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# Simultaneous robust control and sensor fault detection for a ducted coaxial-rotor UAV

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**ABSTRACT** This paper addresses the aerodynamic modeling, observer-based state-feedback robust control and sensor fault detection for a laboratory ducted coaxial-rotor UAV(DCUAV). First, by introducing the main model elements of this novel unmanned vehicle, the detailed nonlinear mathematical model of the hovering flight UAV is presented. Second, through introducing a weighting matrix and a new form of changeof-variables, a new method is proposed by designing two different systems simultaneously as detector and controller. An observer-based controller is proposed to achieve the control objective and finite-frequency sensor fault detection objective simultaneously. The observer-based controller design method is derived from a new formulation of linear matrix inequality (LMI), which can achieve the prescribed  $H_{\infty}$  performance,  $H_{-}$ performance and the stability of the closed-loop system. By constructing a new matrix decomposition form, the simultaneous design of detector parameters and controller parameters is solved. Finally, simulations are conducted for the hover flight with disturbances and sensor faults, the results show the satisfactory control performance and fault detection performance.

**INDEX TERMS** ducted coaxial rotors, UAV, observer-based, robust control, sensor fault detection, linear matrix inequalities

## I. INTRODUCTION

In recent decades, the development of unmanned aerial vehicles covers a wide range of sizes and capabilities [1-4], which has attracted increased interest in developing control algorithms and fault detection methods. Among various UAVs, the ducted coaxial-rotor UAV(DCUAV) is wellsuited for a variety of flight missions and complex environments. It is capable of high-speed flight in addition to the hover and vertical take-off and landing capabilities. Compared with traditional helicopter, the ducted coaxialrotor UAV will produce greater tension than isolated propeller with the same diameter, which makes the fuselage structure more compact [5-8]. The configuration layout of the ducted coaxial-rotor UAV developed by our laboratory is depicted in Fig.1. The DCUAV is highly unstable and highly nonlinear with complex aerodynamics, which makes the control of the DCUAV present many unique challenges. Furthermore, any undetected sensor faults may degrade the overall system performance, cause catastrophic accidents, and

even threaten flight safety [9-10]. The main mission of our designed DCUAV is surveying and mapping, it is often equipped with photographic equipment. Therefore, in order to achieve high flight performance and fault diagnosis and fault tolerance performance, it is necessary to design a controller with the capability to solve the simultaneous control and fault detection problem.

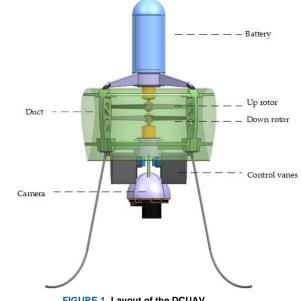
In the literature, various control and detection approaches of the ducted fan aircrafts, coaxial-rotor aircrafts and other types of UAVs, have been developed to achieve flight performances and fault detection objective. Reference [11] used a PID control method, which has a simple control structure, but it has a poor adaptability for the coupling between axes. In [6], by comparing PID, LQR and  $H_{\infty}$  mixed synthesis techniques on linearized sub-plants of a small coaxial helicopter about hover, it is proved that the robust  $H_{\infty}$  controller has better performance in suppressing the disturbances caused by the wind. Backstepping techniques have been used in attitude stabilization [12] and trajectory tracking [13] for small VTOL

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UAVs. An extended state observer-based controller is developed for a coaxial-rotor UAV in [14], where the observer is used to estimate the state and the unknown aerodynamic disturbance. The closed-loop system is stabilized by the interaction of the controller and the observer. Nonlinear dynamic inversion control in [15] and sliding mode control in [16] are designed for one ducted-fan UAV, but both rely on the accuracy of the UAV mathematical model. Neural Network techniques are also presented in many literatures. In [17], a controller combined the neural networks and adaptive backstepping control is designed for a ducted-fan UAV. A neural network based optimal controller for an unmanned helicopter was proposed in [18] to accomplish trajectory tracking. However, the disturbances, uncertainties and faults are not fully taken into consideration, and the majority of their methods have limitations in the engineering application.

On the other hand, the sensor faults usually emerge in lowfrequency domain in our DCUAV flight practice, which is one of the main causes of aircraft system instability and poor flight performance. This motivates the problem of integrated control and fault detection that has attracted significant attention in recent years. A supertwisting-based observer is utilized to estimate the servo's stuck fault for the tilt trirotor UAV in [48]. Based on the proposed observer, a nonlinear FTC controller is developed to maintain the UAV's attitude stability. In [45], the unknown input observer was used to diagnose the icing and actuator faults of a typical small UAV. In [49], an integrated fault tolerant control framework was proposed based on Reduced-order simultaneous state and fault estimator for discrete-time linear time-invariant systems, which was performed at the  $H_{\infty}$  optimization level. Also, the observerbased fault detection and tracking control method was proposed in [46] and [47] for a quadrotor UAV and a planar vertical take-off and landing UAV respectively. By integrating radial base function neural network (RBFNN) with fuzzy sliding mode control, an actuator fault tolerant control technique for a coaxial octorotor UAV was introduced in [19]. In [20], a structured  $H_{\infty}$  controller tuned by a non-smooth optimization algorithm was proposed for a tandem coaxial ducted fan aircraft. The proposed method can recover the desired performance in the presence of actuator fault, disturbance and system uncertainty. Backstepping technique in [21] and adaptive fault tolerant control in [22] are also presented for quadrotor UAVs. However, little attention has been paid to the fault detection and the detection system is often designed separately form flight control system. Therefore, design of fault tolerant control flight system and faults detection system simultaneously has crucial significance in the field of DCUAV research.

In order to achieve flight control objectives and detect faults simultaneously, especially for systems with uncertainties in model,  $H_{\infty}$  control theories and  $H_{-}$  performance index are widely used [24-28]. Since the sensor faults in our UAV flight system usually emerge in low frequency domain, which will make the faults hidden by control actions and difficult to be detected in the early stage [29]. Some finite-frequency fault detector design approaches have been considered in many works by KYP Lemma [30] [31]. With the defined robust performance index and fault sensitivity index, some works have presented the controller and fault detector design as a multi-objective optimization problem [32] [33]. In [34], the simultaneous fault detection and control problem for linear uncertain discrete-time systems has been studied. In [35] and [36], a single unit is designed as





detector/controller to produce the detection and control signals. However, by unifying the control and detection units into a single unit, these schemes may not be able to take both control and detection objectives into account. Further, the system model uncertainties are also not taken into consideration.

Motivated by the aforementioned analysis, a new DCUAV integrated control and sensor fault detection methodology considering the system model uncertainties is introduced based on  $H_{\infty}$  theory,  $H_{-}$  index performance and finitefrequency index performance. The main contributions of this paper are summarized as follows. First, the mathematical model of the ducted coaxial-rotor UAV is obtained by analyzing the aerodynamic forces and moments acting on the vehicle. Second, simultaneous control and sensor fault detection problem is considered, by introducing a new linear change-of-variables, the observer-based controller design conditions can convert into convex optimization problem with linear matrix inequalities. Note that, most papers presented the schemes which were designed to implement fault detection and control by a single unit. Therefore, in some cases, considerations cannot be given to both control objective and detection objective. Third, unlike most articles on faulttolerant control and multi-objective optimization, the proposed method fully considers the parameter uncertainties of the ducted coaxial-rotor UAV model, rather than simply treating it as unknown disturbances. And this mathematic



processing is very meaningful, since the ducted coaxial-rotor UAV has a more complex aerodynamic model. Finally, the strict observer-based controller design condition is developed for guaranteeing the robustness,  $H_{-}$  performance and stability of the flight system in the presence of uncertainties.

This paper is organized as follows: Section 2 presents the dynamical model of the ducted coaxial-rotor UAV. Section 3 considers the simultaneous robust control and sensor fault detection, controller and fault detector design conditions are developed. The simulation results and discussions are presented in Section 4. Finally, the conclusions are provided in Section 5.

Notation: for a matrix  $A, A^T, A^{\perp}$  denote its transpose and orthogonal complement, respectively; denotes *I* the identity matrix with an appropriate dimension; The Hermitian part of a square matrix *A* is denoted by  $He(A) = A + A^T$ ; The symbol \* in a matrix represents the symmetric entries.

