

Identification and thermodynamic mechanism of the phase transition in hafnium nitride films

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Abstract—A stoichiometry-driven phase transition from rocksalt to “nitrogen-rich” structure exists in *group-IVB* transition metal nitride films. As this phase transition is critical in controlling the film properties it has attracted numerous studies. However, researchers are still divided with regard to the structural identity of this “nitrogen-rich” phase, not to mention detailed exploration of the phase transition mechanisms. In this study, we confirmed that the “nitrogen-rich” phase in hafnium nitride (HfN_x) films had a cubic Th_3P_4 structure of space group symmetry of $I-43d$ (220), namely $c\text{-Hf}_3\text{N}_4$. The confirmation was obtained by combining the first-principle calculations with a series of experiments: Selected Area Electron Diffraction, High Resolution Transmission Electron Microscopy, Raman, Grating Incident X-ray Diffraction and X-ray Photoelectron Spectroscopy. The mechanisms of the phase transition were elucidated through calculations on enthalpy of formation (*EOF*). The experimental results agree well with the theoretical calculations. We conclude that with increasing nitrogen, phase transition takes place from rocksalt ($\delta\text{-HfN}$) to $c\text{-Hf}_3\text{N}_4$ through three stages of structural evolution: $\delta\text{-HfN}$ (containing Hf vacancies) \rightarrow mixture of ($\delta\text{-HfN} + c\text{-Hf}_3\text{N}_4$) $\rightarrow c\text{-Hf}_3\text{N}_4$. The driving force of the phase transition is energy minimization. The three stages of structural evolution are explained by comparing the *EOF* of the $\delta\text{-HfN}$ and $c\text{-Hf}_3\text{N}_4$ phases. As the phase transition takes place, the hafnium nitride film morphs from a conductive and opaque metal into an insulating and transparent semiconductor.

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1. Introduction

Transition metal nitrides are well known as a class of fascinating and technologically important materials in the fields of electronic devices, cutting- and machining-tool industry [1–3]. Among them, hafnium nitride (HfN_x) and zirconium nitride (ZrN_x) films have attracted much attention recently [4–6] because of their high electrical conductivity, large “phononic band gap”, small real permittivity, high infrared reflectance coupled with high abrasion, corrosion resistance and thermal stability [7–10]. These make them very promising candidates for use as counter electrode in dyesensitized solar cells [11], hot carrier solar cell absorber [12], alternative plasmonic materials [13], solar control

coatings on windows [14], decorative coatings [15], as well as reflecting back contacts in solar cells [5,16] and light-emitting-diode (LED) devices [17]. In these applications, electric and optical properties are of utmost importance. ZrN_x and HfN_x films exist in various phase structures thus present different electric and optical properties [14,18]. To obtain tailored properties for desired applications, therefore, it is crucial to understand how to control the phase structure.

Stoichiometry (x) is an important factor in determining phase structure [14,18,19]. Extensive studies confirm that near-stoichiometric ($x = 1.00$) HfN_x and ZrN_x films are of a thermodynamically most stable rocksalt structure [20]. In this structure, the films are optically opaque, gold-like in color, highly infrared reflecting as well as electrically conductive [14,17]. Interestingly, as x increases from ~ 1.00 to ~ 1.33 , a phase transition from rocksalt structure to a so-called “nitrogen-rich” phase takes place [21]. Different from rocksalt phase, the films with “nitrogen-rich” phase are optically transparent and electrically

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insulating, plus many novel physical properties [22–24]. Obviously this phase transition is important for controlling the properties of the films thus attracting numerous studies. Still, the following three problems remain concerning the identity of the “nitrogen-rich” phase and the mechanisms of the phase transition: (i) What exactly is this “nitrogen-rich” phase? Some believed it was the orthorhombic structure (*o*- TM_3N_4) [18,25–27], some thought it was the cubic Th_3P_4 structure (*c*- TM_3N_4) [24,28–30], others believed that it was still the rocksalt structure [31,32], but this rocksalt structure contained some point defects and lattice distortion (δ - TM_3N_4). (ii) How does the rocksalt phase of $x = 1/1$ transform to the “nitrogen-rich” phase of $x = 4/3$? Does it occur gradually or abruptly? Studies show that stoichiometry of the films can be continuously increased by increasing the nitrogen flow rate, or manipulating other deposition conditions [24,33,34]. In these reports, the phase structures corresponding to a different stoichiometry are not identified, and the details of the transition are unrevealed. (iii) Why does the phase transition take place? i.e., what is the driving force? So far, the mechanisms on phase transition are still not well explored.

With the above three questions in mind, we sputtered HfN_x films with different x through controlling of nitrogen flow rate, and carried out three aspects of studies by employing the first-principle calculations in combination of the structural measurements, namely, Selected Area Electron Diffraction (SAED), High Resolution Transmission Electron Microscopy (HRTEM), Raman, Grating Incident X-ray Diffraction (GIXRD) and X-ray Photoelectron Spectroscopy (XPS). These studies are: (i) identifying structure of the “nitrogen-rich” phase of the HfN_x films; (ii) elucidating the structural evolution process from rocksalt to “nitrogen-rich” phase; and, (iii) clarifying the phase transition mechanism by calculating the enthalpy of formation (*EOF*) at different x . These three aspects of studies are discussed in detail in Sections 3.1, 3.2 and 3.3, respectively. Our experiments and calculations agree well, thus proving three points: (i) This “nitrogen-rich” phase of HfN_x films has a cubic Th_3P_4 structure (i.e., *c*- Hf_3N_4); (ii) The phase transition from rocksalt (δ - HfN) to *c*- Hf_3N_4 is not an abrupt but a gradual transition process of three distinct stages of structural evolution; (iii) The driving force of the phase transition is energy minimization; all these three stages of structural evolution are well explained by comparing the *EOF* of the δ - HfN and the *c*- Hf_3N_4 phases.

2. Experimental and computational details

2.1. Preparation and characterization of the HfN_x films

HfN_x films with a thickness of about 600 nm were simultaneously deposited on single-crystal Si (001) wafers and optical glass substrates by radio-frequency (RF) reactive sputtering a pure Hf target in the mixed discharge gases of Ar and N_2 [35]. The distance between the target and substrate holder was fixed at 55 mm, and the chamber was evacuated by a turbomolecular pump to 4×10^{-4} Pa prior to deposition. Prior to entry into the vacuum chamber, the Si wafer and the glass substrates were cleaned ultrasonically in acetone, alcohol and distilled water, consecutively. During the deposition, the flow rate of Ar and N_2 was accurately controlled by independent mass flow controllers.

