

# Understanding efficiency improvements of betavoltaic batteries based on 4H-SiC, GaN, and diamond

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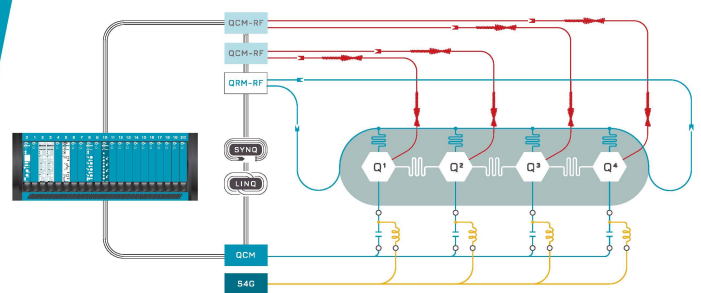
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# Understanding efficiency improvements of betavoltaic batteries based on 4H-SiC, GaN, and diamond

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## ABSTRACT

Wide-bandgap semiconductors are more advantageous for betavoltaic batteries due to their high conversion efficiency and strong radiation resistance. However, there has been little comprehensive analysis of how wide-bandgap semiconductors lead to efficiency improvements. In this work, we proposed a simulation model to predict the output performance of betavoltaic batteries based on 4H-SiC, hexagonal-GaN, and diamond, in which the Monte Carlo code and COMSOL Multiphysics software were combined. The energy deposition of a <sup>63</sup>Ni source in semiconductors and the electrical characteristics of p-n junctions were investigated and compared. Our simulation results showed that the mass density and atomic number of semiconductor materials will cause the difference in energy deposition distribution, further leading to the different electron-hole pair generation rates. Then, the internal efficiency of batteries is co-determined by the energy band structure, depletion region width, built-in potential barrier, and minority carrier lifetime. The batteries based on wide-bandgap semiconductors can achieve the larger open-circuit voltage, further leading to higher efficiency. Additionally, to optimize the energy converter structure, the output parameters were calculated with a variation of doping concentrations and thicknesses of each region. Under the irradiation of a <sup>63</sup>Ni source, the diamond-based battery with a p-n junction structure has the highest internal efficiency of 31.3%, while the GaN-based battery has the lowest one (16.8%), which can be attributed to the larger carrier recombination rate.

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In recent years, radioisotope micro-batteries have attracted much attention in the field of low-power devices, where micro-power sources with long service life, small scale, and high power density are urgently needed.<sup>1,2</sup> They typically consist of a radioactive source and a semiconductor energy converter, the radioactive source can be an x ray, gamma-ray, alpha particle, or beta particle source, and the semiconductors generally include Si, GaAs, GaP, SiC, GaN, diamond, etc.<sup>3,4</sup> Due to their advantages of easy shielding and small radiation damage, the betavoltaic batteries are more attractive than other types, and they can convert the decay energy into electrical energy in a similar way to solar cells. Researchers have done theoretical and experimental studies on the battery performance, and considerable efforts have been

devoted to the optimization design in terms of semiconductor materials and device structures.<sup>5,6</sup>

Si-based betavoltaic batteries were first studied due to their mature technology and low cost.<sup>7</sup> However, the low conversion efficiency and poor radiation resistance limited their application space.<sup>1,4</sup> Theoretical studies showed that using wide-bandgap semiconductors is beneficial to improve the conversion efficiency of batteries,<sup>8</sup> so the focus of researchers gradually turned toward the batteries based on wide-bandgap semiconductors. As a III-V compound semiconductor, GaAs was an excellent material for space solar cells, and it was also suitable for betavoltaic batteries.<sup>9</sup> Unfortunately, the minority carrier diffusion lengths of GaAs are too small, this means multiple devices

need to be connected in series to improve the collection efficiency.<sup>4</sup> Semiconductors with wider bandgap seem to be a better option, and betavoltaic batteries based on SiC,<sup>10,11</sup> GaN,<sup>12,13</sup> and diamond<sup>14,15</sup> have been demonstrated. In 2020, a SiC-based p–n junction battery was fabricated.<sup>16</sup> Under 20 keV electron beam irradiation, the conversion efficiency was measured as 20.17%. In 2021, a GaN-based p–i–n junction battery was reported, and the conversion efficiency was 6.6% under 30 keV electron beam irradiation.<sup>17</sup> In 2020, a betavoltaic battery using a diamond p–n junction achieved a semiconductor conversion efficiency of 28% under 20 keV electron beam irradiation.<sup>18</sup> These are the highest values ever reported for betavoltaic batteries.

From these reports, the batteries based on wide-bandgap semiconductors exhibit better output performance, and the conversion efficiency increases with increasing bandgap, which is well-accepted. Prelas *et al.* defined the driving potential efficiency as the ratio of open-circuit voltage to bandgap, so as to link the transducer efficiency to bandgap.<sup>5</sup> Maximenko *et al.* analyzed the Shockley equation and concluded that an increase in bandgap leads the reverse saturation current density to decrease and the open-circuit voltage to increase, thereby improving the semiconductor conversion efficiency.<sup>19</sup> Zhao *et al.* attributed the high conversion efficiency of batteries based on wide-bandgap semiconductors to the low recombination loss, which is represented by the open-circuit voltage loss.<sup>6</sup> These results explained in different ways how wide-bandgap semiconductors improve the battery efficiency. However, there has been little discussion in terms of the device energy band structure and radiation-induced carrier transport, which directly determine the output performance. Therefore, it is necessary to conduct a systematic investigation to understand the energy conversion process and factors that affect conversion efficiency. This can provide a reference for the selection and evaluation of wide-bandgap semiconductors for betavoltaic batteries.

