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# Efficient energy back transfer from Ce $^{3+}$ 5d state to Pr $^{3+}$ $^1$ D $_2$ level in Lu $_3$ Al $_5$ O $_{12}$ upon Pr $^{3+}$ 4f5d excitation $^{\,\,\!\!\!\!/}$



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#### ABSTRACT

The step energy transfers from  $Pr^{3+}$  4f5d state to  $Ce^{3+}$  5d state followed by energy back transfer from  $Ce^{3+}$  5d state to  $Pr^{3+}$   $^{1}D_{2}$  level are studied. The  $Ce^{3+}$   $^{2}Pr^{3+}$  energy back transfer upon  $Pr^{3+}$  4f5d excitation is found to be more efficient than the normal  $Ce^{3+}$   $^{2}Pr^{3+}$  energy transfer upon  $Ce^{3+}$  5d excitation. The efficient energy back transfer is attributed to preferential excitation of the  $Ce^{3+}$  ion with an adjacent  $Pr^{3+}$  surrounding in  $Pr^{3+}$   $^{2}Ce^{3+}$  energy transfer of the first step, whereas  $Ce^{3+}$  is excited randomly in the normal energy transfer. The efficiencies of  $Ce^{3+}$   $^{2}Pr^{3+}$  energy back transfer as a function of  $Ce^{3+}$  and  $Pr^{3+}$  concentration are evaluated, respectively.

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## 1. Introduction

Energy transfer followed by energy back transfer between luminescent centers considerably affects luminescent properties of luminescent materials and it has been observed in various rare earth ion pairs [1–3]. Ce<sup>3+</sup> doped rare earth aluminium garnets e.g. Yttrium aluminium garnet (YAG) and Lutetium aluminium garnet (LuAG) exhibit highly efficient luminescence. These materials can serve as excellent phosphors for use in white light emitting diodes (w-LEDs) and high energy radiation detection [4–7]. Introducing Pr<sup>3+</sup> into Ce<sup>3+</sup> doped garnets can modify their luminescent properties through energy transfer between Ce<sup>3+</sup> and Pr<sup>3+</sup> [8,9]. In our previous work [10,11], we have studied  $Ce^{3+} \rightarrow Pr^{3+}$  energy transfer upon  $Ce^{3+}$  5d excitation at around 450 nm in YAG. The energy transfer results in the appearance of pronounced red emission line of  $Pr^{3+} {}^{1}D_{2} \rightarrow {}^{3}H_{4}$  transition added into the yellow emission band of  $Ce^{3+}$   $5d \rightarrow 4f$  transition, being helpful for the improvement of color rendering in YAG:Ce<sup>3+</sup> converted w-LEDs. Yang and Kim have studied luminescent properties of YAG:Ce<sup>3+</sup>, Pr<sup>3+</sup> nanocrystalline phosphors [12]. They selected 287 nm wavelength to excite  $Pr^{3+}$  4f5d state and observed both the red emission line of Pr<sup>3+</sup> and the yellow emission band of  $Ce^{3+}$ . This result was attributed to two step energy transfers, i.e., from  $Pr^{3+}$  4f5d to  $Ce^{3+}$  5d, and from  $Ce^{3+}$  5d back to  $Pr^{3+}$   $^{1}D_{2}$ . The emission spectra also demonstrated that the intensity ratio of the red emission line to the yellow emission band upon  $Pr^{3+}$  excitation is larger than that upon  $Ce^{3+}$  5d excitation. This phenomena is not yet explained.