Stoichiometry x in HfN_x films was varied from 1.039 to 1.334 by increasing the flow rate ratios of $\text{N}_2/(\text{Ar} + \text{N}_2)$ from 3% to 50% while the RF power, work pressure, substrate negative bias and substrate temperature were kept constant at 150 W, 1.0 Pa, -80 V and 200°C , respectively. X-ray diffraction (XRD) measurements were carried out in both symmetric $\theta/2\theta$ and grazing-incidence (GIXRD) modes of a Bruker D8tools X-ray diffractometer using $\text{Cu K}\alpha$ as the incident radiation. The microstructure of the films was characterized using a high-resolution transmission electron microscope (HR-TEM, JEOL TEM-2010). The stoichiometry x and core-level spectra of the films was determined by XPS measurements (VG ESCA LAB MKII), in which a monochromatized $\text{Al K}\alpha$ (1486.6 eV) X-ray source was used, and Ar^+ cleaning procedure lasting 180 s was applied to all samples prior to XPS quantitative analysis to remove possible adventitious carbon and absorbed oxygen from the sample surface. Raman measurements (T64000 (Horiba)) were obtained by using a 633 nm line Ar^+ laser excitation with a laser power of 200 mW, and an accumulation time of 30 s under the frequency range of $50\text{--}1600\text{ cm}^{-1}$. The transmission spectrum in the range of 300–2500 nm was obtained by a PerkinElmer Lambda 900 Ultraviolet–visible–near infrared (UV–vis–NIR) spectrometer. The optical gap of the films was determined by plotting $(\alpha h\nu)^2$ against the photon energy $h\nu$ according to the Tauc equation. The film thickness was determined by using a Dektak³ surface profile measuring system.

2.2. Computational methodology

Density functional theory (DFT) calculations were performed to explore the electronic structure of the defective and non-defective HfN_x in the rocksalt structure and Hf_3N_4 in cubic Th_3P_4 structure. The method of projector-augmented wave potentials was employed as implemented in the Vienna ab initio simulation package (VASP) code [36,37]. The generalized gradient approximation (GGA) with the parametrization of Perdew–Burke–Ernzerhof (PBE) was used to express the exchange–correlation energy of interacting electrons [38]. The kinetic energy cutoff of 550 eV was used for the plane wave expansion. The Monkhorst–Pack method was used to sample the k points. The Brillouin zones are sampled with the high-density Γ -centered k -point grid. The spin-polarization effect has been considered in the calculation. The introduction of point defects in HfN_x does not induce the localized magnetic moment nor result in the spin-polarization. The calculated lattice constant of pristine HfN of space group Fm-3m is 4.53 Å, very close to that from the measurements (~ 4.58 Å). To model high- and low-point defect concentration, one or two Hf vacancies are considered in the ideal 8-, 12-, 16-, 18-, 24-, and 32-atom HfN cells. A 28-atom supercell was used in modeling the cubic- Th_3P_4 -structured Hf_3N_4 of space group $I-43d$. The calculated lattice constant is 6.69 Å, very close to that from the measured (~ 6.71 Å).

3. Results and discussion

3.1. Structure identification of the “nitrogen-rich” phase

Fig. 1a and b plots the Selected Area Electron Diffraction (SAED) patterns of the near-stoichiometric

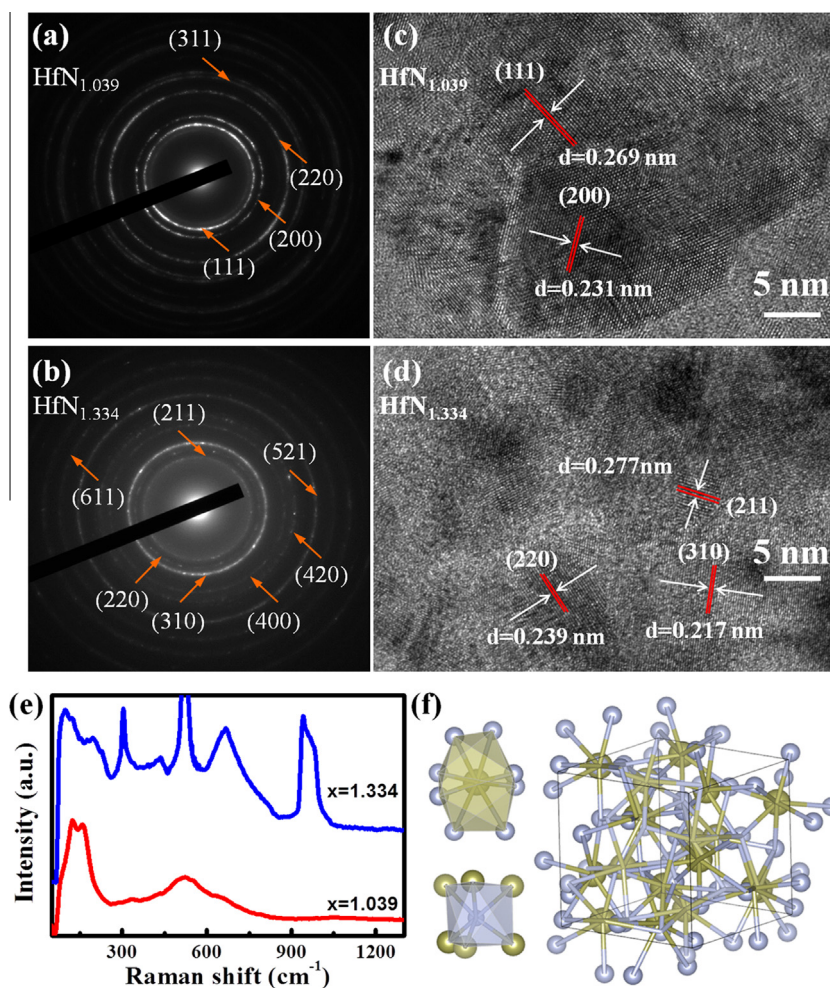


Fig. 1. The (a and b) SAED patterns, (c and d) HRTEM lattice images, (e) Raman spectra for nearly-stoichiometry $\text{HfN}_{1.039}$ and “nitrogen-rich” $\text{HfN}_{1.334}$ films. The (f) coordination polyhedral of atoms in $c\text{-Hf}_3\text{N}_4$: the $\{\text{Hf}\}\text{N}_8$ bisdisphenoid and the $\{\text{N}\}\text{Hf}_6$ metaprism.