In this paper, we predicted the output performance of betavoltaic batteries based on wide-bandgap semiconductors by the Monte Carlo N-Particle Transport Code, Version 5 (MCNP5-1.51, 2009.01) and COMSOL Multiphysics software (version: 5.4, 2018.10). The energy deposition of a <sup>63</sup>Ni source and electrical characteristics of p–n junctions in 4H-SiC, hexagonal-GaN, and diamond-based batteries were investigated and compared. Then, the effect of factors on conversion efficiency, including the energy band structure, depletion region width, built-in potential barrier, and carrier generation, recombination, and collection, were systematically analyzed. Moreover, to optimize the energy converter structure, the short-circuit current density, open-circuit voltage, and maximum output power density were calculated with a variation in doping concentrations and thicknesses of each region. This work provides a perspective for understanding the efficiency improvements of betavoltaic batteries by using the wide-bandgap semiconductors.

The output power of a betavoltaic battery depends on the energy deposition of beta particles in semiconductor materials and the collection of radiation-induced electron–hole pairs in energy converters. In this study, the betavoltaic batteries are co-simulated by the Monte Carlo code and COMSOL Multiphysics software, and in order to connect these two parts, the average energy dissipated per electron–hole pair generated ( $E_{ehp}$ ) is used to estimate the electron–hole pair generation rate distribution from the energy deposition distribution.<sup>20</sup>

The Monte Carlo code is used to simulate the energy deposition distribution of <sup>63</sup>Ni beta particles in semiconductor materials, including 4H-SiC, hexagonal-GaN, and diamond. Previous studies have shown

that as the source thickness increases, the apparent power density reaches saturation due to the self-absorption effect.<sup>21</sup> Therefore, a rectangular <sup>63</sup>Ni source with an optimal thickness of 2  $\mu\text{m}$  and a full energy spectrum are used in the simulation model (a cross-sectional area of  $1 \times 1 \text{ cm}^2$  and a total activity density of  $100 \text{ mCi/cm}^2$ ). In order to ensure complete energy deposition, the total thickness of the semiconductor material bulk is set as 0.5 cm (a cross-sectional area of  $1 \times 1 \text{ cm}^2$ ). The number of particles simulated is  $10^8$ , and the error is below 0.01.

The energy deposition rates in semiconductor materials vs the radiation transport depth are shown in Fig. 1(a) and also the accumulation energy deposition distributions. It is seen that the energy deposition rate decreases rapidly with increasing depth, especially in GaN due to its largest mass density. This means that the beta energy is mainly deposited near the material surface; thus, a shallow junction is more appropriate when designing the semiconductor energy converters. Figure 1(a) also shows that the accumulation energy deposition increases with depth, eventually reaching saturation. According to the definition of penetration depth that the position where 99% of the total energy is deposited,<sup>22</sup> the specific values are 7.5, 4.1, and 7.2  $\mu\text{m}$  in 4H-SiC, GaN, and diamond, respectively. In addition, the total energy deposition power density is largest in diamond ( $1.53 \mu\text{W/cm}^2$ ), followed by 4H-SiC ( $1.44 \mu\text{W/cm}^2$ ) and GaN ( $1.27 \mu\text{W/cm}^2$ ). This can

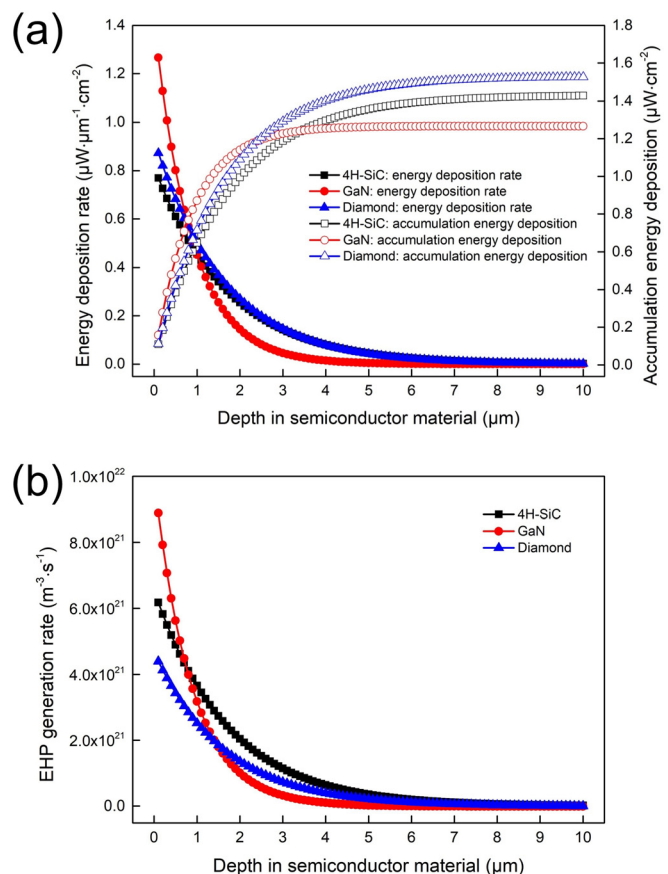


FIG. 1. (a) Energy deposition distributions of <sup>63</sup>Ni beta particles and (b) electron–hole pair (EHP) generation rate distributions in 4H-SiC, GaN, and diamond.

be explained considering the backscattering losses of beta particles. The energy backscattering coefficient depends on the atomic number of semiconductor materials, and it is 11.8% for diamond ( $Z=6$ ), 19.8% for 4H-SiC ( $Z=10$ ), and 32.5% for GaN ( $Z=19$ ).