# **II. DYNAMIC MODELING OF DCUAV**

In this section, we describe the dynamic model of the ducted coaxial-rotor UAV. Consider the ducted coaxial-rotor UAV depicted in Fig.1 as a solid body incorporating a force and moment generation process. Let  $O_{x_b y_b z_b}$  be the body-fixed frame attached to the center of gravity of the UAV, where  $x_b$ is the longitudinal axis,  $y_b$  is the lateral axis and  $z_b$  is the vertical direction, and  $Ox_g y_g z_g$  be the Earth frame as depicted in Fig. 2. The position and attitude of the UAV in the body-axes coordinate relative to the earth-axes coordinate are usually described by three Euler angles, where  $\varphi$  is the Roll angle (rotation around the x-axis),  $\theta$  is the Pitch angle (rotation around the y-axis), and  $\phi$  is the Yaw angle (rotation around the z-axis). According to the principle of coordinate transfer, the transfer matrix between  $Ox_g y_g z_g$ and  $Ox_b y_b z_b$  is obtained,

$$R_{gb}(\phi,\theta,\varphi) = R_x^T(\varphi)R_y^T(\theta)R_z^T(\phi)$$
$$= \begin{bmatrix} \cos\theta\cos\phi & \cos\theta\sin\phi & -\sin\theta\\ \cos\phi\sin\theta\sin\varphi - \sin\phi\cos\varphi & \sin\phi\sin\theta\sin\phi + \cos\phi\cos\varphi & \cos\theta\sin\phi\\ \cos\phi\sin\theta\cos\varphi + \sin\phi\sin\varphi & \sin\phi\sin\theta\cos\varphi - \cos\phi\sin\varphi & \cos\theta\cos\phi \end{bmatrix}$$
(1)

The accurate flight dynamics model of the ducted coaxial rotorcraft can be expressed by the Newton-Euler formalism:

$$m\dot{v} + m(\omega \times v) = F$$

$$J\dot{\omega} + (\omega \times J\omega) = M$$
(2)

The force and moment vectors can be expressed as:

$$F = F_{grav} + F_{rotor} + F_{vane} + F_{duct}$$

$$M = M_{grav} + M_{rotor} + M_{vane} + M_{gyro}$$
(3)

where all the component forces and moments are discussed below.

# A. GRAVITY

The gravity of the UAV expressed in earth-axes can be as:

$$F_{eg} = \begin{bmatrix} 0 & 0 & mg \end{bmatrix}^T \tag{4}$$

Considering the transformation between the body-axes and the earth-axes, the gravitational force in body-axes coordinate system is given by:

$$F_{grav} = R_{gb}F_{eg} = \begin{vmatrix} mg\cos\varphi\sin\theta \\ -mg\sin\varphi \\ mg\cos\theta\cos\varphi \end{vmatrix}$$
(5)

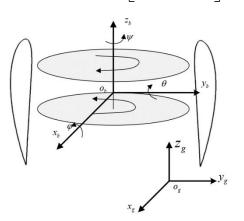


FIGURE 2. Frame system of the DCUAV

#### **B. COAXIAL-ROTORS**

The thrust generated by the coaxial-rotors in the duct can be expressed by the aerodynamic actuator disk theory (Bramwell et al.2001)

$$T_i = \rho C_{T,i} A \left( \omega_i R \right)^2 \tag{6}$$

where  $T_i(i = up, dw)$  are thrusts when the rotor blades spin in the opposite direction,  $\rho$  is the freestream density,

 $C_{T,i}$  is the lift coefficient, A is the rotor disk area,  $\omega_i$  is the angular velocity of the rotor, and R is the radius of the rotor. Since the UAV discussed in this paper uses fixed-pitch rotors,  $C_{T,i}$  is constant like the other parameters in (6) expect the variable  $\omega_i$ . Hence, the force on the

vehicle due to the rotor can now be simplified to

$$F_{rotor} = \begin{bmatrix} 0\\ 0\\ k_{T,up}\omega_{up}^{2} + k_{T,dw}\omega_{dw}^{2} \end{bmatrix}$$
(7)

with  $k_{T,i}$  representing a lumped lift coefficient that needs to be identified. The moments generated by the rotors can apply the similar assumptions and formulations above to establish the relationship with the angular velocity of the rotor:

$$M_{rotor,i} = k_{M,i} \omega_i^2 \tag{8}$$

Since the two rotors rotate in opposite directon, the drag torques of the rotors can be expressed as:

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$$M_{rotor} = \begin{bmatrix} 0\\ 0\\ k_{M,up}\omega_{up}^2 - k_{M,dw}\omega_{dw}^2 \end{bmatrix}$$
(9)

## C. DUCT

In this paper, we use the simplified Bernoulli's principle to analyze the state of 0-1 and 2-3 in hover flight, which is shown in Fig. 3. The expression for the relationship between different states is given as:

$$\begin{cases} p_0 + \frac{1}{2}\rho v_0^2 = p_1 + \frac{1}{2}\rho v_i^2 \\ p_2 + \frac{1}{2}\rho v_i^2 = p_0 + \frac{1}{2}\rho v_e^2 \end{cases}$$
(10)

where  $p_0$ ,  $p_1$ ,  $p_2$  represent the hydrostatic pressure of position 0, 1, and 2.  $v_0$  represents the velocity of the air outside the air cone formed by the rotation of rotors.  $v_i$  represents the rotor induced velocity.  $v_e$  represents the air velocity inside the air cone formed by the rotation of rotors.

Due to the Coanda effect, the airflow tends to follow the direction of the duct contour. As a result, the wake will have a larger area than that of a traditional helicopter. Comparing with a traditional helicopter, the wake of the duct has a larger area, which can provide additional thrust. As shown in [37], the equation to determine the thrust produced by both of the rotors and the duct is given by:

$$T = \dot{m}_{\Delta}v = \rho A v_i \left( v_e - v_0 \right)$$
  

$$T = T_{rotor} + T_{duct}$$
(11)

with:

$$v_i = a_d v_e$$

$$A_e = a_d A$$
(12)

where  $a_d$  represents the radio between the area of the wake and the disc formed by the propellers when they are rotating. The thrust experienced by the duct can be now expressed as:

$$\frac{T_{rotor}}{T} = \frac{1}{2a_d}$$
(13)  
$$T_{duct} = (2a_d - 1)T_{rotor}$$

The force on the vehicle generated by the duct is given as follows:

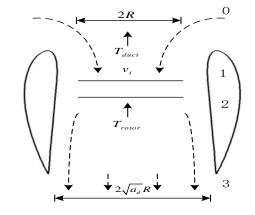


FIGURE 3. Flow schematic diagram

$$F_{duct} = \begin{bmatrix} 0 \\ 0 \\ (2a_d - 1)(k_{M,up}\omega_{up}^2 - k_{M,dw}\omega_{dw}^2) \end{bmatrix}$$
(14)

## D. CONTROL VANES

The control surfaces consist of four sets of vanes with one set in each quadrant of the duct. The configuration of these vanes are shown in the Fig. 4. Vane 1 and vane 3 are deflected symmetrically to control the pitch angle. Similarly, vanes 2 are used for roll control. Vane 1 and vane 3 are deflected differently to realize yaw control.