$\text{HfN}_{1.039}$ and the “nitrogen-rich” $\text{HfN}_{1.334}$ films, respectively. In the near-stoichiometric film (Fig. 1a), the diffraction rings are assigned to (111), (200), (220) and (311) in the rocksalt phase, indicating that the near-stoichiometric film has only a single-phase rocksalt structure ($\delta\text{-HfN}$ phase). In the “nitrogen-rich” film (Fig. 1b), however, all those diffraction rings disappear, and new diffraction rings emerge. In order to identify these unknown diffraction rings, we obtained the interplanar spacings of the perfect Hf_3N_4 crystal with cubic Th_3P_4 structure ($c\text{-Hf}_3\text{N}_4$) by first-principles calculations. The corresponding results are tabulated in Table 1. The measured values of interplanar spacings in the “nitrogen-rich” $\text{HfN}_{1.334}$ film are in good agreement with the calculation for $c\text{-Hf}_3\text{N}_4$ crystal. Based on the calculated results of the interplanar spacings, the experimentally observed diffraction rings can thus be indexed as $c\text{-Hf}_3\text{N}_4$ (211), (220), (310), (400), (420), (521) and (611), respectively. Since nothing but the diffraction rings from $c\text{-Hf}_3\text{N}_4$ phase appear in the SAED image in Fig. 1b, this “nitrogen-rich” $\text{HfN}_{1.334}$ film is believed to have a pure $c\text{-Hf}_3\text{N}_4$ structure.

Fig. 1c and d displays the HRTEM lattice images for the near-stoichiometric $\text{HfN}_{1.039}$ and the “nitrogen-rich” $\text{HfN}_{1.334}$ films, respectively, wherein the nanograins are uniformly distributed on the film surface. In the near-

stoichiometric film, the interplanar distances are found to be 0.269 and 0.231 nm, matching well with the (111) and (200) plane distances in $\delta\text{-HfN}$ phase. In the “nitrogen-rich” film, the measured interplanar spacings are consistent with the calculated values for (211), (220) and (310) planes in the perfect $c\text{-Hf}_3\text{N}_4$ crystal (Table 1), indicating that the “nitrogen-rich” $\text{HfN}_{1.334}$ film is crystallized into $c\text{-Hf}_3\text{N}_4$ phase. This also agrees well with the results from SAED.

Fig. 1e plots the Raman spectra for the near-stoichiometric $\text{HfN}_{1.039}$ and the “nitrogen-rich” $\text{HfN}_{1.334}$ films. In the near-stoichiometric film, the first-order acoustic and optical peaks at 168, 189 and 532 cm^{-1} occur simultaneously, indicating that the near-stoichiometric film has a $\delta\text{-HfN}$ phase containing hafnium vacancies [39]. However, in the “nitrogen-rich” $\text{HfN}_{1.334}$ film, the peaks from the $\delta\text{-HfN}$ phase disappear, and many new peaks emerge. Among them, two peaks located at $\sim 520\text{ cm}^{-1}$ and 965 cm^{-1} arise from the silicon substrate, and their appearance indicates that the film is optically transparent. This observation agrees well with the optical transmission measurements, proving that the “nitrogen-rich” film possesses semiconducting behavior, which is totally different from the metallic characteristics of the near-stoichiometric film. In addition to the two peaks from silicon substrate, there are

Table 1. Measured interplanar spacing (d) of the “nitrogen-rich” $\text{HfN}_{1.334}$ film by SAED, HRTEM and GIXRD experiments. For the sake of comparison, the theoretical values of $c\text{-Hf}_3\text{N}_4$ obtained by first-principles calculations are also shown.

hkl	Theoretical 2θ	Theoretical d (Å)	Measured d (Å) (SAED)	Measured d (Å) (HRTEM)	Measured d (Å) (GIXRD)
211	32.80	2.73	2.74	2.77	2.72
220	38.01	2.37	2.38	2.39	–
310	42.76	2.11	2.16	2.17	–
400	55.03	1.67	1.67	–	1.64
420	62.06	1.49	1.49	–	–
521	78.29	1.22	1.24	–	–
611	90.56	1.08	1.08	–	–

Table 2. Measured peak positions (cm^{-1}) of Raman spectra of the “nitrogen-rich” $\text{HfN}_{1.334}$ film. For the sake of comparison, the calculated values of $c\text{-Hf}_3\text{N}_4$ reported by Kroll and the measured values of $c\text{-Zr}_3\text{N}_4$ reported by Zerr are also shown.

Calculated $c\text{-Hf}_3\text{N}_4$	Measured $c\text{-Zr}_3\text{N}_4$	Measured $\text{HfN}_{1.334}$
111	136	111
229	161	195
362	323	302
432	424	434
695	668	669

five unknown peaks centered at 111, 195, 302, 434 and 669 cm^{-1} . To identify these peaks, we tabulated in Table 2 the positions of Raman peaks of $c\text{-Hf}_3\text{N}_4$ were calculated by Kroll [40] and those of $c\text{-Zr}_3\text{N}_4$ were measured by Zerr [41]. It can be clearly seen that the peak positions of the present “nitrogen-rich” film are not only consistent with the theoretical calculations of $c\text{-Hf}_3\text{N}_4$, but are also fairly close to the measured values of $c\text{-Zr}_3\text{N}_4$. This observation further confirms that our “nitrogen-rich” film is of the $c\text{-Hf}_3\text{N}_4$ structure.

Our SAED, HRTEM and Raman measurements unambiguously prove that the “nitrogen-rich” hafnium nitride film has the cubic Th_3P_4 structure. Its lattice parameter a_0 , obtained by diffraction data, is about $\sim 6.71\text{ Å}$ and its space group symmetry is $I\bar{4}3d$ (220) [34]; Hf atoms are in 12a and N atoms are in 16c. The coordination polyhedral of atoms in $c\text{-Hf}_3\text{N}_4$ is shown in Fig. 1f, where Hf is coordinated by 8 N atoms forming $\{\text{Hf}\}\text{N}_8$ bisdisphenoids. The eight surrounding N atoms build two tetrahedral intergrown into each other. N is coordinated by six Hf atoms forming $\{\text{N}\}\text{Hf}_6$ metaprisms, an environment between octahedral and trigonal prismatic.