Furthermore, the electron-hole pair (EHP) generation rates in semiconductor materials vs the radiation transport depth are obtained, as shown in Fig. 1(b). The EHP generation rate decreases exponentially with increasing radiation transport depth ( $Y$ ), and it is expressed as

$$G(Y) = \frac{E(Y)}{E_{\text{ehp}}} = G_0 \exp(-\alpha Y), \quad (1)$$

where  $E(Y)$  is the energy deposition rate from Fig. 1(a),  $E_{\text{ehp}}$  is the average energy dissipated per electron-hole pair generated, and  $G_0$  and  $\alpha$  are the exponential fitting parameters, as listed in Table I. It should be noted that the predicted values for  $E_{\text{ehp}}$  from the Klein formula are different than the measured values especially for wider bandgap semiconductors. Therefore, the measured values reported in the literature are used,<sup>5</sup> which agree with the predicted values from the Bertuccio-Maiocchi-Barnett (BMB) relationship.<sup>23</sup>

COMSOL Multiphysics software is used to simulate the electrical characteristics of energy converters, and the p-n junctions based on 4H-SiC, hexagonal-GaN, and diamond are modeled. To obtain a fast computation time, the cross-sectional area of a device is set as  $1 \times 1 \mu\text{m}^2$ , and the total thickness is set as  $30 \mu\text{m}$ . The thicknesses of the p-region and n-region are variables, denoted as  $H_{\text{p-region}}$  and  $H_{\text{n-region}}$ , respectively. The acceptor concentration of the p-region and the donor concentration of the n-region are denoted as  $N_a$  and  $N_d$ , respectively. In the following simulations, these structure parameters will be optimized to maximize the battery output power.

To simulate the transport and collection of radiation-induced carriers, the Poisson and carrier continuity equations are solved as<sup>24–26</sup>

$$\nabla^2 V = -\frac{\rho}{\epsilon_0 \epsilon_r}, \quad (2)$$

$$-\frac{1}{q} \nabla j_n = G - R_n, \quad (3)$$

$$\frac{1}{q} \nabla j_p = G - R_p, \quad (4)$$

where  $\rho$  is the charge density,  $\epsilon_r$  is the relative permittivity of material,  $V$  is the electrostatic potential,  $\epsilon_0$  is the vacuum permittivity,  $R_n$  ( $R_p$ ) is the electron (hole) recombination rate,  $G$  is the electron-hole pair generation rate, and  $q$  is the electron charge.  $j_n$  ( $j_p$ ) is the electron (hole) current density, and it is expressed as

$$j_n = -\frac{\mu_n kT}{q} \nabla n + \mu_n n \nabla V, \quad (5)$$

**TABLE I.** The  $E_{\text{ehp}}$  of semiconductor materials and the fitting parameters of the electron-hole pair generation rate.

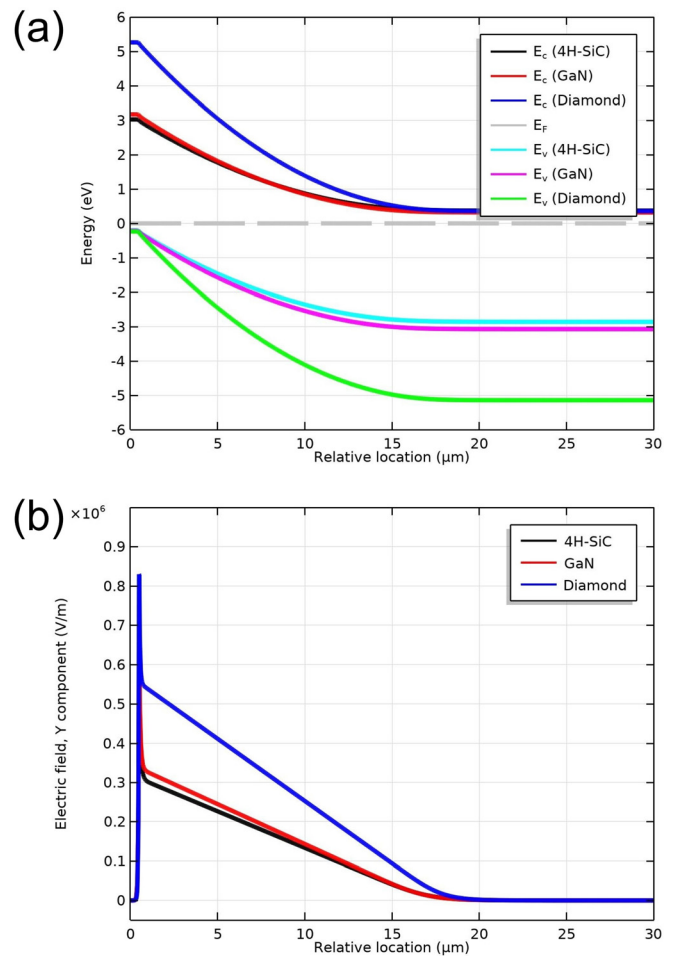
Materials	$E_{\text{ehp}}$ (eV) <sup>5</sup>	$G_0$ ( $\times 10^{21} \text{m}^{-3} \cdot \text{s}^{-1}$ )	$\alpha$ ( $\mu\text{m}^{-1}$ )
4H-SiC	7.78	6.5443	0.581 59
GaN	8.9	9.9560	1.142 19
Diamond	12.4	4.6726	0.615 91