LuAG is a good host for scintillation due to its higher density, effective atomic number ( $Z_{eff} = 62.9$ ) and higher light yield compared with YAG [13-15]. Ogieglo et al. have codoped Pr<sup>3+</sup> into LuAG:Ce<sup>3+</sup> scintillator in attempt to increase the light yield as Pr<sup>3+</sup> 4f5d state can efficiently capture the electron-hole pairs generated by radiation and subsequently transfer energy to  $Ce^{3+}$  5d state. They also found that Ce<sup>3+</sup> excited by energy transfer from Pr<sup>3+</sup> can transfer energy back to Pr<sup>3+</sup> to populate Pr<sup>3+</sup> <sup>1</sup>D<sub>2</sub> level [9]. However, the efficiency of the  $Ce^{3+} \rightarrow Pr^{3+}$  energy back transfer has rarely been studied. In principle, the  $Ce^{3+} \rightarrow Pr^{3+}$  energy back transfer upon Pr<sup>3+</sup> 4f5d excitation should be more efficient than the  $Ce^{3+} \rightarrow Pr^{3+}$  energy transfer upon  $Ce^{3+}$  5d excitation. The reasons for that are as follows. Upon  $Pr^{3+}$  4f5d excitation,  $Ce^{3+}$  is excited by energy transfer from Pr<sup>3+</sup>, resulting in that the Ce<sup>3+</sup> ion that has an adjacent Pr<sup>3+</sup> surrounding is preferentially excited, i.e., preferential excitation of Ce<sup>3+</sup> in the closely spaced Ce<sup>3+</sup>-Pr<sup>3+</sup> pairs, whereas direct photo-excitation of Ce3+ 5d undergoes random excitation of  $Ce^{3+}$ . As a result, the  $Ce^{3+} \rightarrow Pr^{3+}$  energy back transfer should be

more efficient than the  $Ce^{3+} \rightarrow Pr^{3+}$  energy transfer. In this paper, we study  $Pr^{3+} \rightarrow Ce^{3+} \rightarrow Pr^{3+}$  step energy transfers in LuAG upon  $Pr^{3+} \rightarrow 4f5d$  excitation. The efficient  $Ce^{3+} \rightarrow Pr^{3+}$  energy

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 $<sup>^{\</sup>circ}$ This work highlights that the energy back transfer from  $Ce^{3+}$  5d state to  $Pr^{3+}$   $^{1}D_{2}$  level after the  $Ce^{3+}$  5d state is populated by energy transfer from  $Pr^{3+}$ .

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back transfer with respect to the  $Ce^{3+} \rightarrow Pr^{3+}$  energy transfer is observed. The efficiencies of these energy transfers as a function of  $Ce^{3+}$  and  $Pr^{3+}$  concentration are evaluated, respectively.

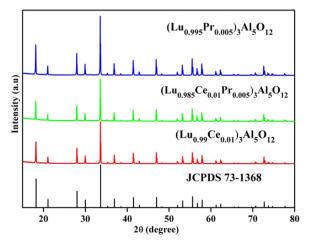
## 2. Experimental

The powder phosphor samples were synthesized by the high temperature solid-state reaction with mixtures of high-purity  $\text{Lu}_2\text{O}_3$ ,  $\text{CeO}_2$ ,  $\text{Al}_2\text{O}_3$ , and  $\text{Pr}_6\text{O}_{11}$  in molar of  $(\text{Lu}_{1-x-y}\text{Ce}_x\text{Pr}_y)_3\text{Al}_5\text{O}_{12}$  (x, y represent the concentration of  $\text{Ce}^{3+}$ ,  $\text{Pr}^{3+}$ , respectively), 3 wt% AlF3 was appended as the flux. After a good mixing in an agate mortar, the mixtures were sintered under CO reducing condition at 1550 °C for 5 h. The structure of the final products was characterized by powder X-ray diffraction (XRD). Room temperature photoluminescence (PL) and photoluminescence excitation (PLE) spectra were measured with a Hitachi Spectrometer (F-7000). The fluorescence decays of  $\text{Ce}^{3+}$  were measured by an FL920 fluorimeter (Edinburgh Instruments, Livingston, UK) with a hydrogen flash lamp (nF900; Edinburgh Instruments). All the measurements were conducted at room temperature.

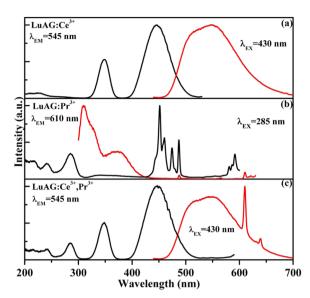
#### 3. Results and discussion

Fig. 1 shows the XRD patterns of  $(Lu_{(1-x-y)}Ce_xPr_y)_3Al_5O_{12}$  samples. It is obvious that all the diffraction peaks of the samples can be well indexed to the cubic phase (JCPDS no. 73–1368) and no detectable impurities are present, indicating that doping  $Ce^{3+}$  and  $Pr^{3+}$  does not generate any impurities or induce significant changes in the host structure.