3.2. Structural evolution during phase transition

Understanding the nature of the “nitrogen-rich” phase, we now investigate the detail of the phase transition from $\delta\text{-HfN}$ to $c\text{-Hf}_3\text{N}_4$ by XRD and XPS. Fig. 2a and b plot the GIXRD and symmetric $\theta/2\theta$ XRD spectra for HfN_x films with different x ($1.039 \leq x \leq 1.334$). At $x = 1.039$ and 1.165, four diffraction peaks ($2\theta = 33.65^\circ$, 39.27° , 56.78° , 67.94°) appear attributing to (111), (200), (220) and (311) in the $\delta\text{-HfN}$ phase. In this region, no other peaks are observed, indicating the films are of pure $\delta\text{-HfN}$ phase. In contrast, at $x = 1.334$, the diffraction peaks from $\delta\text{-HfN}$ structure completely disappear, and new peaks emerge that are assigned to (211) and (400) in the $c\text{-Hf}_3\text{N}_4$ phase (c.f., Table 1), indicating pure $c\text{-Hf}_3\text{N}_4$ structure appears when $x = 1.334$. These observations are in good agreement with the above SAED, HRTEM and Raman analysis. Interestingly, as x falls in between 1.195 and 1.278, the diffraction peaks from both $\delta\text{-HfN}$ and $c\text{-Hf}_3\text{N}_4$ phases are observed, indicating co-existence of both structures in the same film. Furthermore, it can be seen from the GIXRD spectra (Fig. 2a) that as x increases from 1.195 to 1.278, the intensity of the diffraction peaks from $\delta\text{-HfN}$ phase (200), (220) and (311) become weaken, while that of the (400) diffraction peak ($2\theta = 55.90^\circ$) from $c\text{-Hf}_3\text{N}_4$ gets stronger. Meanwhile, the dominant diffraction peak gradually shifts from larger $\delta\text{-HfN}$ (111) 33.65° to smaller $c\text{-Hf}_3\text{N}_4$ (211) 32.79° . These phenomena all point to one fact: with x increases from 1.195 to 1.278, the fraction of $\delta\text{-HfN}$ phase gradually decreases while that of the $c\text{-Hf}_3\text{N}_4$ phase gradually increases. This is further confirmed by XPS measurements.

Fig. 3 plots the XPS N1s core-level spectra for HfN_x films with different x , where no apparent changes in the

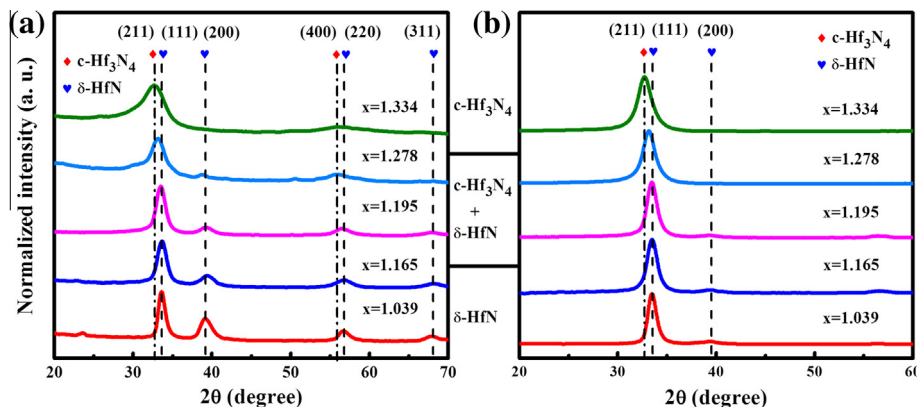


Fig. 2. The (a) GIXRD and (b) symmetric $\theta/2\theta$ XRD spectra for HfN_x films with different x .

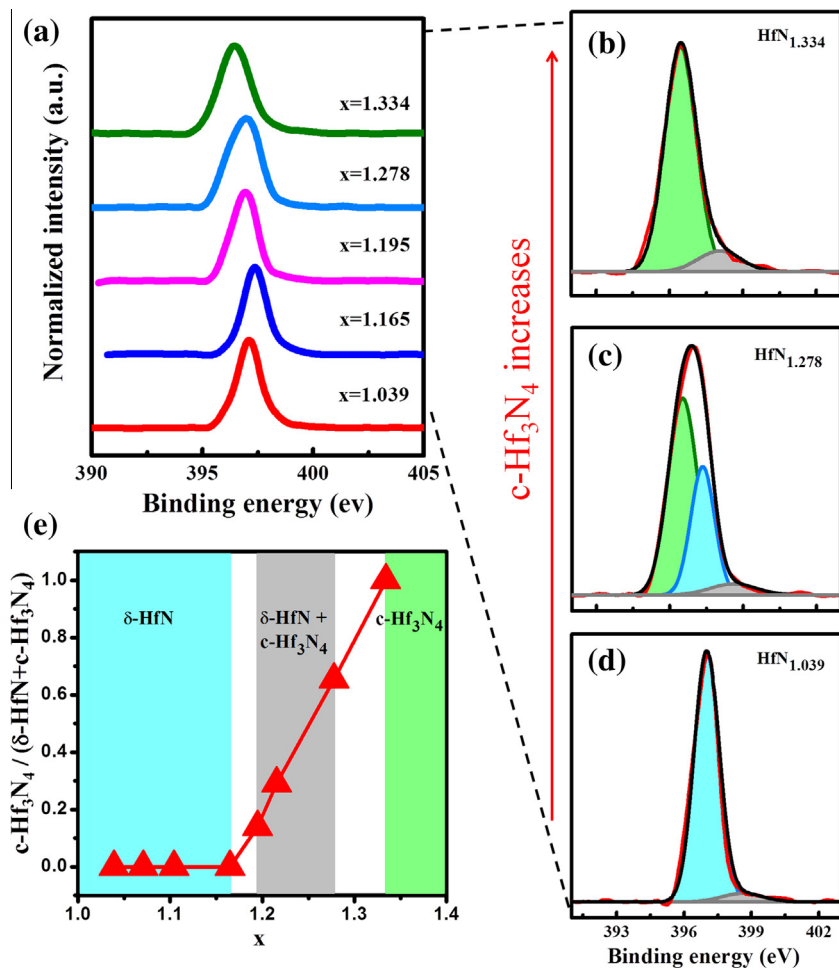


Fig. 3. The (a) XPS N1s core-level spectra for HfN_x films with different x , (b–d) the schematic deconvolution of typical N1s spectra, and (e) the ratios between integrated intensities of de-convoluted components, $c\text{-Hf}_3\text{N}_4/(\delta\text{-HfN} + c\text{-Hf}_3\text{N}_4)$.