$$j_p = -\frac{\mu_p kT}{q} \nabla p - \mu_p p \nabla V, \quad (6)$$

where  $\mu_n$  ( $\mu_p$ ) is the electron (hole) mobility,  $n$  ( $p$ ) is the electron (hole) concentration,  $T$  is the absolute temperature, and  $k$  is Boltzmann's constant.

In addition, various physical models are employed to define additional components. For example, the background concentration and the main p and n regions of the device are defined by the analytic doping model. The changes in minority carrier mobility with doping concentration are calculated by the low-field mobility model.<sup>27–29</sup> The trap-assisted recombination is defined by the Shockley-Read-Hall (SRH) recombination model. The electron-hole pair generation is defined according to the Monte Carlo simulation results (Figure 1 and Table I, the p-region is the incident position of beta particles). In the COMSOL calculations, the tolerance is less than  $10^{-6}$ .

Figure 2(a) shows the energy diagram of the batteries based on 4H-SiC, GaN, and diamond at thermodynamic equilibrium. In the



**FIG. 2.** (a) Energy diagram and (b) electric field Y-component distribution of the batteries based on 4H-SiC, GaN, and diamond at thermodynamic equilibrium. The  $H_{\text{p-region}}$ ,  $H_{\text{n-region}}$ ,  $N_a$ , and  $N_d$  values are  $0.5 \mu\text{m}$ ,  $29.5 \mu\text{m}$ ,  $1 \times 10^{16} \text{cm}^{-3}$ , and  $1 \times 10^{13} \text{cm}^{-3}$ , respectively.

space charge region, the conduction band ( $E_c$ ) and the valence band ( $E_v$ ) are bent, and an energy potential barrier (built-in potential barrier) is formed. The diamond-based battery has the highest energy potential barrier of 4.91 eV, followed by the GaN-based battery (2.86 eV) and 4H-SiC-based battery (2.66 eV). This observation can be explained by the wider bandgap bringing the lower intrinsic carrier concentration, and then the higher energy potential barrier can be obtained, which is beneficial to achieve a larger open-circuit voltage.

In the p-n junction batteries, the transport and collection of radiation-induced carriers are affected by the electric field Y-component (normal to the junction plane) distribution. As shown in Fig. 2(b), the electric field is mainly distributed in the depletion region (the positive direction is the n-region pointing to the p-region), where the radiation-induced electron-hole pairs can be separated. The variation in the electric field intensity with position agrees with the band bending in Fig. 2(a). In addition, the depletion region widths are 16.9, 16.8, and 17.6  $\mu\text{m}$  for 4H-SiC-, GaN-, and diamond-based batteries, respectively, indicating that the electron-hole pairs can be collected effectively.

In order to evaluate the battery performance, the current density-voltage ( $J$ - $V$ ) characteristics are extracted by sweeping the forward voltage across the device. The current density-voltage ( $J$ - $V$ ) and power density-voltage ( $P$ - $V$ ) characteristics of the batteries based on 4H-SiC, GaN, and diamond are shown in Fig. 3(a). It is observed that the 4H-SiC-based battery has the largest short-circuit current density ( $J_{sc}$ ) of 156  $\text{nA}/\text{cm}^2$ , which can be attributed to the smallest  $E_{ehp}$  (7.78 eV) bringing the most electron-hole pairs generated in the energy converter. In contrast, the total energy deposition power

