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## Measurement of the picosecond population relaxation time of cresyl violet by time-delayed four-wave mixing with incoherent light

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Measurements of the picosecond population relaxation time of cresyl violet in methanol were performed by phase-conjugation time-delayed four-wave mixing using incoherent light. This time is about 157 ps. The result was verified with the correlation technique of mode-locked picosecond pulses with different intensities.

### 1. Introduction

The time resolution of the measurement of transient processes using coherent light is determined by the pulse duration  $t_p$ . In order to obtain a higher time resolution, much effort has been made to generate picosecond or femtosecond ultrashort light pulses. Very recently, the shortest pulse of 6 fs was obtained by compressing the output of a group-velocity-dispersion-compensated colliding pulse mode-locked laser [1]. However, such ultrashort pulses can be generated only in a very limited wavelength region and the apparatus is complicated.

Based on transient coherent optical effects, a new spectroscopic technique using incoherent light has recently been developed [2,3]. In the transient coherent spectroscopy used for studies of ultrafast dynamics, the signal light generated or modulated by nonlinear optical effects is detected using the cross-correlation between the excitation and the probe light beams. Therefore, in such cases, one expects the time resolution to be determined by the

correlation time  $\tau_c$  instead of the pulse duration  $t_p$  [3]. Based on the uncertainty principle, the correlation time  $\tau_c$  is approximately the inverse bandwidth of the incoherent light  $\tau_c \sim 1/\Delta\nu$  [2,3]. Obviously, the wider the bandwidth,  $\Delta\nu$ , of a non-transform-limited pulse, the smaller is the correlation time  $\tau_c$  and the higher the time resolution which can be obtained.

Since 1984, coherent transient spectroscopy with incoherent light has become a field of particular interest. In this paper we report the population relaxation time,  $T_1$ , of cresyl violet in methanol which was measured by phase-conjugation time-delayed four wave mixing with incoherent light (TDFWM-IL). The measured time is about 157 ps. This result is in good agreement with the values of 162 ps, obtained by pump-probe measurements using coherent picosecond pulses [4], and 160 ps with an optical Kerr shutter technique [5].

### 2. Theory

There are two types of TDFWM-IL, the so-called BOXCARS and phase-conjugation techniques for measurement of the population relaxation time as depicted in fig. 1. In the former

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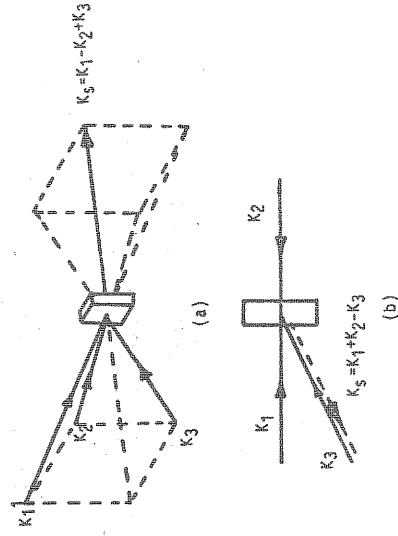


Fig. 1. Schematic of (a) BOXCARS type (b) phase-conjugation type TDFWM-IL experiments for measurement of population relaxation.

type the pump beams  $K_1$  and  $K_2$  and the probe beam  $K_3$  are noncoplanar [6]. In the latter case the three beams are coplanar. Our experiment was performed in the later configuration. The pump beams  $K_1$  and  $K_3$  intersect at an angle of about  $2^\circ$  and the delay time between them was  $-\tau$  i.e. the  $K_3$  beam reached the sample before the  $K_1$  beam. The pump beam  $K_1$  and the probe beam  $K_2$  were counterpropagating and the delay time between them was  $T \rightarrow 0$ . The pump beam  $K_3$  and the signal beam  $K_2$  are phase-conjugated with each other [6]. The three beams of this incoherent light field were applied to the resonant nonlinear material in a sequence of time represented in fig. 2. The medium contains a two-level system. The total electric field of the input beams is given by

$$E(t) = E(t) \exp[-i(\omega t - K_1 r)] + E(t - T) \exp\{-i[\omega(t - T) - K_2 r]\} + E(t + \tau) \exp\{-i[\omega(t + \tau) - K_3 r]\}. \quad (1)$$

The notation  $E(t)$  represents the envelope function of the electric field slowly varying compared with the optical frequency. The random variations of the amplitude and phase are included in  $E(t)$ . To derive the dependence of the signal intensity on the delay time  $-\tau$  between  $K_3$  and  $K_1$ , we consider that the  $K_2$  beam was scattered by the grating formed by  $K_1$  (at  $t_2$ ) and  $K_3$  (at  $t_1$ ) shown in fig. 2(a). Similarly,  $K_1$  was scattered by the grating formed by

