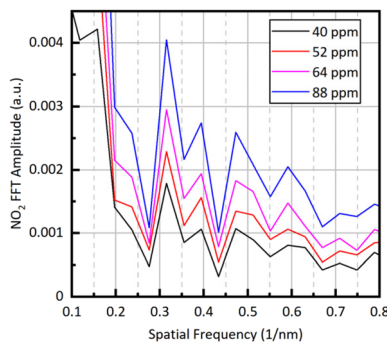


Fig. 10 FFT amplitude of the absorbance at 229.1–254.4 nm of NO<sub>2</sub> with different concentrations.

partial concentrations of  $\text{NO}_2$ , respectively. It can be seen from Fig. 9 and 10 that the absorbance and FFT amplitude of  $\text{NO}_2$  increase with increasing  $\text{NO}_2$  concentration. The FFT amplitudes at  $0.315 \text{ nm}^{-1}$  of  $\text{NO}_2$  absorbance were fitted with the  $\text{NO}_2$  concentrations; the fitting results are shown in Fig. 11 and eqn (14), and their goodness of fit reaches 0.9963. In eqn (14),  $\text{AMP}_{\text{NO}_2}$  is the  $\text{NO}_2$  FFT amplitude at  $0.315 \text{ nm}^{-1}$ , and  $C_{\text{NO}_2}$  is the retrieval concentration of  $\text{NO}_2$ . From the above analysis, it can be seen that the FFT amplitude of  $\text{NO}_2$  absorbance can be used for  $\text{NO}_2$  concentration retrieval.

$$C_{\text{NO}_2} = 20\,022.245 \times \text{AMP}_{\text{NO}_2} + 5.348 \quad (14)$$

## 4.2 Binary-gases retrieval express

**4.2.1  $\text{SO}_2$  concentration retrieval.** In the wavelength range of 193–223 nm,  $\text{SO}_2$  has a larger absorption cross-section than  $\text{NO}_2$  and  $\text{NO}$ , so  $\text{SO}_2$  is less influenced by  $\text{NO}$  and  $\text{NO}_2$  within the emission concentration range required by the rules. Moreover, in this paper, the FFT amplitude method is used to retrieve  $\text{SO}_2$  concentration, which further reduces the influence of  $\text{NO}_2$  and  $\text{NO}$  on the retrieval accuracy of  $\text{SO}_2$ . Just like single  $\text{SO}_2$  concentration retrieval, the FFT amplitude at  $0.628 \text{ nm}^{-1}$  of the absorbance at 193–223 nm was selected as the eigenvalue for the concentration retrieval of  $\text{SO}_2$  mixed with  $\text{NO}_2$  or  $\text{NO}$ .

In order to study the influence of  $\text{NO}_2$  on  $\text{SO}_2$  concentration retrieval, the spectral data of gas mixtures with different concentrations of  $\text{SO}_2$  and  $\text{NO}_2$  were collected in the experiment. When the concentrations of  $\text{SO}_2$  were 24 ppm and 52 ppm, the concentration range of  $\text{NO}_2$  was from 20 ppm to 52 ppm at intervals of 4 ppm. The results of this experiment are shown in Fig. 12. It can be seen from Fig. 12 that, no matter how the concentration of  $\text{NO}_2$  changes in the mixed gases of  $\text{NO}_2$  and  $\text{SO}_2$ , there is no significant change in the eigenvalues of  $\text{SO}_2$  which represent the concentration information of  $\text{SO}_2$ . Therefore, in the process of  $\text{SO}_2$  concentration retrieval, the influence of  $\text{NO}_2$  on  $\text{SO}_2$  concentration retrieval can be ignored.