The PLE and PL spectra for  $(Lu_{0.99}Ce_{0.01})_3Al_5O_{12}$  (a),  $(Lu_{0.995}Pr_{0.005})_3Al_5O_{12}$  (b),  $(Lu_{0.985}Ce_{0.01}Pr_{0.005})_3Al_5O_{12}$  (c) are shown in Fig. 2. The Ce<sup>3+</sup> singly doped sample exhibits a broad green emission band around 545 nm, which originates from the transition of the lowest-lying 5*d* state to the 4*f* ground state of Ce<sup>3+</sup>. Meanwhile, the PLE spectrum of the green emission consists of two strong bands located around 445 nm and 350 nm, which originates from the transitions of the 4*f* ground state to the lowest and upper 5*d* states of Ce<sup>3+</sup>, respectively [16]. The PL spectrum of Pr<sup>3+</sup> singly doped sample upon 285 nm excitation exhibits several emission bands (see Fig. 2(b)). In the UV region, the two strong emission bands peaked at 310 nm and 372 nm are assigned to the transitions from the lowest-lying 4*f*5*d* state to <sup>3</sup>H<sub>J</sub> (J=4, 5, 6) and <sup>3</sup>F<sub>J</sub> (J=2, 3, 4) levels, respectively. There are also two weak emission lines at 488 nm and 610 nm, which are assigned to <sup>3</sup>P<sub>O</sub>  $\rightarrow$  <sup>3</sup>H<sub>4</sub>



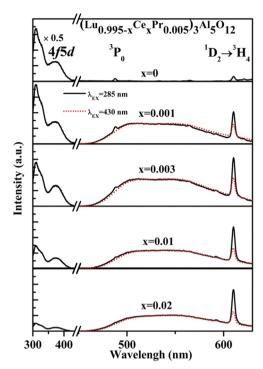
**Fig. 1.** The XRD patterns of  $(Lu_{0.99}Ce_{0.01})_3Al_5O_{12}$ ,  $(Lu_{0.985}Ce_{0.01}\ Pr_{0.005})_3Al_5O_{12}$  and  $(Lu_{0.995}Pr_{0.005})_3Al_5O_{12}$ .



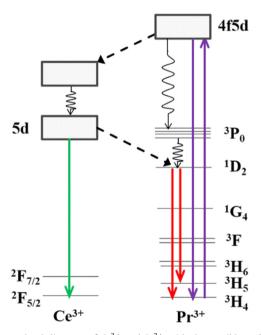
**Fig. 2.** PL and PLE spectra of  $(Lu_{0.99}Ce_{0.01})_3Al_5O_{12}$ ,  $(Lu_{0.995}Pr_{0.005})_3Al_5O_{12}$  and  $(Lu_{0.985}Ce_{0.01}Pr_{0.005})_3Al_5O_{12}$ .

and  $^1\mathrm{D}_2 \rightarrow ^3\mathrm{H}_4$  transitions, respectively. The PLE spectrum of the red emission line contains three groups of excitations in  $\mathrm{Pr}^{3+}$  singly doped sample. In the UV spectral region the bands located at 285 nm and 242 nm are due to the  $4f \rightarrow 5d$  transitions of  $\mathrm{Pr}^{3+}$ . The lines in the range of 430 nm-500 nm are attributed to  $^3\mathrm{H}_4 \rightarrow ^3\mathrm{P}_J$  (J=0,1,2),  $^1\mathrm{I}_6$  transitions. The excitation lines around 600 nm originates from  $^3\mathrm{H}_4 \rightarrow ^1\mathrm{D}_2$  transition. In  $\mathrm{Ce}^{3+}$  and  $\mathrm{Pr}^{3+}$  codoped sample, as shown in Fig. 2(c), the PLE spectrum for monitoring the  $\mathrm{Ce}^{3+}$  emission at 545 nm appears remarkable 4f5d bands of  $\mathrm{Pr}^{3+}$  peaking at 242 and 285 nm. This indicates the existence of energy transfer from  $\mathrm{Pr}^{3+}$  4f5d state to  $\mathrm{Ce}^{3+}$  5d state. When only  $\mathrm{Ce}^{3+}$  is excited at 430 nm, the PL spectrum contains not only the green band of  $\mathrm{Ce}^{3+}$  but also an intense red emission line of  $\mathrm{Pr}^{3+}$  at 610 nm, indicating the occurrence of energy transfer from  $\mathrm{Ce}^{3+}$  5d state to  $\mathrm{Pr}^{3+}$   $1\mathrm{D}_2$  level.