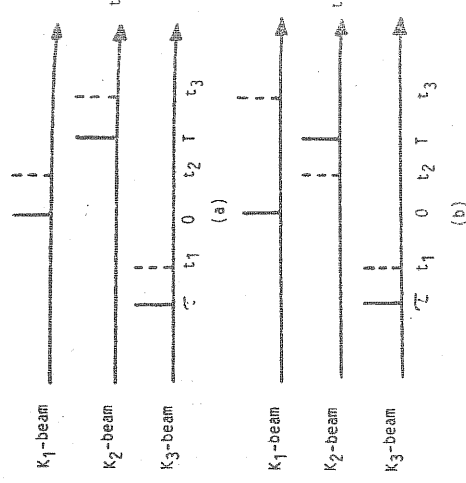


Fig. 2. Time sequence of the pulses, (a) the  $K_2$  beam is scattered by the grating formed by the  $(K_1, K_3)$  interference. (b) The  $K_1$  beam is scattered by the grating formed by the  $(K_2, K_3)$  interference.

$K_2$  (at  $t_2$ ) and  $K_3$  (at  $t_1$ ) in fig. 2(b). The third-order nonlinear polarization in the direction  $K_3$  is obtained as

$$P^{(3)}(t, \tau, \omega) = \chi^{(3)} \int d\Delta g(\Delta) \int df_3 \int dt_2 \int dt_1 \times \exp[-(t - t_3 + t_2 - t_1)/T_2 - (t_3 - t_2)/T_1] \times \{ [E^*(t_1 + \tau)E(t_2)E(t_3 - T) + E^*(t_1 + \tau) \times E(t_2 - T)E(t_3)] \exp[-i\Delta(t - t_3 - t_2 + t_1)] + [E(t_1)E^*(t_2 + \tau)E(t_3 - T) + E(t_1 - T) \times E^*(t_2 + \tau)E(t_3)] \exp[-i\Delta(t - t_3 + t_2 - t_1)] \}, \quad (2)$$

where  $g(\Delta)$  is the distribution function of the frequency difference  $\Delta = \omega - \omega_0$  between the transition frequency of the material  $\omega_0$  and the laser frequency  $\omega$  and  $T_2$  is the dephasing time. The signal intensity as a function of  $\tau$  is represented by

$$I(\tau) \propto \langle |P^{(3)}(t, \tau, \omega)|^2 \rangle. \quad (3)$$

The scattering efficiency of  $K_2$  by the grating formed by the  $(K_1, K_3)$  interference is much higher than that of  $K_1$  by the grating formed by the

$(K_2, K_3)$  interferences. Therefore  $E(t_2 - T)E(t_3)$  be omitted. For  $T_2$  is much  $\exp[-(t - t_3 - t_2 - t_1)/T_2]$

$$\exp[-(t - t_3 - t_2 - t_1)/T_2] \delta(t - t_3 - t_2 - t_1)$$

For  $\tau > 0$ , an incoherent and in

$$I(\tau) \propto 1 + 1.6 + 2.9(\tau/T_2)^2$$

Equation (5) contains a constant background "spike" because of the information

### 3. Experiment

The experiment is performed by the incoherent light pumped by the

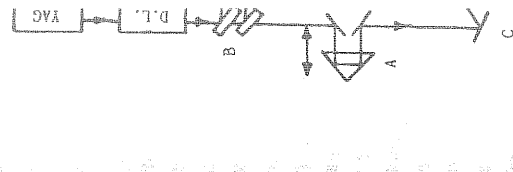
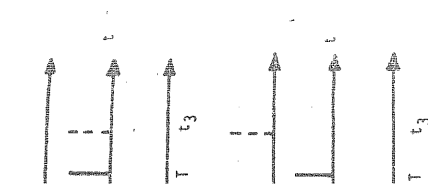


Fig. 3. TDFWM-IL B-beam setup.