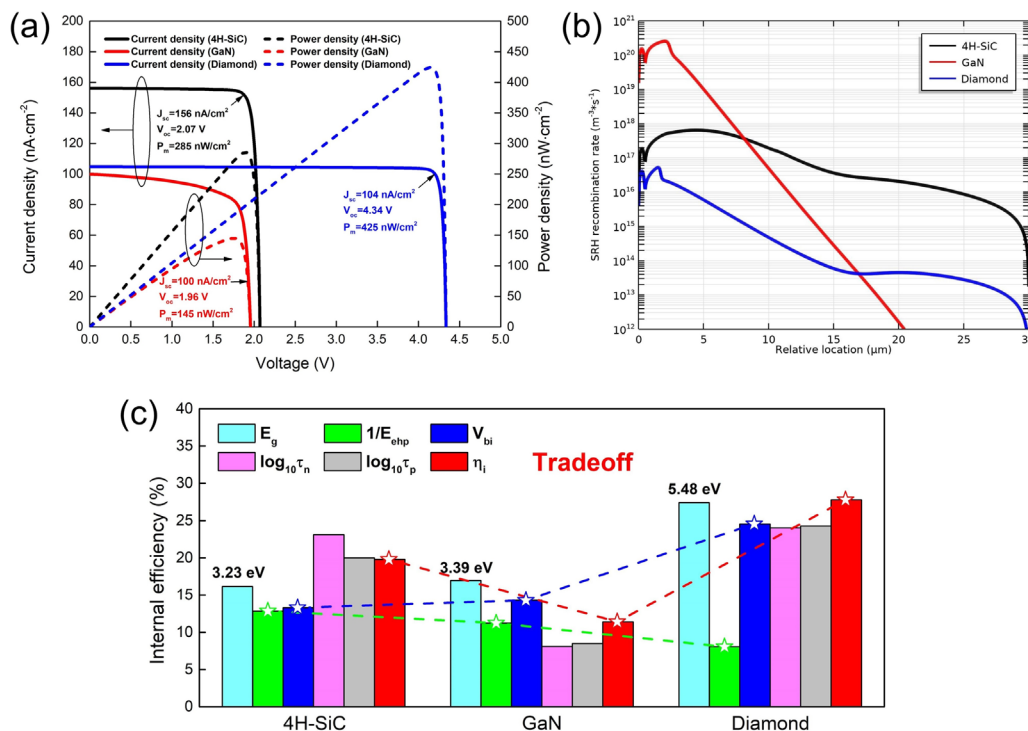
density is largest in diamond (1.53  $\mu\text{W}/\text{cm}^2$ ), but the  $E_{ehp}$  of 12.4 eV suggests a rather low electron-hole pair generation rate. In terms of the open-circuit voltage ( $V_{oc}$ ), the highest built-in potential barrier (4.91 V) of the diamond-based battery contributes to the largest  $V_{oc}$  of 4.34 V, further leading to the largest maximum output power density ( $P_m$ ) of 425  $\text{nW}/\text{cm}^2$ .

In addition, the carrier recombination has significant effects on the battery performance, which depends on the minority carrier lifetime. In our simulation model, the lifetime values ( $\tau_n$  and  $\tau_p$ ) are based on the current technology reported in the literature.<sup>27,28,30</sup> The Shockley-Read-Hall (SRH) recombination rates across the batteries based on 4H-SiC, GaN, and diamond are shown in Fig. 3(b). When the doping concentrations are  $N_a = 1 \times 10^{16}$  and  $N_d = 1 \times 10^{13} \text{ cm}^{-3}$ , the minority carrier lifetimes ( $\tau_n$  and  $\tau_p$ ) in GaN are less than 1 ns, while they are more than 100 ns in 4H-SiC and diamond. The relatively small carrier lifetimes result in the larger recombination rate, especially around the p-region, where the beta particles are incident and the EHP generation rate is higher. This is why the GaN-based battery has the smallest  $V_{oc}$  and  $P_m$  in Fig. 3(a).

We define the battery internal efficiency ( $\eta_i$ ) by the following equation, which represents the ability to convert absorbed energy into electrical energy:

$$\eta_i = \frac{P_m}{P_{in}}, \quad (7)$$

where  $P_{in}$  is the total energy deposition power density entering the semiconductor material from the radioactive beta source. Then, the



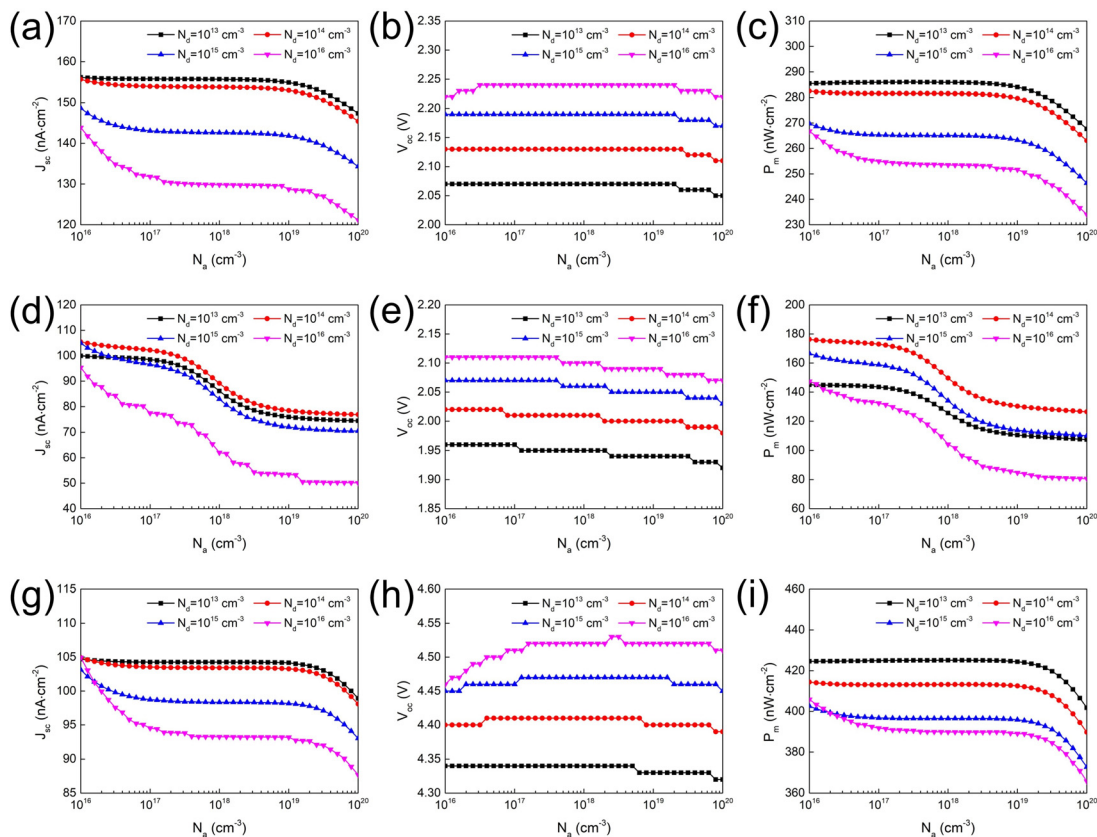
**FIG. 3.** (a)  $J$ - $V$  and  $P$ - $V$  characteristics. (b) Shockley-Read-Hall (SRH) recombination rates. (c) Internal efficiency ( $\eta_i$ ) difference of the batteries based on 4H-SiC, GaN, and diamond, and changes in  $E_g$ ,  $E_{ehp}$ ,  $V_{bi}$ ,  $\tau_n$ , and  $\tau_p$ . The  $H_p$ -region,  $H_n$ -region,  $N_a$ , and  $N_d$  values are 0.5  $\mu\text{m}$ , 29.5  $\mu\text{m}$ ,  $1 \times 10^{16} \text{ cm}^{-3}$ , and  $1 \times 10^{13} \text{ cm}^{-3}$ , respectively.