The rudder control torque is

$$L = \frac{1}{2} \rho v_r^2 S_r C_{Lr} \left( \delta \right) \tag{15}$$

In which  $C_{Lr}$  is dimensionless lift coefficient,  $\upsilon_r$  is the air velocity through the vanes,  $S_r$  is the rudder surface area and  $\delta$  represents the control vane deflection. Hence, the components of the lift forces and the moments created by the forces which are acting in the vehicle's body axes is given as

$$F_{vane} = \begin{bmatrix} \frac{1}{2} \rho v_r^2 S_r C_{Lr} \left(\delta_1\right) + \frac{1}{2} \rho_r v_r^2 S_r C_{Lr} \left(\delta_3\right) \\ \rho_r v_r^2 S_r C_{Lr} \left(\delta_2\right) \\ 0 \end{bmatrix} (16)$$

$$v_{vane} = \begin{bmatrix} \frac{\rho_r v_r^2 S_r C_{Lr} \left(\delta_2\right) l_{2z}}{\frac{1}{2} \rho v_r^2 S_r C_{Lr} \left(\delta_1\right) l_{1z} + \frac{1}{2} \rho_r v_r^2 S_r C_{Lr} \left(\delta_3\right) l_{3z}} \\ \frac{1}{2} \rho v_r^2 S_r C_{Lr} \left(\delta_1\right) l_{1x} - \frac{1}{2} \rho_r v_r^2 S_r C_{Lr} \left(\delta_3\right) l_{3x}} \end{bmatrix} (17)$$

where  $l_{1x}, l_{3x}, l_{1z}, l_{2z}, l_{3z}$  represent the  $\chi$ -components and z-components of the distances between the vehicle center of gravity and the vane aerodynamic center. The effect of the drag forces and moments has been neglected for simplification.

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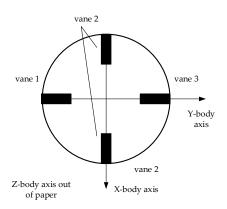


FIGURE 4. Vane configuration for ducted fan as viewed from above

#### E. GYROSCOPIC MOMENT

The spinning rotors of the ducted fan UAV will cause the gyroscopic precession torque effect. the expression for this moment vector is given as follows:

$$M_{gyro} = \begin{bmatrix} I_{zprop} q \left( \Omega_1 - \Omega_2 \right) \\ -I_{zprop} p \left( \Omega_1 - \Omega_2 \right) \\ 0 \end{bmatrix}$$
(18)

where  $I_{zprop}$  is the component of the rotors inertia about its spin axis.

The ducted coaxial-rotor UAV dynamics and kinematics equations are given as

$$\begin{split} \dot{u} &= vr - qw + \frac{1}{m}F_{x} \\ \dot{w} &= pw - ur + \frac{1}{m}F_{z} \\ \dot{w} &= uq - pv + \frac{1}{m}F_{z} \\ \dot{p} &= -\frac{I_{zx}}{I_{xx}}\left(\dot{r} + pq\right) + \frac{I_{xy}}{I_{xx}}\left(pr - \dot{q}\right) + \frac{(I_{yy} - I_{zz})}{I_{xx}}qr + \frac{I_{yz}}{I_{xx}}\left(r^{2} - q^{2}\right) + \frac{1}{I_{xx}}M_{x} \\ \dot{q} &= -\frac{I_{xx}}{I_{yy}}pr - \frac{I_{xy}}{I_{yy}}\left(\dot{p} + qr\right) + \frac{I_{yz}}{I_{yy}}\left(pq - \dot{r}\right) + \frac{I_{xz}}{I_{yy}}\left(p^{2} - qr\right) + \frac{I_{zz}}{I_{yy}}pq + \frac{1}{I_{yy}}M_{y} \\ \dot{r} &= \frac{(I_{yy} - I_{xx})}{I_{zz}}pq + \frac{I_{xy}}{I_{zz}}\left(q^{2} - p^{2}\right) - \frac{I_{yz}}{I_{zz}}\left(\dot{q} + pr\right) + \frac{I_{xz}}{I_{zz}}\left(qr - \dot{p}\right) + \frac{1}{I_{zz}}M_{z} \\ \dot{\phi} &= p + \tan\theta\left(q\sin\theta + r\cos\phi\right) \\ \dot{\theta} &= q\cos\phi - r\sin\phi \\ \dot{\psi} &= \left(q\sin\phi + r\cos\phi\right)\sec\theta \end{split}$$

(19)

In hovering condition, we use small perturbation theory and the Taylor expansion to linearize the nonlinear model at the equilibrium point:  $\dot{u} = \dot{v} = \dot{w} = 0$ ,  $\dot{p} = \dot{q} = \dot{r} = 0$ . The nonlinear system can be linearized:

$$\dot{x}(t) = A(t)x(t) + B(t)u(t)$$

$$y(t) = C(t)x(t) + D(t)u(t)$$
(20)

where the state vector  $x = [p, q, r, \varphi, \theta, \psi]^T$ , control input  $u = [\delta_1, \delta_2, \delta_3]^T$  and output vector  $y = [\varphi, \theta, \psi]^T$ .

The nominal system matrixes A and B have been obtained by theoretical calculation, system identification and some flight tests in hovering condition. The process will not be detailed in this paper, the results are as follows:

	Γ	0.546	0	0	0	~	1	0 1154	25 5267	0.1154 ]	
A=	0	0.546	0	0	0	0	, B=	-0.1154	35.5267	0.1154	
	-0.548	0	0	0	0	0		-17.8150	0	-17.8150	
	0	0	0	0	0	0		-36.8704	0	36.8704	
	1	0	0	0	0	0		0	0	0	
	0	1	0	0	0	0		0	0	0	
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#### III. PROBLEM FORMULATION AND PRELIMINARIES

#### A. PROBLEM FORMULATION

Considering the disturbances, model uncertainties and sensor fault, we introduce d(t),  $\Delta A$  and  $f_s(t)$  in the ducted coaxial-rotor UAV model (20) setup in section II, which is described as

$$\dot{x}(t) = (A + \Delta A)x(t) + Bu(t) + B_d d(t)$$

$$y(t) = C_1 x(t) + f_s(t) \qquad (21)$$

$$z(t) = C_2 x(t)$$

where  $x(t) \in \mathbb{R}^n$  is the system state vector,  $u(t) \in \mathbb{R}^r$  is the control input,  $d(t) \in \mathbb{R}^q$  is the unknown input vector and disturbance signal,  $f_s(t) \in \mathbb{R}^f$  is the sensor fault signal,  $y(t) \in \mathbb{R}^y$  and  $z(t) \in \mathbb{R}^z$  are the measurement output and performance output.  $A, B, B_d, C_1, C_2$  and  $D_2$  are kown matrices with appropriate dimensions,  $\Delta A$  represents time-varying parameter uncertainties of system, defined in the following form:[44]

$$\Delta A = HF(t)G \tag{22}$$

$$F(t)^{T} F(t) \le I \tag{23}$$

where H and G are given matrices of appropriate dimensions, which can describe the structured uncertainties of the system precisely.

The observer-based controller is designed to detect faults and meet some desired control objectives. We use the state-feedback controller

$$u(t) = -K\hat{x}(t) \tag{24}$$

where  $\kappa$  is the controller gain to be designed. Then, we have the observer-based controller

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$$\dot{\hat{x}}(t) = (A + \Delta A) \hat{x}(t) + Bu(t) + L(y(t) - \hat{y}(t))$$

$$\hat{y}(t) = C_1 \hat{x}(t)$$

$$r(t) = y(t) - \hat{y}(t)$$

$$u(t) = -K\hat{x}(t)$$
(25)

where L is the observer gain to be designed,  $\hat{x}(t)$  is the estimate of x(t), r(t) is the generated residual.

Denoting  $e(t) = x(t) - \hat{x}(t)$ ,  $\hat{f}(t) = r(t) - f_s(t)$   $\tilde{x} = [x^T, e^T]^T$ , where e(t) is the state estimation error,  $\hat{f}(t)$  is the sensor fault estimation error. Hence, we can write the augmented error system as

$$\begin{aligned} \dot{\tilde{x}}(t) &= \bar{A}\tilde{x}(t) + \bar{B}_{d}d(t) + \bar{B}_{fs}f(t) \\ \hat{f}(t) &= \bar{C}_{1}\tilde{x}(t) \\ z(t) &= \bar{C}_{2}\tilde{x}(t) \end{aligned}$$
(26)

Thus, the closed-loop state matrices are obtained as

$$\bar{A} = \begin{bmatrix} A + \Delta A - BK & BK \\ 0 & A + \Delta A - LC_1 \end{bmatrix}$$
$$\bar{B}_d = \begin{bmatrix} B_d \\ B_d \end{bmatrix}, \quad \bar{B}_{fs} = \begin{bmatrix} 0 \\ -L \end{bmatrix}$$
(27)
$$\bar{C}_1 = \begin{bmatrix} 0 & C_1 \end{bmatrix}, \quad \bar{C}_2 = \begin{bmatrix} C_2 & 0 \end{bmatrix}$$

The scheme of observer-based simultaneous flight control and sensor fault detection is shown in Fig. 5.