Fig. 3 shows the PL spectra of sample series A: (Lu<sub>0.995-x</sub>  $Ce_xPr_{0.005})_3Al_5O_{12}$ , with a fixed  $Pr^{3+}$  concentration at 0.005 and various Ce<sup>3+</sup> concentrations ranging from 0 to 0.02 upon Pr<sup>3+</sup> 4f5d excitation at 285 nm (solid) and/or upon  $Ce^{3+}$  5d excitation at 430 nm (dotted). Upon  $Pr^{3+}$  4f5d excitation in  $Pr^{3+}$  singly doped sample, the 4f5d emission bands in the UV spectral region dominate the PL spectrum with a weak  ${}^{3}P_{0} \rightarrow {}^{3}H_{4}$  blue emission line at 488 nm and a  ${}^{1}D_{2} \rightarrow {}^{3}H_{4}$  red emission line at 610 nm. With addition of  $Ce^{3+}$ , the UV emission bands and the blue emission line of Pr<sup>3+</sup> are weakened with the appearance of the strong green emission band of Ce<sup>3+</sup> and the strongly enhanced red emission line of Pr<sup>3+</sup>. In Pr<sup>3+</sup> singly doped sample, the blue emission line and the red emission line are very weak with respect to the UV emission bands, indicating that the rate of nonradiative relaxation from the 4f5d state down to the <sup>3</sup>P<sub>0</sub> and <sup>1</sup>D<sub>2</sub> levels is much smaller than the radiative rate of the 4f5d emission [17]. If the nonradiative relaxation rate is independent of Ce<sup>3+</sup> addition, the intensity ratio of the blue and/or the red emission line to the UV emission should keep unchanged in the presence of Ce<sup>3+</sup>. This is evidenced by the intensity reduction of both the UV and the blue emission in the presence of Ce<sup>3+</sup>. The strong enhancement of the red emission line with respect to both the UV and the blue emission in the presence of Ce<sup>3+</sup> is attributed to the step energy transfers, that is, energy transfer from  $Pr^{3+}$  4f5d state to  $Ce^{3+}$  5d state and energy back transfer from Ce<sup>3+</sup> 5d state to Pr<sup>3+</sup> <sup>1</sup>D<sub>2</sub> level. The two step energy transfers open an additional route for populating the Pr<sup>3+ 1</sup>D<sub>2</sub> level from Pr<sup>3+</sup> 4f5d state with the use of Ce<sup>3+</sup> 5d as an intermediate state, as sketched in Fig. 4.

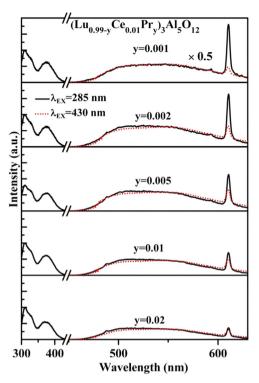


**Fig. 3.** PL spectra of sample series A:  $(Lu_{0.995-x}Ce_xPr_{0.005})_3Al_5O_{12}$ , (x=0-0.02) upon  $Pr^{3+}$  4f5d excitation at 285 nm (solid), and/or upon  $Ce^{3+}$  5d excitation at 430 nm (dotted). The intensity of the  $Ce^{3+}$  emission band for 430 nm excitation is scaled to that for 285 nm excitation.



**Fig. 4.** Energy level diagrams of  $Ce^{3+}$  and  $Pr^{3+}$  with the possible pathways of  $Pr^{3+} \rightarrow Ce^{3+} \rightarrow Pr^{3+}$  step energy transfers.