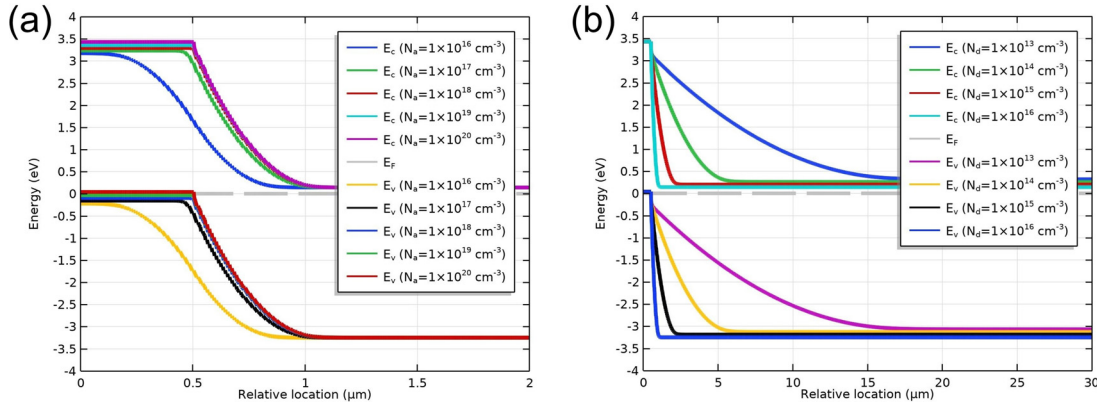
internal efficiency difference of the batteries based on 4H-SiC, GaN, and diamond is shown in Fig. 3(c). The changes in bandgap ( $E_g$ ), average energy dissipated per electron-hole pair generated ( $E_{ehp}$ ), built-in potential barrier ( $V_{bi}$ ), minority electron lifetime ( $\tau_n$ ), and minority hole lifetime ( $\tau_p$ ) are also plotted. For comparison, the reciprocal or logarithmic values of some parameters are taken, and the effects of  $1/E_{ehp}$ ,  $V_{bi}$ ,  $\log_{10}\tau_n$ , and  $\log_{10}\tau_p$  on  $\eta_i$  are shown. (A large value indicates a large contribution.) Since the dimensions of each parameter are different, the height of bar chart only shows the relative sizes for different semiconductor materials. It is clear to see that from the 4H-SiC-based battery to diamond-based battery, the contribution of  $1/E_{ehp}$  to  $\eta_i$  decreases, correspondingly the electron-hole pair generation rate decreases. Conversely, the contribution of  $V_{bi}$  increases, which is beneficial to achieve a larger  $V_{oc}$ . It can also be seen that for the GaN-based battery, the  $\tau_n$  and  $\tau_p$  contribute very little, further leading to a significant decrease in  $\eta_i$ . In conclusion, the internal efficiency of betavoltaic batteries depends on the trade-off among various factors, and ideally, the batteries based on wide-bandgap semiconductors can achieve a higher efficiency because of the larger open-circuit voltage. However, practically, considering the current technology, the minority carrier lifetimes of some wide-bandgap semiconductors are relatively small.<sup>31</sup> This means smaller minority carrier diffusion lengths and a larger recombination rate, which are disadvantageous to the efficiency

improvements. Therefore, the selection and evaluation of wide-bandgap semiconductors should be based on these simulation results taking into account the realistic parameters.