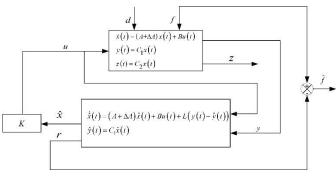


FIGURE 5. The scheme of simultaneous sensor fault detection and control

Then, the simultaneous sensor fault detection and attitude control problem in hover condition to be addressed in this paper can be expressed as follows.

Consider the new augmented system described by (26), we propose our design objectives as follows:

1) For control objective, we use the  $H_{\infty}$  norm constraint to guarantee robust stability of the closed-loop system. The constraint  $||G_{zd}(j\omega)||_{\infty} < \gamma$  can minimise the effects of the disturbances on the performance output z(t) in the presence of model uncertainties.

2) For detection objective, we ues the  $H_{-}$  to measure the fault sensitivity. The constraint is  $\|G_{\hat{f}f_s}(j\omega)\| > \beta$  useful to

increase the sensitivity of faults to the sensor fault estimation error.

3) For the stability of the closed-loop system, we use regional pole constraints to place the ploes in the left-half plane, which can be defined as:

$$\left\{s \in \mathbb{C} : s + \overline{s} < 0\right\}$$

where

$$G_{zd}(j\omega) = \overline{C}_2(j\omega I - \overline{A})^{-1} \overline{B}_d$$
$$G_{\hat{f}_s}(j\omega) = \overline{C}_1(j\omega I - \overline{A})^{-1} \overline{B}_{f_s}$$

# **B. PRELIMINARIES**

The following lemmas are essential for the later developments

Lemma 1 [50]: (Finsler's Lemma): Let  $\xi \in \mathbb{C}^n$ ,  $L \in \mathbb{C}^{n \times n}$  and  $H \in \mathbb{C}^{n \times m}$ . Let  $H^{\perp}$  be any matrix such that  $H^{\perp}H = 0$ . The following statements are equivalent:

(i)  $\xi^* L \xi < 0, \forall H^* \xi = 0, \xi \neq 0,$ 

(ii) 
$$H^{\perp}LH^{\perp'} < 0$$

(iii) 
$$\exists \chi \in \Re^{m \times n} : L + H\chi + \chi^* H^* < 0,$$

(iv)  $\exists \mu \in \Re : L - \mu H H^{\perp} < 0.$ 

Lemma 2: Let  $\Gamma$ , W, and  $\Lambda$  be given matrices, there exists a matrix F satisfying

$$\Gamma FW + \left(\Gamma FW\right)^T + \Lambda < 0$$

If and only if the following two conditions hold

$$\Gamma^{\perp} \Lambda \Gamma^{\perp T} < 0$$
$$W^{T^{\perp}} \Lambda W^{T^{\perp}} < 0$$

Lemma 3 [30]: (Generalised KYP lemma): Considering system  $G(j\omega) = C(j\omega I - A)^{-1}B + D$ , let a sysmetric matrix  $\Pi$  with appropriate dimensions be given, the following statements are equivalent:

(i) The finite frequency inequality

$$\begin{bmatrix} G(j\omega) \\ I \end{bmatrix}^* \prod \begin{bmatrix} G(j\omega) \\ I \end{bmatrix} < 0, \forall \omega \in [-\omega_l, \omega_l]$$

0

(ii) There exists Hermitian matrices P and Q > 0 satisfying

$$\begin{bmatrix} A & I \\ C & 0 \end{bmatrix}^T \Xi \begin{bmatrix} A & I \\ C & 0 \end{bmatrix} + \begin{bmatrix} B & 0 \\ D & I \end{bmatrix}^T \Pi \begin{bmatrix} B & 0 \\ D & I \end{bmatrix} < 0$$

where

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$$\Xi = \begin{bmatrix} -Q & P \\ P & \sigma_l^2 Q \end{bmatrix}$$

Lemma 4 [38]: ( $H_{\infty}$  performance ): Let  $||T(s)||_{\infty}$  denote the

 $H_{\infty}$  norm to T(s), where  $T(s) = C(sI - A)^{-1}B + D$ 

is the continumous-time system. Then, the following three conditions are equivalent.

- (i) Matrix A is stable and the  $H_{\infty}$  performance is bounded by  $\gamma > 0$ . Namely,  $\|T(s)\|_{\infty} < \gamma$ .
- (ii) There exists a symmetric positive-definite matrix P to satisfy

$$\begin{bmatrix} AP + PA^T & PC^T & B\\ CP & -\gamma I & D\\ B^T & D^T & -\gamma I \end{bmatrix} < 0$$

(iii) There exists a symmetric positive-definite matrix P and a general matrix F satisfying

$$\begin{bmatrix} AF + F^{T}A^{T} & P - F^{T} + r_{\infty}AF & F^{T}C^{T} & B\\ P - F + r_{\infty}A^{T}F^{T} & -r_{\infty}\left(F + F^{T}\right) & r_{\infty}F^{T}C^{T} & 0\\ CF & r_{\infty}CF & -\gamma I & D\\ B^{T} & 0 & D^{T} & -\gamma I \end{bmatrix} < 0$$

For a sufficiently small scalar  $r_{\infty} > 0$ .

Lemma 5 [39]: Let X , Y and F be real matrices of appropriate dimension with  $F^T F \leq I$ , then, for any scalar  $\varepsilon > 0$ ,

$$X^{T}FY + Y^{T}F^{T}X^{T} \le \varepsilon^{-1}X^{T}X + \varepsilon Y^{T}Y$$
  
Lemma 6 [40]: Let  $S = \begin{bmatrix} S_{11} & S_{12} \\ S_{12}^{T} & S_{22} \end{bmatrix}$  be symmetric matrix

of  $S_{11}$ ,  $S_{12}$ ,  $S_{22}$  with appropriate dimensions satisfying  $S_{11} = S_{11}^{T}$ ,  $S_{12} = S_{12}^{T}$ . then the following propositions are equivalent:

(i) S < 0(ii)  $S_{11} < 0$ ,  $S_{22} - S_{12}^{T} S_{11}^{-1} S_{12} < 0$ (iii)  $S_{22} < 0$ ,  $S_{11} - S_{12} S_{22}^{-1} S_{12}^{T} < 0$ 

# IV. SIMULTANEOUS FAULT DETECTION AND CONTROL

A robust control and fault detection approach based on observer technique is proposed to solve the hovering attitude control problem for a ducted coaxial-rotor UAV in the presence of unknown disturbance, system uncertainties and sensor fault. The aim of the proposed methodology is to give a design technique that guarantees the robustness to disturbances and uncertainties and sensitivity of faults of the UAV. In addition, the stability problem of the UAV can be satisfied by the Lyapunov theorem.

In this section, the LMI formulation for solving the simultaneous fault detection and control problem would be given. The main results are summarized in Theorems 1-7, such that a desired integrated detector/controller could be constructed.

## A. CONDITIONS FOR CONTROL PERFORMANCE

Recall lemma 4, we can get the following inequality which can guarantee the prescribed  $H_{\infty}$  performance level  $\gamma > 0$ of the closed-loop system (26)

$$\begin{bmatrix} \bar{A}F + F^{T}\bar{A}^{T} & P - F^{T} + r_{\infty}\bar{A}F & F^{T}\bar{C}_{2}^{T} & \bar{B}_{d} \\ P - F + r_{\infty}\bar{A}^{T}F^{T} & -r_{\infty}\left(F + F^{T}\right) & r_{\infty}F^{T}\bar{C}_{2}^{T} & 0 \\ \bar{C}_{2}F & r_{\infty}\bar{C}_{2}F & -\gamma I & D \\ \bar{B}_{d}^{T} & 0 & D^{T} & -\gamma I \end{bmatrix} < 0$$

$$(28)$$

Notice that, the augmented matrix  $\overline{A}$  is complicated and contains the system time-vary uncertainties, controller gain and observer gain to be designed, in order to linearize the design conditions and make the inequality solvable, we need to introduce the following change of variables.[42]. Clearly, this critical and special structure of the variables is stringent and brings conservatism into the proposed method design. We introduce the following change of variables *F* and  $F^{-1}$  as

$$F = \begin{bmatrix} X & (I - XY^{T})V^{-T} \\ U & -UY^{T}V^{-T} \end{bmatrix}$$

$$F^{-1} = \begin{bmatrix} Y^{T} & (I - Y^{T}X)U^{-1} \\ V^{T} & -V^{T}XU^{-1} \end{bmatrix}$$
(29)

where matrices X , Y are symmetric and U , V and X are invertible.