A notable result in Fig. 3 is that the intensity ratio of the red emission line of  $Pr^{3+}$  to the green emission band of  $Ce^{3+}$ , R/G ratio, for  $Pr^{3+}$  4f5d excitation at 285 nm is always larger than that for  $Ce^{3+}$  5d excitation at 430 nm. In view of negligible contribution of the nonradiative relaxation from  $Pr^{3+}$  4f5d to the red emission line, the enhancement of the red emission indicates that the  $Ce^{3+} \rightarrow Pr^{3+}$  energy back transfer is more efficient than the  $Ce^{3+} \rightarrow Pr^{3+}$  energy transfer. This feature can be well explained as preferential excitation of  $Ce^{3+}$  in the closely spaced  $Ce^{3+} - Pr^{3+}$  pairs due to the first step  $Pr^{3+} \rightarrow Ce^{3+}$  energy transfer upon  $Pr^{3+}$ 



**Fig. 5.** PL spectra of  $(Lu_{0.99-y}Ce_{0.01}Pr_y)_3Al_5O_{12}$ , (y=0.001-0.02) upon  $Pr^{3+}$  4f5d excitation at 285 nm (solid), and/or upon  $Ce^{3+}$  5d excitation at 430 nm (dotted). The intensity of the Ce3+ emission band for 430 nm excitation is scaled to that for 285 nm excitation.

4f5d excitation. Here, we define n by

$$n = \frac{(R/G)_{Pr^{3}+4f5d}}{(R/G)_{Ce^{3}+5d}} \tag{1}$$

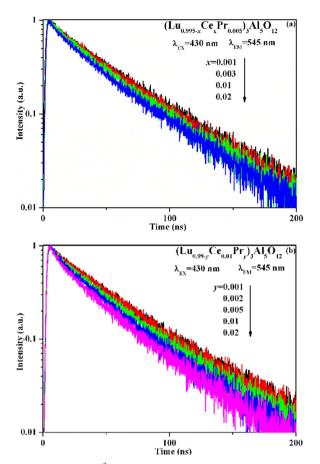
The subscript  $(Pr^{3+} 4f5d \text{ or } Ce^{3+} 5d)$  indicates the excitation level for which the R/G ratio is obtained. One can find from Fig. 3 that the n values increase with increasing  $Ce^{3+}$  concentration up to 0.02.

For comparison the emission spectra of sample series B:  $(Lu_{0.99-y}Ce_{0.01}Pr_y)_3Al_5O_{12}$ , (y=0.001-0.02) with a fixed  $Ce^{3+}$  concentration at 0.01 and various  $Pr^{3+}$  concentrations are also measured, as shown in Fig. 5. Obviously, there is a high n value for low  $Pr^{3+}$  concentration and it reduces with increasing  $Pr^{3+}$  concentration.

From the definition of n, its value is determined by  $\eta_{ET}$ , the efficiency of  $Ce^{3+} \rightarrow Pr^{3+}$  energy back transfer upon  $Pr^{3+}$  4f5d excitation, and  $\eta'_{ET}$ , the efficiency of  $Ce^{3+} \rightarrow Pr^{3+}$  energy transfer upon  $Ce^{3+}$  5d excitation, written as

$$n = \frac{(R/G)_{\text{Pr}^3 + 4f5d}}{(R/G)_{\text{Ce}^3 + 5d}} = \frac{\left(\frac{\eta_{\text{ET}}\eta_{\text{A}}}{1 - \eta_{\text{ET}}}\right)_{\text{Pr}^3 + 4f5d}}{\left(\frac{\eta'_{\text{ET}}}{1 - \eta'_{\text{ET}}}\right)_{\text{Ce}^3 + 5d}}$$
(2)

where  $\eta_A$  is the radiative efficiency of  $Pr^{3+}:^1D_2$  level, which is a conctant and does not change with the excitation wavelength. To calculate  $\eta_{ET}$ ,  $\eta'_{ET}$  must be obtained first. As shown in Fig. 6(a) and (b), the decay curves of  $Ce^{3+}$  emission upon  $Ce^{3+}$  5d excitation are measured for both the sample series A:  $(Lu_{0.995-x}Ce_xPr_{0.005})_3Al_5O_{12}$ , (x=0.001-0.02) and the sample series B:  $(Lu_{0.99-y}Ce_{0.01}Pr_y)_3Al_5O_{12}$ , (y=0.001-0.02). For comparison, the decay curves of  $Ce^{3+}$  emission upon  $Pr^{3+}$  4f5d excitation are also shown in Fig. 7(a) and (b). Upon  $Ce^{3+}$  5d excitation, the decay becomes faster with increasing the dopant concentrations due to energy transfer from  $Ce^{3+}$  to  $Pr^{3+}$ . However, one can find from Fig. 7 that the decay curves of  $Ce^{3+}$ 