(a)  $K_2$  beam is scattered interference. (b) The third-order direction  $K_3$  is formed by the  $(K_2, K_3)$

(c) The third-order direction  $K_3$  is formed by the  $(K_2, K_3)$

$$\int dt_2 \int dt_1 \{ - (t_3 - t_2)/T_1 \} + E^*(t_1 + \tau) - t_3 - t_2 + t_1 \} + E(t_1 - T) - t_3 + t_2 - t_1 \} \} \quad (2)$$

tion of the frequency between the transverse  $\omega_0$  and the laser dephasing time. The is represented by

$$\text{by the grating } K_3 \text{ is much higher } K_3 \text{ formed by the}$$

( $K_2, K_3$ ) interference due to mixing frequency processes. Therefore, the terms containing  $E^*(t_1 + \tau)E(t_2 - T)E(t_3)$  and  $E(t_1 - T)E^*(t_2 + \tau)E(t_3)$  can be omitted. For the case where the dephasing time  $T_2$  is much shorter than  $\tau_c$  and  $T_1$ , the term  $\exp[-(t - t_3 + t_2 - t_1)/T_2]$  is nonzero only for  $(t - t_3 + t_2 - t_1) \rightarrow 0$ ; thus

$$\exp[-(t - t_3 + t_2 - t_1)/T_2] \rightarrow T_2^2 \delta(t - t_3) \delta(t_2 - t_1) \quad (4)$$

For  $\tau > 0$ , and, eq. (3) is the cases of both homogeneous and inhomogeneous broadening [6],

$$I(\tau) \propto 1 + 1.6(T_1/\Delta\tau) \exp[-2(\tau/\Delta\tau)^2] + 2.9(\Delta\tau/T_1) \exp[-(2/T_1)\tau] \quad (5)$$

Equation (5) consists of three terms, the first one is a constant background term, the second is a coherence "spike" term, and the last "tail" term contains the information about  $T_1$ .

3. Experimental

The experimental setup is shown in fig. 3. As an incoherent light source we used a pulsed dye laser pumped by the second harmonic of a Q-switched

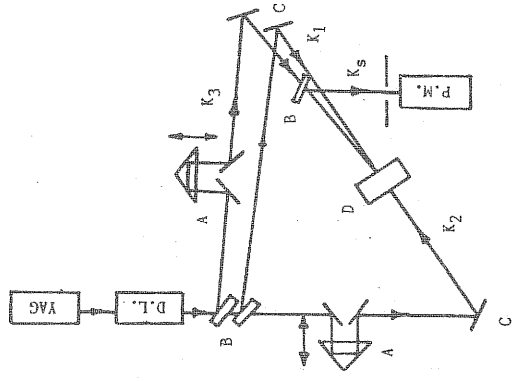


Fig. 3. TDFWM-IL experimental setup. A - variable delay; B - beam splitter; C - mirror; and D - sample.

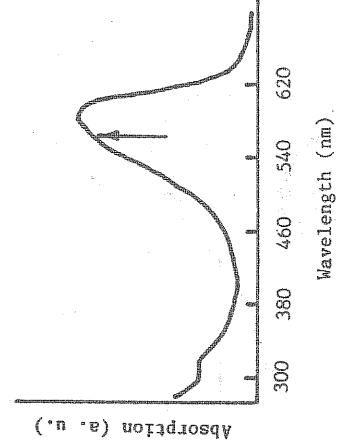


Fig. 4. Absorption spectrum of cresyl violet in methanol. The arrow indicates the excitation wavelength used.

Nd:YAG laser with a repetition rate 20 Hz. The output pulse of the dye laser was 7 ns wide and was tuned to 560 nm. This excitation wavelength is indicated by an arrow in the absorption spectrum of cresyl violet in methanol, (see fig. 4). The bandwidth (FWHM) of the power spectrum was about  $0.63 \text{ cm}^{-1}$ , corresponding to a correlation time  $\tau_c \approx 53 \text{ ps}$ . As a resonant material we chose cresyl violet in methanol because this kind of organic dye solution is known to have an appropriate population relaxation time to demonstrate the applicability of the present method and to satisfy the condition  $T_2$  (for cresyl violet in cellulose  $T_2 \approx 100 \text{ fs}$  [7])  $\ll \tau_c$ . The sample was  $5 \times 10^{-4} \text{ M}$  in concentration and 1.5 mm thick.

4. Results and discussion

The measured traces using phase-conjugation TDFWM-IL of cresyl violet are shown in fig. 5. They represent the signal intensities of the mixing frequency as a function of the delay time  $-\tau$  between  $K_3$  and  $K_1$  under various average power densities of the excitation field. Incoherent light can be regarded as a train of incoherently phased ultra-short spike pulses. Although the phase of each spike pulse is random, each correlated spike pulse pair having wave vector  $K_3$  and  $K_1$  has the same relative phase and therefore contributes coherently to forming the population grating. The probe beam  $K_2$  was scattered by the population grating resulting in a signal propagating in the direction  $K_s = K_1 + K_2 - K_3$ . Because of the phase "memory" of