In addition, a transformation matrix has been introduced

$$T = \begin{bmatrix} I & 0\\ Y & V \end{bmatrix}$$
(30)

Define

$$\hat{A} = T\bar{A}FT^{T}$$

$$= \begin{bmatrix} (A + \Delta A)X - NX + NU & A + \Delta A - N \\ M & YA - YN \end{bmatrix}$$
(31)
$$\hat{B}_{d} = T\bar{B}_{d} = \begin{bmatrix} B_{d} \\ YB_{d} + VB_{d} \end{bmatrix}$$

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$$\hat{B}_{f_{S}} = T\bar{B}_{f_{S}} = \begin{bmatrix} 0 \\ -VL \end{bmatrix}$$

$$\hat{C}_{1} = \bar{C}_{1}FT^{T} = \begin{bmatrix} C_{1}U & 0 \end{bmatrix}$$

$$\hat{C}_{2} = \bar{C}_{2}FT^{T} = \begin{bmatrix} C_{2}X & C_{2} \end{bmatrix}$$

$$\hat{F} = TFT^{T} = \begin{bmatrix} X & I \\ Z & Y \end{bmatrix}$$
(31)

where Z = XY + VU.

Then the control objective 1) is transformed to an inequality condition in the following theorem:

Theorem 1: Consider the augmented system (26), given positive scalar  $\gamma$ , the  $H_{\infty}$  performance  $\|G_{zd}(j\omega)\|_{\infty} < \gamma$  holds if, for some positive scalar  $r_{\infty}$ , there exists a solution  $(X, Y, M, N, Z, \hat{P})$  to the following LMI

$$\begin{bmatrix} \hat{A} + \hat{A}^{T} & \hat{P} - \hat{F}^{T} + r_{\infty}\hat{A} & \hat{C}_{2}^{T} & \hat{B}_{d} \\ * & -r_{\infty}\left(\hat{F} + \hat{F}^{T}\right) & r_{\infty}\hat{C}_{2}^{T} & 0 \\ * & * & -\gamma I & 0 \\ * & * & * & -\gamma I \end{bmatrix} < 0 (32)$$

where  $\hat{P}$  is a positive-definite matrix, and,

$$\begin{bmatrix} \hat{A} & \hat{B}_d \\ \hat{C}_2 & 0 \end{bmatrix} = \begin{bmatrix} (A + \Delta A)X + BG & A + \Delta A - BH & B_d \\ M + Y \Delta AX + V \Delta AU & Y (A + \Delta A) - N & YB_d + VB_d \\ C_2 X & C_2 & 0 \end{bmatrix}^{(33)}$$

where the change of observer and controller variables are defined as follows

$$\begin{bmatrix} M & N \\ G & H \end{bmatrix}$$
$$= \begin{bmatrix} YAX + VAU & 0 \\ 0 & 0 \end{bmatrix} +$$
$$\begin{bmatrix} YB & -V \\ I & 0 \end{bmatrix} \begin{bmatrix} K & 0 \\ 0 & L \end{bmatrix} \begin{bmatrix} U - X & I \\ C_1U & 0 \end{bmatrix}$$
(34)

Proof:

By premultiplying and postmultiplying diag{T, T, I, I} and diag{ $T^T, T^T, I, I$ } on inequality (28), we can get the Theorem 1. It is worth noting that the nonlinear terms in the simultaneous fault detection and control augmented system of our UAV makes it impossible to directly apply Lemma 4. The problem is solved by the changes of variables, then the  $H_{\infty}$  performance of the designed system can be guaranteed. However, there are uncertainty terms  $\Delta A$  in inequality (32). In practical engineering, the uncertain parameters are unknown, so we need a condition for the existence of the

controller and the observer which are independent of the uncertain parameters. That is the following theorem:

Theorem 2: For the augmented system (26) with uncertainties and performance  $\|G_{zd}(j\omega)\|_{\infty} < \gamma$ , given positive scalar  $\gamma$ , positive real number  $\varepsilon_1$  and some positive scalar  $r_{\infty}$ , if there exists a solution  $(X, Y, M, N, Z, \hat{P})$ , and  $\hat{P}$  is a positive-definite matrix, the following LMI

$$\begin{bmatrix} \hat{A}_{1} + \hat{A}_{1}^{T} & \hat{P} - \hat{F} + r_{\infty} \hat{A}_{1} & \hat{C}_{2}^{T} & \hat{B}_{d} & G_{1}^{T} & \varepsilon_{1} H_{1}^{T} \\ * & -r_{\infty} \left( \hat{F} + \hat{F}^{T} \right) & r_{\infty} \hat{C}_{2}^{T} & 0 & 0 & 0 \\ * & * & -\gamma I & 0 & 0 \\ * & * & * & -\gamma I & 0 & 0 \\ * & * & * & * & -\varepsilon_{1} I & 0 \\ * & * & * & * & * & -\varepsilon_{1} I \end{bmatrix} < 0$$

$$\begin{bmatrix} 0 \\ - \\ - \\ (35) \end{bmatrix}$$

holds, then the designed controller gain K and the observer gain L can guarantee the  $H_{\infty}$  robust performance of the system (26).

Proof:

The inequality (32) is equivalent to

$$\Omega_1 + \Delta \Omega_1 < 0$$

where

where



$$\Delta_{11} = (HFG) X + X^{T} (HFG)^{T}$$

$$\Delta_{12} = (HFG) + X^{T} (HFG)^{T} Y^{T} + U^{T} (HFG)^{T} V^{T}$$

$$\Delta_{22} = Y (HFG) + (HFG)^{T} Y^{T}$$

$$\Delta_{13} = r_{\infty} (HFG) X$$

$$\Delta_{14} = r_{\infty} (HFG)$$

$$\Delta_{23} = r_{\infty} Y (HFG) X + r_{\infty} V (HFG) U$$

$$\Delta_{24} = r_{\infty} Y (HFG)$$

$$\Delta \Omega_1$$

By lemma 5, for any scalar  $\mathcal{E}_1 > 0$ , we can get

$$\Omega_{l} + \varepsilon_{l} H_{l} H_{l}^{T} + \varepsilon_{l}^{-1} G_{l} G_{l}^{T} < 0$$
(36)

where

Then, by lemma 6, the inequality (36) is equivalent to

$$\begin{bmatrix} \Omega_1 & G_1^T & H_1 \\ G_1 & -\varepsilon_1 I & 0 \\ H_1^T & O & \varepsilon_1^{-1} I \end{bmatrix} < 0$$
(37)

By premultiplying and postmultiplying diag  $\{I, I, \varepsilon I\}$  on the inequality (37), we can get the Theorem 2, which completes the proof.

Hence, Theorem 1 can be solved in the existence of the timevarying and unknown uncertainties. Based on Theorem 1, we can get Theorem 2, the sufficient condition of existence for augmented error system (26) without model parameter uncertainty  $\Delta A$  is given.

**B.** CONDITIONS FOR FAULT DETECTION SENSITIVITY Consider system (26), the sensor faults considered in this paper are assumed to be in the low frequency domain, by lemma 3, the following statements are equivalent:

(i) 
$$\left\| G_{\hat{f}_{s}}(j\omega) \right\|_{2} > \beta$$
  
(ii)  $\begin{bmatrix} \bar{A} & I \\ \bar{C}_{1} & 0 \end{bmatrix} \Phi \begin{bmatrix} \bar{A} & I \\ \bar{C}_{1} & 0 \end{bmatrix}^{T} + \begin{bmatrix} \bar{B}_{f} & 0 \\ 0 & I \end{bmatrix} \Pi \begin{bmatrix} \bar{B}_{f} & 0 \\ 0 & I \end{bmatrix}^{T} < 0$  (38)

where 
$$\Phi = \begin{bmatrix} -Q & I_1 \\ P_1 & \sigma_l^2 Q \end{bmatrix}$$
,  $\Pi = \begin{bmatrix} -I & 0 \\ 0 & \beta^2 I \end{bmatrix}$ ,  $P_1$  is a

symmetric matrix and Q is a positive-definite matrix.