features of N1s curves are observed as x increases from 1.039 to 1.165, indicating that the bonding state of N atoms does not change significantly. However, as x increases further from 1.165 to 1.334, the N1s peaks gradually shift to lower binding energy and show asymmetric line shape with a tailing toward lower binding energy. These results clearly indicate that the chemical environment surrounding the incorporated N atoms is significantly changed by the increase in x . To further analyze the evolution process, the decomposition of N1s spectra has been performed, and the corresponding results are shown in Fig. 3b–d. The N1s spectra for the films with $1.039 \leq x \leq 1.165$ are nicely deconvoluted into two peaks (Fig. 3d), with the stronger one located at ~ 397.1 eV assigned to N–Hf bonds in $\delta\text{-HfN}$ phase [42] and the weaker one centered at ~ 398.4 eV ascribed to N–N and/or N–O bonds [42]. In contrast, the N1s spectra for the films with $1.195 \leq x \leq 1.278$ are split nicely into three peaks (Fig. 3c). The two peaks at the higher binding energy of ~ 397.1 eV and ~ 398.4 eV come from N–Hf bonds in $\delta\text{-HfN}$ phase and N–N and/or N–O bonds. The third peak located at a lower binding energy of ~ 396.4 eV is assigned to N–Hf bonds in $c\text{-Hf}_3\text{N}_4$ phase based on the results of the previous studies [42,43]. The emergence of this peak indicates that $c\text{-Hf}_3\text{N}_4$ phase gradually forms as x further increases. For sample with $x = 1.334$ (Fig. 3b), only

N–Hf peak from $c\text{-Hf}_3\text{N}_4$ phase exists in addition to N–N and/or N–O peak, indicating that these films are of pure $c\text{-Hf}_3\text{N}_4$ phase, matching well with the above SAED, HRTEM, Raman and XRD results. The ratios $c\text{-Hf}_3\text{N}_4/(\delta\text{-HfN} + c\text{-Hf}_3\text{N}_4)$ of the integrated intensities of the deconvoluted components are calculated from Fig. 3b–d and plotted in Fig. 3e as a function of x . It can be seen that the HfN_x films with $x \leq 1.165$ and $x = 1.334$ are composed of pure $\delta\text{-HfN}$ phase and $c\text{-Hf}_3\text{N}_4$ phase, respectively. The films with $1.195 \leq x \leq 1.278$ consist of mixture phase of $\delta\text{-HfN}$ and $c\text{-Hf}_3\text{N}_4$. As x increases from 1.195 to 1.278, $\delta\text{-HfN}$ gradually reduces while the $c\text{-Hf}_3\text{N}_4$ phase increases at the same time.

The XRD and XPS results are in good agreement with above SAED, HRTEM and Raman results, all pointing to the same conclusion: when $x = 1.334$ the film is composed of a pure $c\text{-Hf}_3\text{N}_4$ phase. The structural transition from $\delta\text{-HfN}$ phase to $c\text{-Hf}_3\text{N}_4$ phase is not an abrupt but a gradual process going through the following three stages of structural evolution: (i) Stage I, $1.039 \leq x \leq 1.165$, features rocksalt structure containing Hf vacancies (V_{Hf}). As x increases Hf vacancies in the films increase. As a result, lattice distortion takes place, but the $\delta\text{-HfN}$ structure still remains. This has been proved by a series of experiments and calculations in our previous study [44]. (ii) Stage II, $1.195 \leq x \leq 1.278$, is a two-phase region where rocksalt $\delta\text{-HfN}$

HfN phase coexists with $c\text{-Hf}_3\text{N}_4$ phase. As x arrives at about 1.195, $c\text{-Hf}_3\text{N}_4$ phase appears in the film, and it gradually increases as x increases. Stage II is a transitional stage. (iii) Stage III, $x = 1.334$, features pure $c\text{-Hf}_3\text{N}_4$ phase. Attainment of x as 1.334, or N to Hf ratio becomes 4 to 3, marks the completion of the $\delta\text{-HfN}$ to $c\text{-Hf}_3\text{N}_4$ transition, i.e., at this point, the $\delta\text{-HfN}$ phase completely transforms into $c\text{-Hf}_3\text{N}_4$ phase.

In summary, the phase evolution progresses as follows, as x in HfN_x increases from about 1/1 to 4/3: V_{Hf} -containing $\delta\text{-HfN} \rightarrow$ mixture of $(\delta\text{-HfN} + c\text{-Hf}_3\text{N}_4) \rightarrow$ pure $c\text{-Hf}_3\text{N}_4$.

3.3. Structural evolution mechanism

To understand the reasons behind the above phase evolution process, we calculated the enthalpy of formation (EOF) for HfN_x at different x by first-principle calculations. To compare with the experiments, eight typical models corresponding to experimentally observed three-stage structural evolution were constructed. For the first stage of $1.000 < x \leq 1.165$, $\delta\text{-Hf}_{31}\text{N}_{32}$ ($x = 1.032$), $\delta\text{-Hf}_{15}\text{N}_{16}$ ($x = 1.067$) and $\delta\text{-Hf}_7\text{N}_8$ ($x = 1.143$) were established; for the second stage of $1.195 \leq x < 1.333$, $\delta\text{-Hf}_5\text{N}_6$ ($x = 1.200$) and $\delta\text{-Hf}_7\text{N}_9$ ($x = 1.286$); for the third stage of $x = 1.334$, $c\text{-Hf}_3\text{N}_4$ was constructed. Furthermore, we also established a defect-free ideal-stoichiometry $\delta\text{-HfN}$ and $\delta\text{-Hf}_3\text{N}_4$ containing a high concentration of V_{Hf} for comparison.