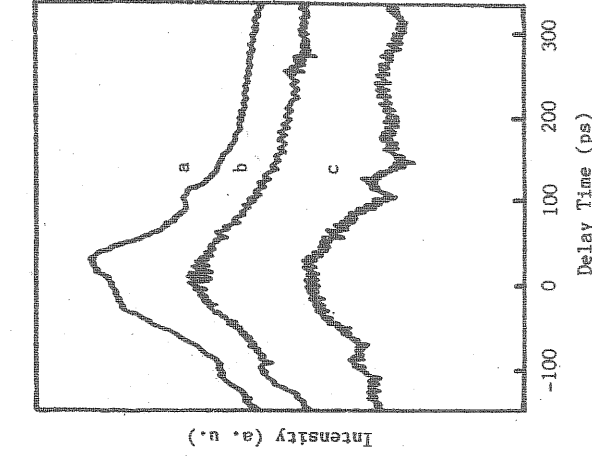


Fig. 5. Experimental traces of the signal intensity of TDFWM-IL vs. delay time  $-\tau$  of  $K_2$  to  $K_1$  beam. Various average power densities of the excitation field of (a) 32, (b) 16 and (c) 9 W/cm<sup>2</sup> were used.

the medium, and the fact that the three beams reached the sample at different times, the TDFWM-IL signal can be obtained, only for  $T \ll \tau_c$  and  $T_2 \ll \tau_c \ll T_1$ .

The experimental data in figs. 5(a)–(c) were obtained using average power densities of 32, 16 and 9 W/cm<sup>2</sup>, respectively. The data were fitted by the curve (b) calculated with eq. (5) (see fig. 6). The population relaxation time obtained was  $T_1 = 157$  ps using  $\Delta\tau = 28$  ps in eq. (5). This result is in good agreement with the results reported in refs. [4,5]. The  $b_1$ ,  $b_2$  and  $b_3$  curves corresponded to the first, second and third terms in eq. (5), respectively, and  $b = b_1 + b_2 + b_3$ . The  $b_1$  curve gives a constant background, the  $b_2$  curve describes a coherent spike and the  $b_3$  curve contains the information about  $T_1$  and decays with  $T_1/2$ .

It was shown in fig. 5 that the peaks of the experimental curves split with an increase in the power density. We suggest that these two peaks corresponded to the two cases shown in figs. 2(a) and (b). The nature of the phenomenon will be investigated in detail. Moreover, the signal-to-noise

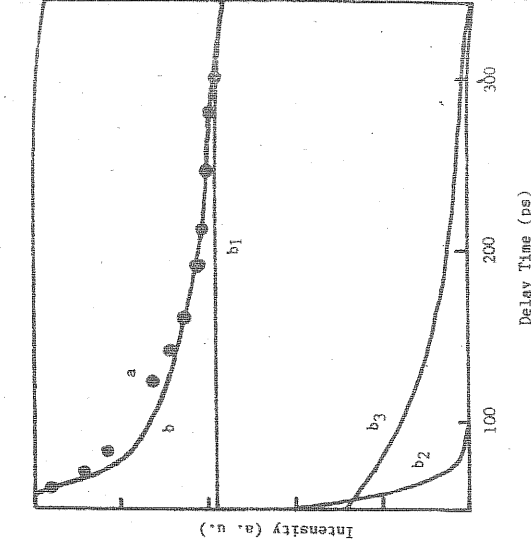


Fig. 6. (a) Experimental data; (b) fit to the curve a calculated with eq. (5);  $b_1$ ,  $b_2$  and  $b_3$  represent the three terms in eq. (5), with  $b = b_1 + b_2 + b_3$ .

ratios for the "tail" of the experimental curves in fig. 5 are increased with enhancing the power densities of the light field. It is easy to understand that an increase in the power density of the field enhanced the nonlinear effects of the interaction between the medium and the light field. The signal-to-noise ratio of TDFWM-IL, therefore, was enhanced.

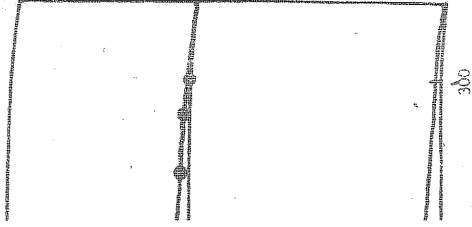
In conclusion, it should be said that this configuration avoided the inconvenience in adjusting the optical paths in the BOXCARS type TDFWM-IL in which three beams are noncoplanar. This technique is also better than the pump-probe scheme, because in the latter the probe light is directly incident on the detector and intensity fluctuations of the probe beam often obscures the signal. In the TDFWM-IL scheme, on the other hand, the signal itself is measured easily because the signal can be generated in a different direction from any incident light beam. This is one of the reasons why a better signal-to-noise ratio can be obtained. Due to the advantages stated above, we believe that the TDFWM-IL technique will be widely applied to ultrahigh time resolution spectroscopy.

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