In order to study the influence of  $\text{NO}$  on the concentration retrieval of  $\text{SO}_2$ , the data collection process of the mixed gases of  $\text{SO}_2$  and  $\text{NO}$  in the experiment is as follows. 45 ppm  $\text{SO}_2$

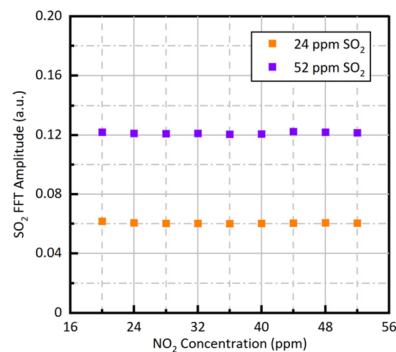


Fig. 12 Influence of  $\text{NO}_2$  concentration change on the  $\text{SO}_2$  FFT amplitude at  $0.628 \text{ nm}^{-1}$ .

and  $\text{NO}$  with different concentrations were filled into the absorption cell, and the concentration range of  $\text{NO}$  was from 40 ppm to 104 ppm at intervals of 4 ppm. The data processing process of  $\text{NO}$  and  $\text{SO}_2$  mixed gases was similar to that of  $\text{SO}_2$  and  $\text{NO}_2$  mixed gases, and the data processing results are shown in Fig. 13. It can be seen from Fig. 13 that  $\text{NO}$  has hardly any influence on the eigenvalues of  $\text{SO}_2$  concentration, so the influence of  $\text{NO}$  on the concentration retrieval of  $\text{SO}_2$  can be ignored.

**4.2.2  $\text{NO}_2$  concentration retrieval.** Just like the concentration retrieval process of single  $\text{NO}_2$  gas, the wavelength range of 229.1–254.4 nm was selected as the retrieval wavelength band of  $\text{NO}_2$  in the mixed gases, and the FFT amplitude at  $0.315 \text{ nm}^{-1}$  of the absorbance in this band was used as the eigenvalue for the concentration retrieval of  $\text{NO}_2$  mixed with  $\text{SO}_2$  or  $\text{NO}$ .

As shown in Fig. 1,  $\text{NO}_2$  has a large differential absorption cross-section in this band and the spectral signal of other gases is weak, so this band has better conditions for extracting concentration eigenvalues than other bands. The experiment collected the spectral signals of different concentrations of  $\text{NO}_2$  and  $\text{SO}_2$  gas mixtures. The concentrations of  $\text{NO}_2$  are 36 ppm and 52 ppm, and the concentration range of  $\text{SO}_2$  is from 20 ppm to 52 ppm at intervals of 4 ppm. The relationship between the concentration eigenvalues of the  $\text{NO}_2$  and  $\text{SO}_2$  concentrations is shown in Fig. 14. As shown in Fig. 14, the

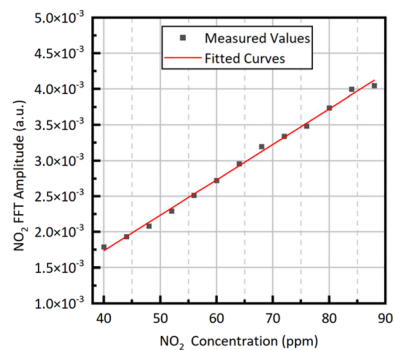


Fig. 11 Relationship between  $\text{NO}_2$  concentration and the FFT amplitude at  $0.315 \text{ nm}^{-1}$ .

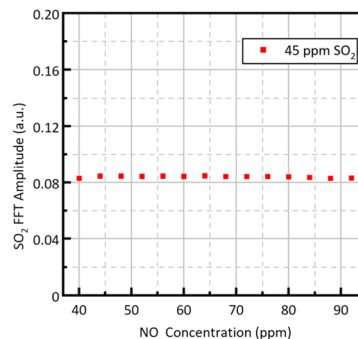


Fig. 13 Influence of  $\text{NO}$  concentration change on the  $\text{SO}_2$  FFT amplitude at  $0.628 \text{ nm}^{-1}$ .