Considering Hf- and N-atom chemical potentials change with variation of deposition conditions such as N_2 partial pressure during practical film preparation, the enthalpy of formation for the compounds Hf_mN_n with different x (n/m) is defined as [45,46].

$$E^f(\mu_{\text{Hf}}, \mu_{\text{N}}) \approx [E_{\text{sys}}^{\text{total}} - m\mu_{\text{Hf}} - n\mu_{\text{N}}]/(m+n) \quad (1)$$

where, E^{total} is the total energy of the Hf–N system calculated using the supercell, and m and n are the number of Hf and N atoms in the supercell, respectively. Here, μ_{N} and μ_{Hf} are the N- and Hf-atom chemical potentials, respectively. The approximate equal sign “ \approx ” indicates that the entropic differences between the different structures are ignored. According to Eq. (1), a given structure will become *unstable* for combinations of μ_{Hf} and μ_{N} which results in $E^f(\mu_{\text{Hf}}, \mu_{\text{N}}) \geq 0$; that is, the structure becomes *endothermic*. For $\mu_{\text{N}} = 1/2E_{\text{N}_2}$ (half the total energy of an N_2 molecule), we call this the “nitrogen-rich” condition and choose it as the zero reference state (μ_{N}^0) of μ_{N} . Similarly, for $\mu_{\text{Hf}} = E_{\text{Hf-bulk}}$ (the total energy of bulk, Hf), we call this the “hafnium-rich” condition, and we choose it to be the zero reference state (μ_{Hf}^0) of μ_{Hf} . The hafnium-rich state reaches when there are excessive Hf atoms in the system compared to nitrogen molecules. Similarly the “nitrogen-rich” state arrives when there are excessive N_2 molecules in the system as compared to Hf atoms. According to Eq. (1), we have calculated the EOF of different theoretical models as a function of chemical potential, and the corresponding results are shown in Fig 4a and b. As is seen, the EOF of different Hf–N system gradually changes with varying N atom chemical potentials (keeping $\mu_{\text{Hf}} = \mu_{\text{Hf}}^0 = E_{\text{Hf-bulk}}$) and Hf atom chemical potentials (keeping $\mu_{\text{N}} = \mu_{\text{N}}^0 = 1/2E_{\text{N}_2}$), respectively. The most stable HfN_x system having the lowest EOF in a given range of μ_{N} and μ_{Hf} are thus identified, as highlighted in a different

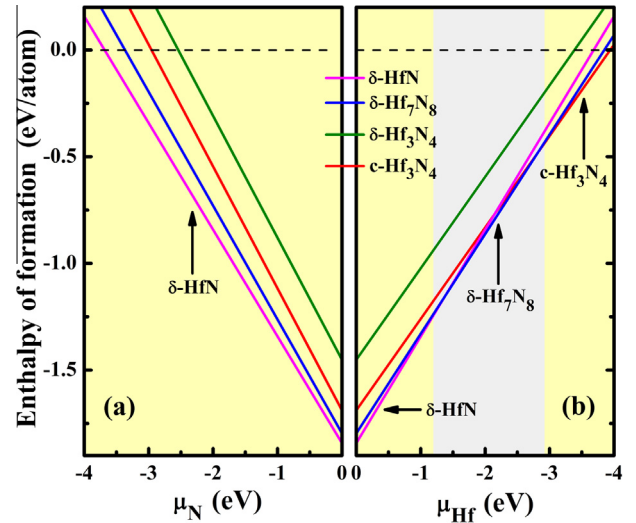


Fig. 4. Enthalpy of formation per atom: (a) as a function of μ_{N} for fixed $\mu_{\text{Hf}} = \mu_{\text{Hf}}^0 = E_{\text{Hf-bulk}}$ and (b) as a function of μ_{Hf} for fixed $\mu_{\text{N}} = \mu_{\text{N}}^0 = 1/2E_{\text{N}_2}$, where the most stable HfN_x systems in a specific range of μ_{N} and μ_{Hf} are highlighted in a different background color. The lines represent the following structures: magenta, defect-free $\delta\text{-HfN}$; blue, V_{Hf} -containing $\delta\text{-Hf}_7\text{N}_8$; olive, V_{Hf} -containing $\delta\text{-Hf}_3\text{N}_4$; red, $c\text{-Hf}_3\text{N}_4$. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

background color in Fig. 4. As μ_{N} varies from -4 to 0 , and μ_{Hf} from 0 to -4 , that is, as relative chemical potential of nitrogen gradually increases, the most stable HfN_x systems change from rocksalt $\delta\text{-HfN}$ (1.000), through Hf-vacancy-containing $\delta\text{-Hf}_{15}\text{N}_{16}$ (1.067), $\delta\text{-Hf}_7\text{N}_8$ (1.143), $\delta\text{-Hf}_5\text{N}_6$ (1.200) and finally to cubic $c\text{-Hf}_3\text{N}_4$ (only $\delta\text{-HfN}$, V_{Hf} -containing $\delta\text{-Hf}_7\text{N}_8$ and $c\text{-Hf}_3\text{N}_4$ are shown in Fig. 4 not to clutter the plot). These results are very consistent with the experimentally observed formation of Hf vacancies in the rocksalt phase as x increases and then the appearance of phase transition from $\delta\text{-HfN}$ to $c\text{-Hf}_3\text{N}_4$, indicating that the driving force of Hf vacancy formation and phase transition is the decrease in EOF, that is, the energy minimization.