**Fig. 6.** Decay curves of  $Ce^{3+}$  emission in  $(Lu_{0.995-x}Ce_xPr_{0.005})_3Al_5O_{12}$ , (x=0.001-0.02) (a) and  $(Lu_{0.99-y}Ce_{0.01}Pr_y)_3Al_5O_{12}$ , (y=0.001-0.02) (b) upon  $Ce^{3+}$  5d excitation at 430 nm.

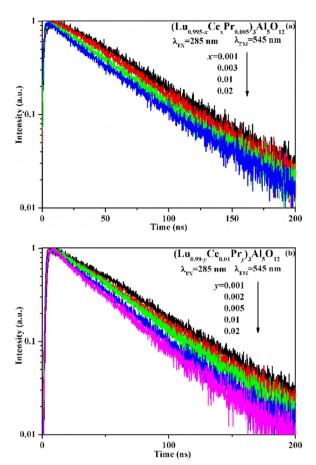
upon  $Pr^{3+}$  4f5d excitation do not appear a fast decay compared with that upon  $Ce^{3+}$  direct excitation. It seems inconsistent with the efficient energy back transfer from  $Ce^{3+}$  to  $Pr^{3+}$ . This behaviour can be understood considering the existence of population build up process of  $Ce^{3+}$  emission due to energy transfer from  $Pr^{3+}$  to  $Ce^{3+}$ . We can see the rising time when  $Ce^{3+}$  emission reaches the maximum upon  $Pr^{3+}$  4f5d excitation is continuously reduced with the increase of dopant concentrations, reflecting that the energy transfer from  $Pr^{3+}$  to  $Ce^{3+}$  continuously shortens the lifetime of  $Pr^{3+}$  4f5d level. Although the rising time is shown to be shorter than 10 ns, the slow rising edge followed with slow decay contributed by distant  $Pr^{3+}$ - $Ce^{3+}$  are still hidden in the temporal behaviour. As a result, the expected fast decay of  $Ce^{3+}$  upon  $Pr^{3+}$  4f5d excitation may be covered by the slow build up and decay processes, leading to a slow decay pattern.

The transfer efficiency upon  $Ce^{3+}$  5*d* excitation can be given by [18]

$$\eta_{ET}' = 1 - \int_0^\infty I(t)dt/\tau_0 \tag{3}$$

where I(t) is the  $Ce^{3+}$  fluorescence decay function with a unit initial intensity;  $\tau_0$  is the fluorescence lifetime of  $Ce^{3+}$  in the absence of  $Pr^{3+}$ . The calculated energy back transfer efficiencies using Eq. (2) are listed in Table 1 and Table 2.

From Tables 1 and 2, one can find that the n values increase with increasing  $Ce^{3+}$  concentration for sample series A and decrease with increasing  $Pr^{3+}$  concentration for sample series B. As mentioned above, the photon-excitation of  $Pr^{3+}$  4f5d state can lead to preferential excitation of  $Ce^{3+}$  in the closely spaced  $Ce^{3+}$ - $Pr^{3+}$  pairs by  $Pr^{3+} \rightarrow Ce^{3+}$  energy transfer. For the sample series A, the average distance between the excited  $Ce^{3+}$  and it's



**Fig. 7.** Decay curves of  $Ce^{3+}$  emission in  $(Lu_{0.995-x}Ce_xPr_{0.005})_3Al_5O_{12}$ , (x=0.001-0.02) (a) and  $(Lu_{0.99-y}Ce_{0.01}Pr_y)_3Al_5O_{12}$ , (y=0.001-0.02) (b) upon  $Pr^{3+}$  4f5d excitation at 285 nm.