Since we focus on augmented error system with low frequency sensor fault, disturbances and model parameter uncertainty, we need to design an new approach to accurately characterise the low-frequency performance index and the existence of this method does not depend on the information of system uncertainties. Different from most existing techniques, better fault sensitivity can be achieved by accurately characterizing the finite frequency performance index.

The detection objective 2) is transformed to an inequality condition in the following theorem:

Theorem 3: Given augmented system (26), the low frequency domain sensor fault sensitivity condition  $\|G_{\hat{f}_s}(j\omega)\|_{-} > \beta$ , for some positive scalar  $\beta > 0$ , holds if

there exists a solution  $(X, Y, M, N, Z, \hat{P}_1)$  to the following LMI

$$\begin{bmatrix} -\hat{Q} & \hat{P}_{1} - \hat{F} & 0 & -\hat{F}\xi \\ * & \sigma_{l}^{2}\hat{Q} + He\left(\hat{A} + \xi\hat{B}_{fs}^{T}\right) & \hat{B}_{fs} - \xi I & \hat{A}\xi + \hat{C}_{1}^{T} \\ * & * & -2I & 0 \\ * & * & & \beta^{2}I + He\left(\hat{C}_{1}\xi\right) \end{bmatrix} < 0$$

(39) Where  $\hat{P}_1$ ,  $\hat{Q}$  are symmetric matrices and  $\hat{Q} > 0$ . Proof: Denoting

$$\Delta = \begin{bmatrix} \Phi & 0 \\ 0 & \begin{bmatrix} \bar{B}_f & 0 \\ 0 & I \end{bmatrix} \Pi \begin{bmatrix} \bar{B}_f & 0 \\ 0 & I \end{bmatrix}^T$$

then, the inequality (38) can be reformulated as

$$\begin{bmatrix} \bar{A}^{T} & \bar{C}_{1}^{T} \\ I & 0 \\ 0 & I \end{bmatrix}^{T} \left( \begin{bmatrix} I & 0 & 0 \\ 0 & I & 0 \\ 0 & I & 0 \\ 0 & 0 & I \end{bmatrix}^{T} \Delta \begin{bmatrix} I & 0 & 0 \\ 0 & I & 0 \\ 0 & I & 0 \\ 0 & 0 & I \end{bmatrix} \right) \begin{bmatrix} \bar{A}^{T} & \bar{C}_{1}^{T} \\ I & 0 \\ 0 & I \end{bmatrix} < 0$$
(40)

On the other hand,

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$$\begin{bmatrix} I \\ 0 \\ 0 \end{bmatrix}^{T} \left( \begin{bmatrix} I & 0 & 0 \\ 0 & I & 0 \\ 0 & 0 & I \end{bmatrix}^{T} \Delta \begin{bmatrix} I & 0 & 0 \\ 0 & I & 0 \\ 0 & 0 & I \end{bmatrix} \right) \begin{bmatrix} I \\ 0 \\ 0 \end{bmatrix} = -Q < 0$$
(41)

then by lemma 2, we have that (38) holds if and only if

$$\Theta + \begin{bmatrix} -I\\ \bar{A}\\ \bar{C}_1 \end{bmatrix} F_1 \begin{bmatrix} 0 & I & 0\\ 0 & 0 & I \end{bmatrix} + \begin{bmatrix} 0 & I & 0\\ 0 & 0 & I \end{bmatrix}^T F_1^T \begin{bmatrix} -I\\ \bar{A}\\ \bar{C}_1 \end{bmatrix}^I < 0 (42)$$

where

W

$$\Theta = \begin{bmatrix} I & 0 & 0 \\ 0 & I & 0 \\ 0 & I & 0 \\ 0 & 0 & I \end{bmatrix}^{I} \Delta \begin{bmatrix} I & 0 & 0 \\ 0 & I & 0 \\ 0 & 0 & I \end{bmatrix} = \begin{bmatrix} -Q & P_{1} & 0 \\ P_{1} & \sigma_{l}^{2}Q - \bar{B}_{f}\bar{B}_{f}^{T} & 0 \\ 0 & 0 & \beta^{2}I \end{bmatrix}$$

In order to make the inequality being feasible, we need to partition  $F_1$  as  $F_1 = [F_{11} \ F_{12}]$ , where  $F_{11} = F, F_{12} = F\xi$ , where  $\xi$  are given matrix, which guarantees that  $F_{12}$  has appropriate dimensions.

By premultiplying diag  $\{T, T, I\}$  and postmultiplying diag $\{T^T, T^T, I\}$ , we have

$$\begin{bmatrix} -\hat{Q} & \hat{P}_1 & 0 \\ * & \sigma_l^2 \hat{Q} - \hat{B}_{f_s} \hat{B}_{f_s}^T & 0 \\ * & * & \beta^2 I \end{bmatrix} + He \left( \begin{bmatrix} -\hat{F} \\ \hat{A} \\ \hat{C}_1 \end{bmatrix} \begin{bmatrix} 0 & I & \xi \end{bmatrix} \right) < 0$$
(A3)

where 
$$\hat{Q} = TQT^{T}$$
 and  $\hat{P}_{1} = TP_{1}T^{T}$ , define  

$$\Psi = \begin{bmatrix} I & 0 & 0 \\ 0 & I & 0 \\ 0 & \hat{B}_{fs}^{T} & 0 \\ 0 & 0 & I \end{bmatrix}$$

$$\Delta = \begin{bmatrix} -\hat{Q} & \hat{P}_{1} - \hat{F} & 0 & -\hat{F}\xi \\ * & \sigma_{l}^{2}\hat{Q} + He(\hat{A}) & -I & \hat{A}\xi + \hat{C}_{1}^{T} \\ * & * & 0 & 0 \\ * & * & * & \beta^{2}I + He(\hat{C}_{1}\xi) \end{bmatrix}$$
(44)

Then, (43) is rewritten as

$$\Psi^T \Delta \Psi < 0 \tag{45}$$

Recall lemma 1, we have that (45) holds if and only if there exists matrix  $\Lambda$  that

$$\Delta + \Lambda \Phi + \Phi^T \Lambda^T < 0$$

where

$$\Phi^{T^{\perp}} = \begin{bmatrix} 0 \\ \hat{B}_{fs} \\ -I \\ 0 \end{bmatrix}^{\perp} = \begin{bmatrix} I & 0 & 0 \\ 0 & I & 0 \\ 0 & \hat{B}_{fs}^{T} & 0 \\ 0 & 0 & I \end{bmatrix}, \Lambda^{T} = \begin{bmatrix} 0 \\ \xi \\ I \\ 0 \end{bmatrix}$$

finally, after calculation, we get the theorem 3, which completes the proof.

Notice that there are also uncertainty terms  $\Delta A$  in inequality (39), by following the similar proof procedure of theorem 2, we can obtain the sufficient codition of existence for augmented error system (26) without model parameter uncertainty  $\Delta A$  is given. The proof is omitted for the sake of brevity.