Taking into consideration the vibrational contributions of different structures, we keep the Hf- and N-atom chemical potentials fixed and use the following formula to calculate the EOF per atom of Hf_mN_n with different x (n/m) and phases [45,46].

$$E^f = [E_{\text{sys}}^{\text{total}} - mE_{\text{Hf-bulk}} - n/2E_{\text{N}_2}]/(m+n) \quad (2)$$

where E^{total} is the total energies of hafnium nitride (Hf_mN_n), m and n are the number of Hf and N atoms in the supercell. μ_{Hf}^0 and μ_{N}^0 are the Hf- and N-atom chemical potentials, corresponding to the total energy of a free N_2 molecule and a bulk (hcp) Hf atom, respectively ($\mu_{\text{Hf}}^0 = E_{\text{Hf-bulk}}$, $\mu_{\text{N}}^0 = 1/2E_{\text{N}_2}$). The results are shown in Fig. 5, where $\delta\text{-HfN}$ has the lowest EOF (-1.842 eV), indicating that it is the thermodynamically most stable structure. As x increases from 1/1 ($\delta\text{-HfN}$) to 8/7 ($\delta\text{-Hf}_7\text{N}_8$, $\text{EOF} = -1.796$ eV), EOF increases slowly, indicating that a small amount of Hf vacancies introduced into the rocksalt structure does not significantly increase the total energy of the system. However, when x further increases from $\delta\text{-Hf}_5\text{N}_6$ (-1.766 eV), through $\delta\text{-Hf}_7\text{N}_9$ (-1.666 eV), to $\delta\text{-Hf}_3\text{N}_4$ (-1.451 eV) EOF of the rocksalt structured

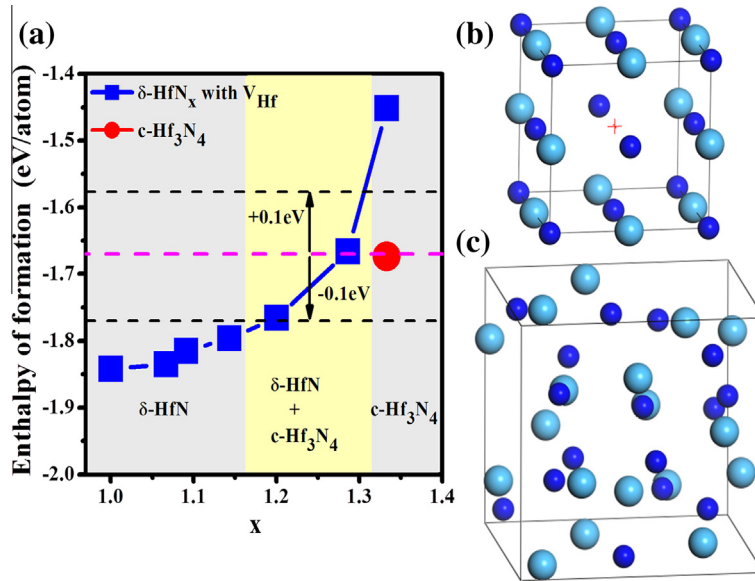


Fig. 5. (a) Enthalpy of formation of $\delta\text{-HfN}_x$ with different x and $c\text{-Hf}_3\text{N}_4$. (b) The typical rocksalt structure with Hf vacancy and (c) the cubic Th_3P_4 structure, wherein the large cyan and small blue balls represent Hf and N atoms, respectively. Three horizontal lines represent the positions of EOF for $c\text{-Hf}_3\text{N}_4$ (-1.674 eV) as well as 0.1 eV larger and smaller than EOF of $c\text{-Hf}_3\text{N}_4$ (-1.574 and -1.774 eV). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Hf_mN_n increases rapidly even beyond that of $c\text{-Hf}_3\text{N}_4$ (-1.674 eV) around $x = 1.286$ ($\delta\text{-Hf}_7\text{N}_9$). Based on the position of EOF of Hf–N systems with rocksalt structure (marked by blue color) relative to EOF of $c\text{-Hf}_3\text{N}_4$ (marked by red color), three distinct regions related to three-stage structure evolution can be distinguished in Fig. 5, indicating that the present three-stage structural evolution is attributed to the stoichiometry-induced change in EOF of $\delta\text{-HfN}$ phase [EOF ($\delta\text{-HfN}$)] relative to EOF of $c\text{-Hf}_3\text{N}_4$ phase [EOF ($c\text{-Hf}_3\text{N}_4$)]:

(i) In the first stage of $1.039 \leq x \leq 1.165$, EOF ($\delta\text{-HfN}$) \ll EOF ($c\text{-Hf}_3\text{N}_4$) (Fig. 5), the films keep a single-phase $\delta\text{-HfN}$ structure to decrease the total energy of the system (Figs. 1–3). In this stage the increase in x causes a gradual formation of Hf vacancies, which leads to a slight increase in EOF. However, the increased EOF is still far lower than that of the $c\text{-Hf}_3\text{N}_4$ (EOF difference exceeds 0.1 eV) (Fig. 5), therefore far from enough to induce a phase transition. Therefore, $\delta\text{-HfN}$ phase containing Hf vacancies is still stable in this stage.

(ii) In the second stage of $1.195 \leq x \leq 1.278$, EOF ($\delta\text{-HfN}$) \approx EOF ($c\text{-Hf}_3\text{N}_4$) (Fig. 5, EOF difference less than 0.1 eV), $\delta\text{-HfN}$ and $c\text{-Hf}_3\text{N}_4$ phases have thermodynamically similar stability, and therefore they coexist in the same film (Figs. 2 and 3). In this stage $c\text{-Hf}_3\text{N}_4$ phase appears, and its amount gradually increases at the expense of $\delta\text{-HfN}$ phase with increasing x (Figs. 2 and 3). When excessive Hf vacancies are formed in the rocksalt network ($1.165 \leq x \leq 1.195$), the lattice distortion becomes serious [44] and at the same time EOF of $\delta\text{-HfN}$ phase hikes close to or even higher than EOF of the $c\text{-Hf}_3\text{N}_4$ phase, rendering single-phase $\delta\text{-HfN}$ structure unstable. Therefore, $c\text{-Hf}_3\text{N}_4$ phase appears at about 1.195 to reduce the lattice distortion and EOF of the $\delta\text{-HfN}$ phase. As a result, a mixture of two phases co-exists (Figs. 2 and 3).

(iii) In the third stage of $x = 1.334$, EOF ($\delta\text{-Hf}_3\text{N}_4$) \gg EOF ($c\text{-Hf}_3\text{N}_4$) (Fig. 5, EOF difference greater

than 0.2 eV), the phase transition is finished and the films are composed of pure $c\text{-Hf}_3\text{N}_4$ phase (Figs. 1–3). As x arrives at $4:3$, EOF of the $c\text{-Hf}_3\text{N}_4$ phase (-1.674 eV) becomes much lower than that of $\delta\text{-HfN}$ phase with the same x , that is $\delta\text{-Hf}_3\text{N}_4$ (-1.451 eV). Naturally, the unstable $\delta\text{-HfN}$ phase disappears (Figs. 1–3) and only the $c\text{-Hf}_3\text{N}_4$ phase remains.