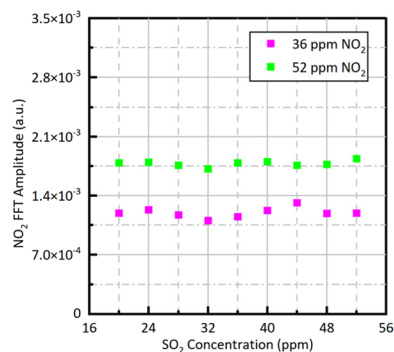


Fig. 14 Influence of  $\text{SO}_2$  concentration change on the  $\text{NO}_2$  FFT amplitude at  $0.315 \text{ nm}^{-1}$ .

concentration eigenvalues of  $\text{NO}_2$  don't show significant change with the changes of  $\text{SO}_2$  concentration. Therefore, the FFT amplitude at  $0.315 \text{ nm}^{-1}$  of the absorbance at  $229.1\text{--}254.4 \text{ nm}$  can effectively reduce the influence of  $\text{SO}_2$  on the concentration retrieval of  $\text{NO}_2$ .

The experiment collected the spectral signals of mixtures of  $50 \text{ ppm NO}_2$  and different concentrations of  $\text{NO}$ . The concentration range of  $\text{NO}$  is from  $40 \text{ ppm}$  to  $112 \text{ ppm}$  at intervals of  $4 \text{ ppm}$ . Just like the data processing process for single  $\text{NO}_2$ , the FFT amplitude at  $0.315 \text{ nm}^{-1}$  of the absorbance at  $229.1\text{--}254.4 \text{ nm}$  was used as the eigenvalue for  $\text{NO}_2$  concentration retrieval. The measurement results are shown in Fig. 15 and show that the concentration retrieval eigenvalues of  $\text{NO}_2$  don't change with the concentration change of  $\text{NO}$ . This also indicates that the FFT amplitude at  $0.315 \text{ nm}^{-1}$  of the absorbance at  $229.1\text{--}254.4 \text{ nm}$  can avoid the influence of  $\text{NO}$  on the retrieval results of  $\text{NO}_2$  concentration.

**4.2.3 NO concentration retrieval.** The wavelength of  $192.3 \text{ nm}$  is still selected as the retrieval wavelength for  $\text{NO}$  concentration retrieval in mixed gases. Unlike the concentration retrieval process of  $\text{SO}_2$  or  $\text{NO}_2$  in mixed gases, the direct absorption method is used for the concentration retrieval of  $\text{NO}$ . Due to the absorption of  $\text{SO}_2$  and  $\text{NO}_2$  at  $192.3 \text{ nm}$ , it is necessary to remove the absorbances of  $\text{NO}_2$  and  $\text{SO}_2$  at this wavelength by post-processing. Then, the  $\text{NO}$  concentration is retrieved according to eqn (12). Due to the fact that

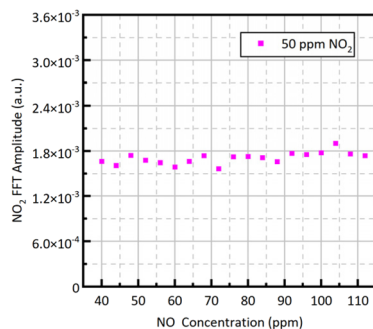


Fig. 15 Influence of  $\text{NO}$  concentration change on the  $\text{NO}_2$  FFT amplitude at  $0.315 \text{ nm}^{-1}$ .

the relationship between the absorbance at  $192.3 \text{ nm}$  and the eigenvalue of the gas concentration is a characteristic of the gas itself, it doesn't change with the change of gas concentration. Therefore, in this paper, the concentration eigenvalue of  $\text{NO}_2$  or  $\text{SO}_2$  is used to calibrate the absorbance of  $\text{NO}_2$  or  $\text{SO}_2$  at  $192.3 \text{ nm}$ .

The experiment collected 26 groups of spectral signals of  $\text{SO}_2$  with different concentrations, ranging from  $42$  to  $142 \text{ ppm}$ . The relationship between the concentration eigenvalues of  $\text{SO}_2$  and the absorbances at  $192.3 \text{ nm}$  is shown in Fig. 16. From Fig. 16, it can be seen that there is a good linear relationship between them, and the absorbance of  $\text{SO}_2$  at  $192.3 \text{ nm}$  can be calibrated by the concentration eigenvalue of  $\text{SO}_2$ . The fitting relationship between them is shown in eqn (15), where  $\text{AMP}_{\text{SO}_2}$  is the  $\text{SO}_2$  FFT amplitude at  $0.628 \text{ nm}^{-1}$  and  $A_{192.3\_SO_2}$  is the  $\text{SO}_2$  absorbance at  $192.3 \text{ nm}$ , and the goodness of fit between them reaches  $0.9989$ .