Generally, the battery performance is also affected by the energy converter structure. Due to the different semiconductor properties (as mentioned above), the effects of doping concentrations and thicknesses of each region on the output parameters of batteries based on different semiconductors are also different. Figure 4 shows the variations in the short-circuit current density ( $J_{sc}$ ), open-circuit voltage ( $V_{oc}$ ), and maximum output power density ( $P_m$ ) depending on the  $N_a$  and  $N_d$  for the batteries based on 4H-SiC, GaN, and diamond. It is seen that the  $J_{sc}$  decreases with increasing  $N_d$ , which can be attributed to the decrease in the depletion region width. To validate this, Figure 5 shows the energy diagram of the GaN-based battery as an example. As  $N_d$  increases, the depletion region extends more in the n-region, where the EHP generation rate is lower, further leading to the decrease in  $J_{sc}$ . In addition, the  $J_{sc}$  also decreases with increasing  $N_d$ , but the GaN-based battery shows a trend of increasing first and then decreasing. This is related to the combined effect of the depletion region extending more in the p-region and depletion region width decreasing. Next, Figs. 4(b), 4(e), and 4(h) show that the  $V_{oc}$  is insensitive to  $N_d$ , and it increases with increasing  $N_d$ , which can be explained by the higher built-in potential barrier (as shown in Fig. 5). Ultimately, as shown in



**FIG. 4.** Variations of (a)  $J_{sc}$ , (b)  $V_{oc}$ , and (c)  $P_m$  dependent on the  $N_a$  and  $N_d$  for the 4H-SiC-based battery. (d)  $J_{sc}$ , (e)  $V_{oc}$ , and (f)  $P_m$  for the GaN-based battery. (g)  $J_{sc}$ , (h)  $V_{oc}$ , and (i)  $P_m$  for the diamond-based battery. The  $H_{p\text{-region}}$  and  $H_{n\text{-region}}$  values are 0.5 and 29.5  $\mu\text{m}$ , respectively.

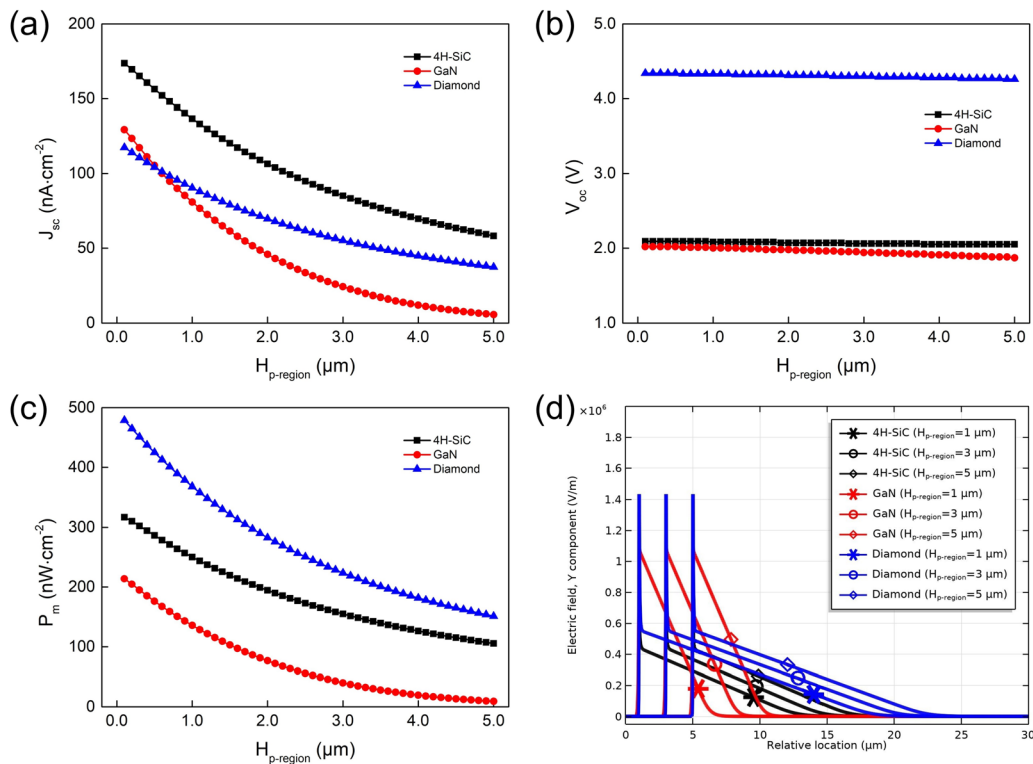


**FIG. 5.** Energy diagram of the GaN-based battery at thermodynamic equilibrium. (a) When  $N_a$  is changed,  $N_d$  is fixed as  $1 \times 10^{16} \text{ cm}^{-3}$ . (b) When  $N_d$  is changed,  $N_a$  is fixed as  $1 \times 10^{20} \text{ cm}^{-3}$ . The  $H_{p\text{-region}}$  and  $H_{n\text{-region}}$  values are 0.5 and 29.5  $\mu\text{m}$ , respectively.

Figs. 4(c), 4(f), and 4(i), the  $P_m$  decreases with increasing  $N_a$ , and it also decreases with increasing  $N_d$  except for the GaN-based battery, which increases first and then decreases.

After determining the optimal values of doping concentrations ( $N_a$  and  $N_d$ ), the variations of  $J_{sc}$ ,  $V_{oc}$ , and  $P_m$  depending on the  $H_{p\text{-region}}$  for the batteries based on 4H-SiC, GaN, and diamond are shown in Figs. 6(a)–6(c). Correspondingly, the electric field Y-component distribution of the batteries at thermodynamic equilibrium is shown in Fig. 6(d).