3.4. Phase-transition-induced evolution in electric and optical properties

To peek into the changes in electric and optical properties that the phase transition may have brought into the films, we made the relevant characterizations before and after the transition. Electrical resistivity measurements show that the film with $x = 1.039$ has a low electric resistivity of $110 \mu\Omega \text{ cm}$, indicating that the film of $\delta\text{-HfN}$ structure is highly conductive. However, when x increases to 1.334 , the electric resistivity of the film becomes as high as $45039 \mu\Omega \text{ cm}$, i.e., increased by nearly three orders of magnitude as compared to that at $x = 1.039$, meaning that the film of $c\text{-Hf}_3\text{N}_4$ structure is almost electrically insulating. Transmission spectra reveal that the transmittance of the film with $x = 1.039$ is almost zero (Fig. 6a), which agrees well with its resistivity results, indicating that the film of $\delta\text{-HfN}$ structure behaves metal-like. However, at $x = 1.334$, large number of interference fringes occur in transmission spectra and the film exhibits high transmittance in the visible to near infrared region, showing that the film is now transparent. This transmittance variation with x also leads to evolution in transparent appearance of the films, as shown in the inset of Fig. 6a. A background text of “HfN” covered by the $\text{HfN}_{1.039}$ film is completely invisible. However, when the $\text{HfN}_{1.039}$ film is replaced by the $\text{HfN}_{1.334}$, the background text becomes evident. These results converge to illustrate that the phase transition from $\delta\text{-HfN}$ to $c\text{-Hf}_3\text{N}_4$ changes an opaque film to transparent,

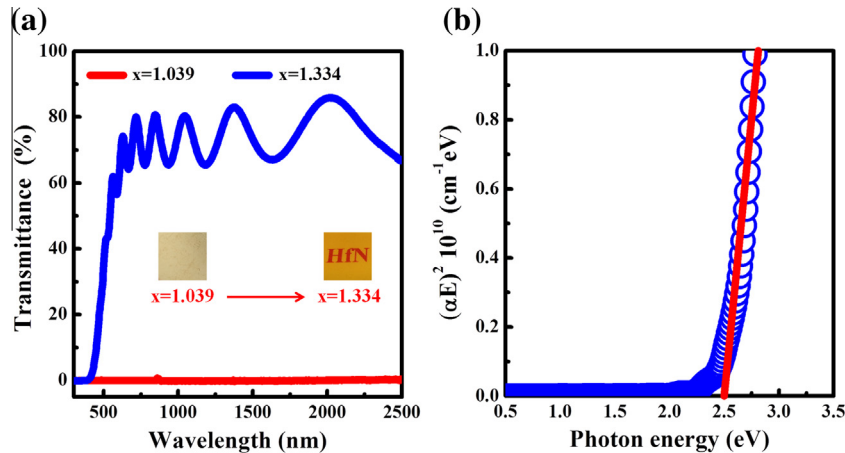


Fig. 6. The (a) Vis–NIR transmission spectra and (b) optical gap for nearly-stoichiometry $\text{HfN}_{1.039}$ and “nitrogen-rich” $\text{HfN}_{1.334}$ films.

as is expected from the optical gap measurement of about 2.5 eV (Fig. 6b) by the well-known Tauc formula [28]. These optical and electric measurements are in good agreement, demonstrating that the δ -HfN to c -Hf₃N₄ phase transition transforms hafnium nitride films from metals to semiconductors.

4. Conclusions

We have successfully identified the “nitrogen-rich” phase of hafnium nitride (HfN_x) films through a combination of SAED, HRTEM, Raman, XRD and XPS measurements and the first-principle calculations and unveiled, for the first time, the details and mechanisms of the phase transition from the rocksalt δ -HfN to the “nitrogen-rich” structure. The experimental measurements and the theoretical calculations match well in good consistence. We thus draw the following conclusions:

- (1) The “nitrogen-rich” phase appearing at $x = \text{N}:\text{Hf} = 4:3$ is of a cubic Th_3P_4 structure with a space group symmetry of $I-43d$ (220) and a lattice parameter of ~ 6.71 Å, namely c -Hf₃N₄.
- (2) The phase transition from the δ -HfN structure at $x \approx 1:1$ to the c -Hf₃N₄ structure at $x \approx 4:3$ undergoes three stages of structural evolution driven by energy minimization, as elucidated by comparison between the enthalpy of formation of the rocksalt phase [$EOF(\delta\text{-HfN})$] and that of the c -Hf₃N₄ phase [$EOF(c\text{-Hf}_3\text{N}_4)$] as follows.
 - (i) In the first stage of $1.039 \leq x \leq 1.165$, $EOF(\delta\text{-HfN}) \ll EOF(c\text{-Hf}_3\text{N}_4)$, the films remain single-phase in δ -HfN structure to keep the total energy of the system the lowest. In this stage, as x increases hafnium vacancies gradually appear in the rocksalt network, but the associated energy change is not enough to trigger phase transition.
 - (ii) In the second stage of $1.195 \leq x \leq 1.278$, $EOF(\delta\text{-HfN}) \approx EOF(c\text{-Hf}_3\text{N}_4)$, the δ -HfN phase and the c -Hf₃N₄ phase coexist in the films because thermodynamically they have similar EOF thus similar stability. In this stage, the phase transition occurs gradually as x increases:

the fraction of δ -HfN phase decreases as that of c -Hf₃N₄ phase gradually becomes dominant.

- (iii) In the third stage of $x = 1.334$, $EOF(\delta\text{-Hf}_3\text{N}_4) \gg EOF(c\text{-Hf}_3\text{N}_4)$, the transition from the δ -HfN phase to the c -Hf₃N₄ phase completes. The film exhibits single-phase c -Hf₃N₄ structure.
- (3) The phase transition from the δ -HfN to the c -Hf₃N₄ structure in the hafnium nitride films transforms the films from conductive and opaque metals to insulating and transparent semiconductors. As they have good mechanical, chemical and oxidation resistance, transparent hafnium nitride films can potentially be used in applications as protective coatings of optical windows in aerospace, thus warrant further investigation.

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