$$A_{192.3\_SO_2} = 5.733 \times \text{AMP}_{\text{SO}_2} - 0.154 \quad (15)$$

The experiment collected 15 groups of spectral signals of  $\text{NO}_2$  with different concentrations, ranging from  $32 \text{ ppm}$  to  $88 \text{ ppm}$ . Fig. 17 shows the relationship between the concentration eigenvalues of  $\text{NO}_2$  and the absorbances of  $\text{NO}_2$  at  $192.3 \text{ nm}$ . As shown in Fig. 17, there is a linear relationship between the concentration eigenvalues of  $\text{NO}_2$  and the absorbances of  $\text{NO}_2$  at  $192.3 \text{ nm}$ . The relationship between them is

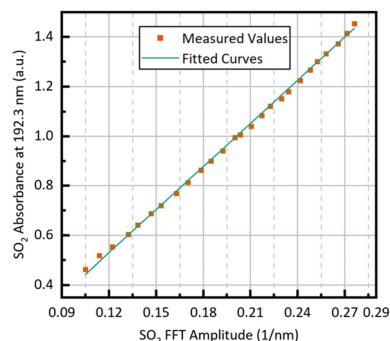


Fig. 16 Relationship between the  $\text{SO}_2$  absorbance at  $192.3 \text{ nm}$  and  $\text{SO}_2$  FFT amplitude at  $0.628 \text{ nm}^{-1}$ .

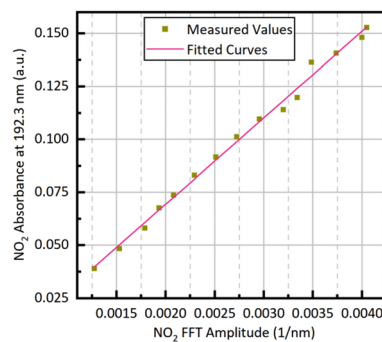


Fig. 17 Relationship between the  $\text{NO}_2$  absorbance at  $192.3 \text{ nm}$  and  $\text{NO}_2$  FFT amplitude at  $0.315 \text{ nm}^{-1}$ .

shown in eqn (16), where  $AMP_{NO_2}$  is the  $NO_2$  FFT amplitude at  $0.315\text{ nm}^{-1}$  and  $A_{192.3\_NO_2}$  is the  $NO_2$  absorbance at  $192.3\text{ nm}$ , and the goodness of fit between them reaches  $0.9941$ .

$$A_{192.3\_NO_2} = 40.819 \times AMP_{NO_2} - 0.012 \quad (16)$$

### 4.3 Retrieval method of ternary-gas

The concentration retrieval process of  $NO$ ,  $NO_2$  and  $SO_2$  mixed gases is shown in Fig. 18. Its detailed process description is as follows.

(1) The absorbance of the mixed gases at  $193\text{--}223\text{ nm}$  is FFT transformed, and then the  $SO_2$  concentration in the mixed gases is calculated by the FFT amplitude at  $0.628\text{ nm}^{-1}$  and eqn (13).

(2) The absorbance of mixed gases at  $229.1\text{--}254.4\text{ nm}$  is FFT transformed, and then the  $NO_2$  concentration in the mixed gases is calculated by the FTT amplitude at  $0.315\text{ nm}^{-1}$  and eqn (14).

(3) The absorbance at  $192.3\text{ nm}$  of the  $SO_2$  in mixed gases is obtained by eqn (15) and the FFT amplitude at  $0.628\text{ nm}^{-1}$  which was obtained from Step 1.

(4) The absorbance at  $192.3\text{ nm}$  of the  $NO_2$  in mixed gases is obtained by eqn (16) and the FFT amplitude at  $0.315\text{ nm}^{-1}$  which was obtained from Step 2.

(5) The  $NO$  concentration in the mixed gases can be calculated by eqn (12).