**Table 1**Fluorescent lifetimes and transfer efficiencies in Samples A: (Lu<sub>0.995-x</sub>Ce<sub>x</sub>Pr<sub>0.005</sub>)<sub>3</sub>Al<sub>5</sub>O<sub>12</sub>.

x	$\int_0^\infty I(t)dt$ (ns)	τ <sub>0</sub> (ns)	η'ετ	n	ηет
0.001	46.8	56.5	0.17	1.9	0.28
0.003	43.4	54.1	0.2	2.0	0.33
0.01	36.8	45.4	0.19	2.2	0.34
0.02	35.0	41.6	0.16	2.8	0.35

 $\label{eq:continuous} \textbf{Table 2} \\ \text{Fluorescent lifetimes and transfer efficiencies in Samples B: } (Lu_{0.99-y}Ce_{0.01}Pr_y)_3Al_5O_{12}. \\$ 

у	$\int_0^\infty I(t)dt$ (ns)	η' <sub>ET</sub>	п	ηЕТ
0	45.4			
0.001	42.8	0.06	6.5	0.29
0.002	40.8	0.1	3.8	0.30
0.005	36.8	0.19	2.2	0.34
0.01	33.4	0.26	1.5	0.35
0.02	27.8	0.39	1.2	0.43

adjacent  $Pr^{3+}$  upon  $Pr^{3+}$  4f5d excitation becomes shorter with the increase of  $Ce^{3+}$  concentration, thus enhancing the  $Ce^{3+} \rightarrow Pr^{3+}$  energy back transfer rate. Whereas, the photon-excitation of  $Ce^{3+}$  5d has no selectivity for the  $Ce^{3+}$ - $Pr^{3+}$  distance and the average distance for  $Ce^{3+} \rightarrow Pr^{3+}$  energy transfer is unchanged with

changing Ce<sup>3+</sup> concentration. For the sample series B, the average rate for the  $Ce^{3+} \rightarrow Pr^{3+}$  energy transfer upon  $Ce^{3+}$  5d excitation is proportional to  $Pr^{3+}$  concentration. While the  $Ce^{3+} \rightarrow Pr^{3+}$  energy back transfer upon Pr<sup>3+</sup> 4f5d excitation includes transfer from  $Ce^{3+}$  to the close  $Pr^{3+}$  and the distant  $Pr^{3+}$ . At low concentration of  $Pr^{3+}$ , the  $Ce^{3+} \rightarrow Pr^{3+}$  energy transfer rate upon  $Ce^{3+}$  5d excitation is low simultaneously, however, the  $Ce^{3+} \rightarrow Pr^{3+}$  energy back transfer is still effective due to the back transfer to the close Pr<sup>3+</sup>, the rate of which is independent of Pr<sup>3+</sup> concentration. As a result, there is a big n value for low concentration of Pr<sup>3+</sup>. With increasing Pr<sup>3+</sup> concentration, the average rate for the  $Ce^{3+} \rightarrow Pr^{3+}$  normal energy transfer is increased. while the average rate for the  $Ce^{3+} \rightarrow Pr^{3+}$  back transfer is also increased because the back transfer from Ce<sup>3+</sup> to distant Pr<sup>3+</sup> ions becomes more and more important and even dominates the overall transfer for a sufficient high concentration of  $Pr^{3+}$ . Hence, the n values reduce with the increase of  $Pr^{3+}$  concentration and it is expected to be 1 at high Pr<sup>3+</sup> concentration similar to the case for  $Pr^{3+}$  concentration of 0.02 with n = 1.2 in this work.

#### 4. Conclusions

In summary, Upon  $Pr^{3+}$  4f5d state excitation, the step energy transfers from  $Pr^{3+}$  4f5d state to  $Pr^{3+}$  5d state followed by energy back transfer from  $Pr^{3+}$  5d state to  $Pr^{3+}$   $1D_2$  level are studied in  $Pr^{3+}$   $1D_2$  level are studied in  $Pr^{3+}$  singly doped sample. The back transfer results in strongly enhanced red emission line of  $Pr^{3+}$  in the codoped sample compared with  $Pr^{3+}$  singly doped sample. The efficiencies of  $Pr^{3+}$  energy back transfer are evaluated. It is evidently found that the  $Pr^{3+}$  energy back transfer upon  $Pr^{3+}$   $Pr^{3+}$  energy transfer upon  $Pr^{3+}$ 

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