The LMI constraints for the low-frequency sensor fault detection sensitivity is given in the following theorem:

Theorem 4: For the augmented system (26) with uncertainties and performance  $||G_{\hat{f}f_s}(j\omega)||_{-} > \beta$ , given positive scalar  $\beta$  and positive real number  $\varepsilon_2$ , if there exists a solution  $(X, Y, M, N, Z, \hat{P}_1)$ , where  $\hat{P}_1$ ,  $\hat{Q}$ , are symmetric matrices and  $\hat{Q} > 0$ , the following LMI

$$\begin{bmatrix} -\hat{Q} & \hat{P}_{1} - \hat{F} & 0 & -\hat{F}\xi & G_{2}^{T} & \varepsilon_{2}H_{2} \\ * & \sigma_{l}^{2}\hat{Q} + He(\hat{A}_{1} + \xi\hat{B}_{js}^{T}) & \hat{B}_{js} - \xi I & \hat{A}_{1}\xi + \hat{C}_{1}^{T} & 0 & 0 \\ * & * & -2I & 0 & 0 & 0 \\ * & * & & \beta^{2}I + He(\hat{C}_{1}\xi) & 0 & 0 \\ * & * & * & * & -\varepsilon_{2}I & 0 \\ & & * & * & * & -\varepsilon_{2}I \end{bmatrix} < 0$$

$$(46)$$

holds, where

then the designed controller gain K and the observer gain L can guarantee the low-frequency fault detection sensitivity performance of the system (26).

# C. CONDITIONS FOR STABILITY

In order to achieve design objective 3), which is to guarantee the stability of the system and the dynamic performance of the closed-loop system, theorem 5 is proposed:

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Theorem 5: Given augmented system (26), conditions for the stability of the closed-loop system holds if there exists a solution  $(X, Y, M, N, Z, P_2)$  to the following LMI

$$\begin{bmatrix} -rHe(\hat{F}_2) & \hat{P}_2 - q\hat{F}_2 + r\hat{A}^T \\ \hat{P}_2 - q\hat{F}_2^T + r\hat{A} & He(\hat{A}) \end{bmatrix} < 0$$
(47)

with r, q are given positive scalars. Proof:

Consider the standard Lyapunov theorem, the matrix  $\overline{A}$  has all its eigenvalues in the open left-half plane if and only if there exists a positive symmetric  $P_2$  that the following inequality holds

$$\begin{bmatrix} \bar{A} & I \end{bmatrix} \begin{bmatrix} 0 & P_2 \\ P_2 & 0 \end{bmatrix} \begin{bmatrix} \bar{A} & I \end{bmatrix}^T = \bar{A}P_2 + P_2\bar{A} < 0$$
(48)

On the other hand,

$$\begin{bmatrix} qI & -rI \end{bmatrix} \begin{bmatrix} 0 & P_2 \\ P_2 & 0 \end{bmatrix} \begin{bmatrix} qI & -rI \end{bmatrix}^T = -rqP - qrP < 0 \quad (49)$$

Explicit null space bases calculations yield

$$\begin{bmatrix} \overline{A} & I \end{bmatrix} = \begin{bmatrix} -I \\ \overline{A} \end{bmatrix}^{\perp}, \begin{bmatrix} qI & -rI \end{bmatrix} = \begin{bmatrix} rI \\ qI \end{bmatrix}^{\perp}$$

Recall lemma 2, (48) and (49) hold that the following inequality holds if and only if there exists a matrix  $F_2$  satisfying

$$\begin{bmatrix} 0 & P_2 \\ P_2 & 0 \end{bmatrix} + \begin{bmatrix} -I \\ \bar{A} \end{bmatrix} F_2 \begin{bmatrix} rI & qI \end{bmatrix} + \left( \begin{bmatrix} -I \\ \bar{A} \end{bmatrix} F_2 \begin{bmatrix} rI & qI \end{bmatrix} \right)^T < 0$$
(50)

By premultiplying diag  $\{T, T\}$  and postmultiplying diag $\{T^T, T^T\}$ , we have the inequality (47), which complets the proof.

Obviously, the model parameter uncertainty term  $\Delta A$  stiil makes it is impossible to solve the stability condition by theorem 5. Following the similar procedure of Theorem 2 and Theorem 4, we can obtain the stability sufficient condition for the system (26) without model parameter uncertainty  $\Delta A$  is given.

Theorem 6: For the augmented system (26) with uncertainties and stability constraints of the closed-loop system, given positive scalar  $\varepsilon_3$ , if there exists a solution  $(X, Y, M, N, Z, \hat{P}_2)$ , where r, q are given positive scalars, and  $\hat{P}_2$  is symmetric positive matrix, the following LMI

$$-rHe(\hat{F}_{2}) \quad \hat{P}_{2} - q\hat{F}_{2} + r\hat{A}_{1}^{T} \quad G_{3}^{T} \quad \varepsilon_{3}H_{3} \\ * \quad He(\hat{A}_{1}) \quad 0 \quad 0 \\ * \quad * \quad -\varepsilon_{3}I \quad 0 \\ * \quad * \quad * \quad -\varepsilon_{3}I \end{bmatrix} < 0 \quad (51)$$

holds, where 
$$H_3 = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ H & 0 & 0 & 0 \\ YH & VH & 0 & 0 \end{bmatrix}$$
  
$$G_3 = \begin{bmatrix} rGX & rG & GX & G \\ rGU & 0 & GU & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

then the designed controller gain K and the observer gain L can guarantee the stability performance of the system (26).

## D. ALGORITHM

According Theorems 1-6, simultaneous robust control and sensor fault detection problem considering system parameter uncertainty can be solved by the following theorem

Theorem 7: Cosider system (26), for given positive scalars  $r_{\infty}, r, q, \gamma, \beta, \varepsilon_1, \varepsilon_2, \varepsilon_3$ , there exist a observer-based controller (25) such that the augmented system (26) satisfying  $H_{\infty}$  performance  $\|G_{zd}(j\omega)\|_{\infty} < \gamma$ , low frequency domain sensor fault sensitivity condition  $\|G_{\hat{f}f_s}(j\omega)\|_{-} > \beta$  and stability of the closed-loop system if the inequality conditions (35), (46), and (51) hold.

## **V. SIMULATIONS**

In this section, the proposed control and detection strategy has been tested by simulation in order to illustrate the effectiveness and the performance attained for the ducted coaxial-rotor UAV control and sensor fault detection problem. The ducted coaxial-rotor UAV model parameters used in the simulations are displayed in Table 1.

TABLE I

THE PARAMETERS OF THE DUCTED COAXIAL-ROTOR UAV FOR SIMULATIONS

Symbol	Value	Unit
g	9.8	m/s²
m	6.56	kg
L	0.208	m
L'	0.129	m
I <sub>xx</sub>	0.345	kg∙m²
$I_{yy}$	0.345	kg⋅m²
I <sub>zz</sub>	0.081	kg⋅m²
Izprop	0.006	kg⋅m²
$\rho_{\infty}$	1.22	kg/m <sup>3</sup>
Sr	0.0138	m <sup>2</sup>
vi	20	m/s
$C_{Lr}$	0.12	1
C <sub>Dr</sub>	0.12	1

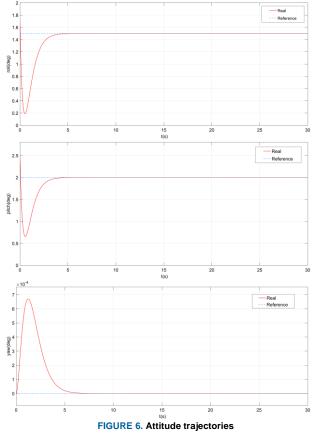
Next, given  $r_{\infty} = r = q = 1$ ,  $\gamma = 0.6$ ,  $\beta = 0.5$ ,  $\varepsilon_1 = \varepsilon_2 = \varepsilon_3 = 1$ , applying Theorem 7, we use the LMI toolbox and Simulation environment in the Matlab to illustrate the effectiveness of the proposed method, we get

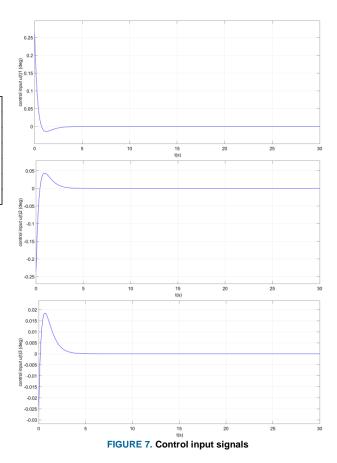


<i>K</i> =	-0.0154	0.1155	-0.0555	0	0.1126	-0.0544
	-0.1158	-0.0154	-0.0275	-0.1129	0	-0.0215
	-0.0153	-0.1154	0.0561	0.0007	0.1120	0.0554
1						
<i>L</i> =	-1.1720	-1.9563	0.0039	1.2190	0.2542	0.0369
	0.8093	-8.3594	-0.0560	-1.5583	0.7164	-0.0255
	-0.0074	0.0179	-0.1368	-0.0095	0.0327	-0.2888
	0.8986	0.5610	0.0397	-0.2324	2.8107	0.0842
	-2.2698	1.0911	-0.0808	-2.5524	-0.1394	-0.0959
	0.0568	0.0608	1.3111	-0.0904	0.0937	-0.0357

A. FLIGHT WITHOUT DISTURBANCES AND FAULTS

To illustrate the attitude tracking control performance without disturbances, uncertainties and faults, the system condition x(0) =intinal is set as  $\begin{matrix} 0 & 0 & 0 \end{matrix} \end{bmatrix}^T$  $\hat{x}(0) =$ [1.7 2.5  $(0 \ 0 \ 0)^T$ . The attitude tracking control 0 0 0 performance and control input responses are shown in Fig. 6 and Fig. 7, respectively. All the attitude variables can track the reference command within 5s and the yaw channel is less affected by the other two channels. The system can converge quickly due to the proposed method. Finally, Fig. 7 illustrates that the control input signals all acceptable and could be applied to real model.