When  $H_{p\text{-region}}$  increases, the depletion region gets away from the energy converter surface, where the EHP generation rate is higher. As a result, the  $J_{sc}$  decreases, especially for the GaN-based battery, in which the EHP distribution range and depletion region width are smaller. In addition, the rather large  $V_{oc}$  makes the  $P_m$  of diamond-based battery always the largest. To be specific, as  $H_{p\text{-region}}$  increases from 0.1 to 5  $\mu\text{m}$ , the  $P_m$  of diamond-based battery decreases from 479 to 151  $\text{nW}/\text{cm}^2$ , while the  $P_m$  of GaN-based battery decreases from 214  $\text{nW}/\text{cm}^2$  to less than 10



**FIG. 6.** Variations of (a)  $J_{sc}$ , (b)  $V_{oc}$ , and (c)  $P_m$  dependent on the  $H_{p\text{-region}}$  for the batteries based on 4H-SiC, GaN, and diamond. (d) Electric field Y-component distribution of the batteries at thermodynamic equilibrium. When  $H_{p\text{-region}}$  is changed,  $H_{n\text{-region}} = 30 \mu\text{m} - H_{p\text{-region}}$ . The  $N_a$  and  $N_d$  values are optimized.

**TABLE II.** Performance comparison of the batteries based on 4H-SiC, GaN, and diamond.

Semiconductors	$H_{p\text{-region}}$ ( $\mu\text{m}$ )	$H_{n\text{-region}}$ ( $\mu\text{m}$ )	$N_a$ ( $\text{cm}^{-3}$ )	$N_d$ ( $\text{cm}^{-3}$ )	$J_{sc}$ ( $\text{nA}/\text{cm}^2$ )	$V_{oc}$ (V)	$P_m$ ( $\text{nW}/\text{cm}^2$ )	$\eta_i$ (%)
4H-SiC	0.1	29.9	$1 \times 10^{16}$	$2 \times 10^{13}$	174	2.09	317	22.0
GaN	0.1	29.9	$1 \times 10^{16}$	$1 \times 10^{14}$	129	2.02	214	16.8
Diamond	0.1	29.9	$1 \times 10^{17}$	$1 \times 10^{13}$	118	4.34	479	31.3

$\text{nW}/\text{cm}^2$ . These results suggest that a shallow junction is more appropriate for a betavoltaic battery with a p–n junction structure. Finally, the performance comparison of the batteries based on 4H-SiC, GaN, and diamond is listed in Table II. These results agree with experimental values reported in the literature, where the diamond-based p–n junction battery achieved a conversion efficiency of 28%.<sup>18</sup>

In summary, the betavoltaic batteries based on wide-bandgap semiconductors, including 4H-SiC, hexagonal-GaN, and diamond, were modeled, and the output performance and efficiency improvement were evaluated. First, the Monte Carlo code was used to simulate the energy deposition of  $^{63}\text{Ni}$  beta particles in energy conversion materials. The results showed that the energy deposition distribution depends on the mass density and atomic number of the target material for the same radioactive source. The total energy deposition power density of  $1.53 \mu\text{W}/\text{cm}^2$  is largest in diamond. Second, COMSOL Multiphysics software was used to simulate the electrical characteristics of p–n junctions and predict the battery performance. The internal efficiency of betavoltaic batteries depends on the trade-off among various factors, and it is co-determined by the bandgap, average energy dissipated per electron–hole pair generated, depletion region width, built-in potential barrier, and minority carrier lifetime. The calculations showed that the batteries based on wide-bandgap semiconductors can achieve a larger open-circuit voltage and, hence, higher efficiency. However, for some semiconductors with small minority carrier lifetimes limited by current technology, the large recombination rate can lead to a significant decrease in efficiency. In addition, the effects of an energy converter structure on battery output parameters were analyzed. Low doping concentrations are beneficial to enlarge the depletion region width, and then a large short-circuit current density can be obtained. Whereas high doping concentrations lead to a high built-in potential barrier, further enhancing the open-circuit voltage. Finally, the diamond-based battery can achieve the highest internal efficiency of 31.3%. The related  $J_{sc}$ ,  $V_{oc}$ , and  $P_m$  are  $118 \text{ nA}/\text{cm}^2$ ,  $4.34 \text{ V}$ , and  $479 \text{ nW}/\text{cm}^2$ , respectively. These results can provide theoretical references and valuable guidance for the optimization design and experimental fabrication of high-performance betavoltaic batteries. The selection and evaluation of wide-bandgap semiconductors should be based on these simulations considering the realistic parameters.

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## AUTHOR DECLARATIONS

### Conflict of Interest

The authors have no conflicts to disclose.

## Author Contributions

**Renzhou Zheng:** Conceptualization (equal); Data curation (equal); Formal analysis (equal); Investigation (equal); Methodology (equal); Writing – original draft (equal); Writing – review & editing (equal). **Yongyi Chen:** Conceptualization (equal); Software (equal). **Yumin Liu:** Conceptualization (equal). **Jing-Bin Lu:** Conceptualization (equal); Investigation (equal); Methodology (equal); Project administration (equal); Writing – review & editing (equal). **Yu Wang:** Conceptualization (equal); Formal analysis (equal); Investigation (equal); Methodology (equal). **Ziyi Chen:** Conceptualization (equal); Investigation (equal); Methodology (equal). **Xue Zhang:** Conceptualization (equal); Investigation (equal); Methodology (equal). **XiaoYi Li:** Conceptualization (equal); Investigation (equal). **Lei Liang:** Conceptualization (equal); Software (equal). **Li Qin:** Conceptualization (equal); Software (equal). **Yugang Zeng:** Conceptualization (equal); Software (equal).

## DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding authors upon reasonable request.

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