### 4.4 Verification of the ternary-gas retrieval method

The spectral signals of gas mixtures with different concentrations of  $NO$ ,  $NO_2$ , and  $SO_2$  were collected in the experiment, and the concentrations of each component gas were retrieved according to the flowchart shown in Fig. 18. The retrieval results and measured concentrations of each component are shown in Table 1, where  $C_s$  is the setting concentration,  $C_d$  is the retrieval concentration, and  $|\Delta C|$  is the absolute value of relative deviations. In Table 1, the maximum absolute values of the relative deviations for the concentration retrieval of  $SO_2$ ,  $NO_2$ , and  $NO$  in ternary-gas mixtures are  $3.868\%$ ,  $4.740\%$ , and  $5.009\%$ , respectively. From the data in Table 1, it can be seen that the process in Fig. 18 can perform high-precision concentration retrieval of  $NO$ ,  $NO_2$  and  $SO_2$  mixed gases.

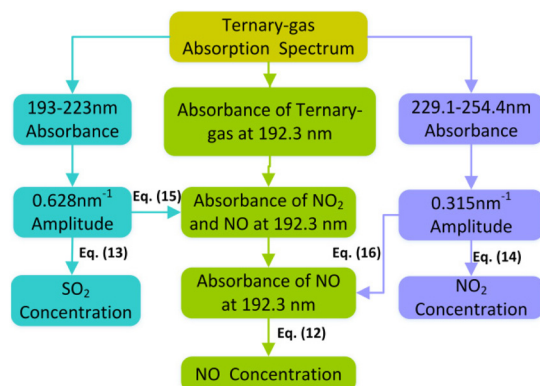


Fig. 18 Flow chart of ternary-gas concentration retrieval.

Table 1 Results of ternary-gas concentration retrieval

SO <sub>2</sub> (ppm)			NO <sub>2</sub> (ppm)			NO (ppm)		
<i>C<sub>s</sub></i>	<i>C<sub>d</sub></i>	$ \Delta C $ (%)	<i>C<sub>s</sub></i>	<i>C<sub>d</sub></i>	$ \Delta C $ (%)	<i>C<sub>s</sub></i>	<i>C<sub>d</sub></i>	$ \Delta C $ (%)
25	25.967	3.868	28	26.673	4.739	28	27.633	1.311
28	28.110	0.393	32	31.207	2.478	26	24.813	4.565
30	29.650	1.167	35	34.061	2.683	24	22.798	5.008
35	35.312	0.891	38	36.264	4.568	20	19.058	4.710

## 5. Conclusions

In this paper, different wavelength bands were selected for the concentration retrieval of different gases: the wavelength range of  $193\text{--}223\text{ nm}$  was selected for  $SO_2$  concentration retrieval, because  $SO_2$  has a large absorption cross-section in this band; as  $NO_2$  has a big differential absorbance at the wavelength range of  $229.1\text{--}254.4\text{ nm}$ , this band was selected as the concentration retrieval range of  $NO_2$ ; and the wavelength of  $192.3\text{ nm}$  was selected as the concentration retrieval wavelength of  $NO$ . The FFT amplitude method was used for the concentration retrievals of  $NO_2$  and  $SO_2$  and the direct absorption method was used for the concentration retrieval of  $NO$ . The spectral signals of  $SO_2$ ,  $NO_2$ , and  $NO$  in mixed gases were effectively separated by selecting different wavelength bands and using different retrieval methods. The experimental results show that the concentration retrieval of ternary-gas can be achieved based on the flowchart in Fig. 18. This study makes it possible to accurately and quantitatively analyze the concentrations of  $SO_2$ ,  $NO_2$  and  $NO$  mixed gases based on ultraviolet absorption spectroscopy. These methods possess the potential to be applied to online flue detection equipment.

## Author contributions

Yibiao Yang: conceptualization, methodology, software, investigation, writing-original draft. Jinhuan Li: data curation, formal analysis, writing-review. Zihui Zhang: editing and visualization, validation. Jianing Wang: resources and supervision. Guanyu Lin: project administration and funding acquisition.

## Conflicts of interest

There are no conflicts to declare.

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