# B. FLIGHT WITH DISTURBANCES, UNCERTAINTIES AND FAULTS

This part simulation is implemented to illustrate the control performance of the proposed method with taking into consideration the system parameter uncertainty, disturbance and constant deviation fault. The system initial condition is  $x(0) = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \end{bmatrix}^T$  and the observer initial condition is also  $\hat{x}(0) = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \end{bmatrix}^T$ . Assume that  $B_d = [0.71 \quad -0.53 \quad 0.80 \quad 1 \quad 1 \quad 1]^T$ uncertainty of  $\Delta A$  is assumed to be in the range [-40%, 40%], and the disturbance d(t) is assumed to be the random noise with power 0.0005. The low-frequency sensor fault  $f_s(t)$  is considered as the X-axis and Y-axis angular velocity sensor constant gain fault, which is assumed to be  $f_s(t) = 1$  for  $5s \le t \le 17s$ , and  $f_s(t) = 0$  elsewhere. It is expected that in the presence of system uncertainty, disturbance and fault, the closed-loop system is still stable and robust to disturbance. It can be seen from Fig. 8 that the poles of the closed-loop system can be all placed in the left-half plan with the system parameter uncertainty vary in the range [-40%, 40%], which means the proposed method can keep the system stable with the system uncertainty.

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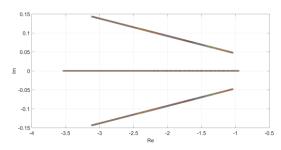
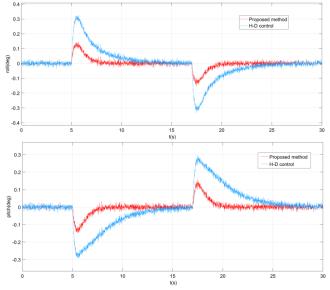


FIGURE 8. Closed loop poles with  $\Delta \in [-40\%, 40\%]$ 

The performance output z(t), which is designed to be hover attitude, is denoted in Fig.9. From Fig.9, it can be seen that the proposed observer-based controller stabilized the closedloop system in the presence of disturbances, system uncertainty and sensor fault, and the effects of disturbance and fault on the performance output have also been weakened. The roll angle response and pitch angle response under the proposed controller converge to small neighborhood of zero in 4s, while the roll and pitch angle response under H-D control converge to small neighborhood of zero in almost 10s. In addition, the vibration amplitude of the proposed controlller is 40% of the H-D control method. Moreover, the yaw angle response under the proposed method is not affected by disturbance, uncertainty and the fault, while it still has slight effect under the H-D control. When a sensor fault occurs, the designed controller succeeded in minimizing the effect of fault on the UAV input-output relationship and ensuring certain level of robustness of the system output to noises and disturbances.



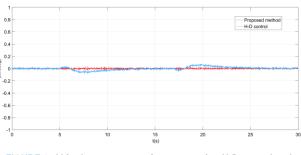


FIGURE 9. Altitude response performance using H-D control and proposed method

The comparison of the control inputs signals of the proposed method and the H-D control are presented in Fig. 10, which shows that the proposed method can achive faster convergence with smaller control effect. Also, it indicats that the control signals are continuos and physically realizable. The measurement noise in engineering is usually white noise, so we can get that the influence of disturbance and measurement noise on control performance and input signal is weakened. Compared with the H-D control method, the proposed method has better noise and disturbances suppression effect, better robustness and easier engineering implementation.

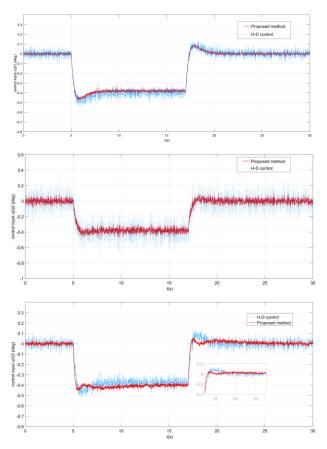


FIGURE 10. Control inputs of altitude response using H-D control and proposed method

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#### C. FAULT ESTIMATION FOR LOW-FREQUENCY FAULT

To illustrate the effectiveness of the observer-based controller for the fault detection objectives, the fault and disturbance signals shown in Fig.11. The residual responses due to the proposed method in this paper and the exsiting method provided in [32] have been shown in Fig. 12. From Fig. 12 we can conclude that that the proposed observerbased controller has good fault sensitivity properties and good disturbance attenuation. Compared with the techniques which do not restrict the fault to a given specific frequency range, the effects of the low-frequency fault in residual are less susceptible to the disturbances effectes. Although the residual responses under the two methods are both affected by the disturbance, the proposed method in this paper has a better performance on fault detection and the control performance is also taken into account. However, due to the accurate description of fault frequency, the proposed method has some limitations in full frequency fault detection.

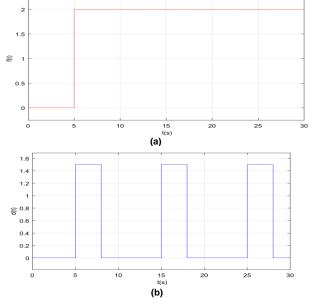


FIGURE 11. (a)Fault signal; (b) Disturbance signal

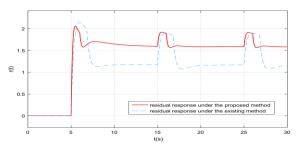


FIGURE 12. Residual response under the proposed method and residual response under the existing method

## **VI. CONCLUSIONS**

This paper presented a solution to the simultaneous control and sensor fault detection problem for the ducted coaxial-rotor UAV in the presence of unknown disturbance and system uncertainties. A complete dynamic model has been established by analyzing the various forces and moments acting on the vehicle respectively. The control architecture was composed of an observer and a controller, which can achieve the fault detection objectives and control objectives simultaneously by one single unit in a design process. The major advantages of this article are as follows: 1) This design idea takes both control and fault detection objectives into account, and reduces the complexity of design. 2) The new approach can accurately characterize the finite frequency performance index by introducing the GKYP lemma to deal with the finitefrequency sensor fault detection problem. Through introducing a new form linearizing change-of-variables, the observer-based controller design conditions converted into LMI-based optimization problem. 3) Different from the most existing techniques, the proposed method is presented by a novel model, which contains time-varying system parameters uncertainty, then the LMI-based theorem can solve the fault tolerant problem with system uncertainty simultaneously. The simulation results have illustrated the proposed control design can guarantee the  $H_{\infty}$  performance to disturbance and system uncertainty,  $H_{-}$  performance which measured the fault sensitivity and stability of the closed-loop system.

The proposed method in this paper still has some limitations and can be improved in near future. Firstly, the method in this paper has some limitations in multi-fault detection and fullfrequency fault detection. Second, some control performance may be lost while the detection performance is taken into account. Our future work will focus on fault tolerant control problem with multi-sensor faults and multi-actuator faults. In addition, simulation on nonlinear model and real flight tests should be performed.

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