

## USING DISPERSION THEORY TO INTERPRET THE POLARIZATION PROPERTIES OF THE BAND-EDGE EMISSION IN GaN CRYSTALS

Bao Qingcheng, Zhang Fengling,\* Li Duolu, Dai Rensong† and Xu Xurong

Changchun Institute of Physics, Chinese Academy of Sciences, Changchun, China

(Received 30 August 1986 by W.Y. Kuan)

In this paper, we report the polarization properties of the near band-edge emission in GaN crystal wafers. When excitation intensity increases in the range of 0–0.1 MW cm<sup>-2</sup>, the polarization of band-edge emissions increase quadratically, then, a saturation appears.

These phenomena can be explained by the dispersion theory of exciton–exciton interaction.

### 1. INTRODUCTION

IT IS WELL-KNOWN that, uniaxial crystal GaN is a direct gap semiconductor, a large amount of works on this promising material for luminescence and laser devices are aiming at the near band-edge emission [1–3].

In our previous papers [4, 5], we proposed the dispersion concept of exciton–exciton interaction. According to dispersion theory, in uniaxial crystal, the dispersion effect between bound excitons is unisotropic, the *C*-axis is the preferential direction. This property should make the luminescence polarization of bound excitons increase with the excitation intensity quadratically.

In this paper, the luminescence polarization properties of bound excitons (*I*<sub>1</sub> and *I*<sub>3</sub> lines) in uniaxial crystal GaN were studied carefully at the temperature of 77 K. In the excitation range of 0–0.1 MW/cm<sup>-2</sup>, we found that, the polarization of band-edge emission *I*<sub>1</sub> and *I*<sub>3</sub> increased with *I*<sub>ex</sub> quadratically at first, and then, a saturation appeared. These experiment facts support the dispersion theory of exciton–exciton interaction.

### 2. SAMPLES AND EXPERIMENTAL SET-UP

Samples used in the experiment were GaN single crystal wafers, which were grown by the vapour phase epitaxy method on sapphire substrates oriented in (0001) direction [6]. There were two kinds of samples, one of them was unintentionally doped GaN crystal wafers, typical sample was labelled by GaN–15 #, another was Zinc-doped GaN crystal wafers, typical was labelled by GaN–16 #. The thickness of GaN crystal

wafers was about 8 μm, the electron concentration of unintentionally doped GaN crystal wafers was about 10<sup>18</sup> cm<sup>-3</sup> at room temperature determined by Hall measurement.

Experimental work was finished on HEPLSM (high excitation photoluminescence spectrum measurement) system of Transient Solid Spectrum Laboratory, Changchun Institute of Physics, C.A.S.

Samples were held in the cryostat ESR–900 and excited by a light beam, whose wavelength of 308 nm comes from an excimer laser EMG–102, with a set of neutral attenuators, *I*<sub>ex</sub> can be varied in the range of 0–100 MW cm<sup>-2</sup> easily. A polarizer was put in before a grating double monochromator to pick out the luminescence intensity polarized in parallel or perpendicular to *C*-axis of GaN crystals respectively. After the monochromator, there was a photomultiplier C–31034 with semiconductor cooling system to measure luminescence signal, and then, recorded by *X*–*Y* recorder.

### 3. EXPERIMENT RESULTS

#### 3.1. Emission spectra

The near band-edge emission spectra of GaN crystal wafers under proper excitation intensity *I*<sub>ex</sub> were shown in Figs. 1 and 2.

There were three emission peaks that could be distinguished apparently in Fig. 1 and 2, which were situated at 3.466, 3.353, and 3.313 eV respectively. Compare GaN–15 # and GaN–16 #, one can see that, as a result of Zn-doping, the intensity of 3.466 eV line decreased and the other two lines (3.353 and 3.313 eV) increased. When *I*<sub>ex</sub> increased, we found that, the peak wavelength of 3.313 eV line shifted to violet side. Combining these points with the temperature effects, we labelled these three peaks as *I*<sub>1</sub>, *I*<sub>3</sub> and *I*<sub>4</sub>

\*Present address: The Physics – Mathematics Department, Jiaotong University, Beijing, China.

†Present address: Hushu Nan Rode 186, Hangzhou, China.

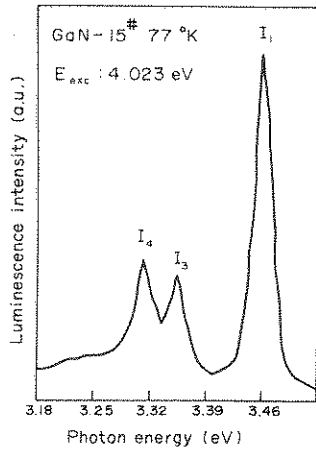


Fig. 1. The emission spectrum of GaN-15#.

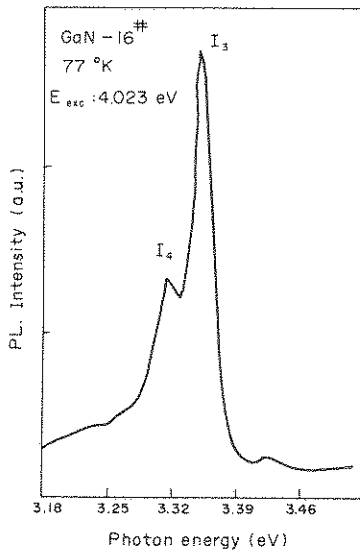


Fig. 2. The emission spectrum of GaN-16#.

line respectively, see [3]. In [3],  $I_1$  line was due to neutral donor center bound excitons ( $BED^\circ$ ),  $I_4$  was due to  $D-A$  pairs,  $I_3$  was due to neutral acceptor center bound excitons ( $BEA^\circ$ ). (Whether  $I_3$  is due to the recombination of  $BEA^\circ$ 's or isoelectron center bound excitons, need to be identified further, but this does not affect the basic idea of the paper).

3.2. Experiment results of luminescence polarization

At first, we define the luminescence polarization  $P$  as follows:

$$P = I_{\parallel} / I_{\perp} \tag{1}$$

where,  $I_{\parallel}$  and  $I_{\perp}$  are the luminescence intensity parallel and perpendicular to  $C$ -axis of GaN crystal wafers respectively, see Fig. 3.

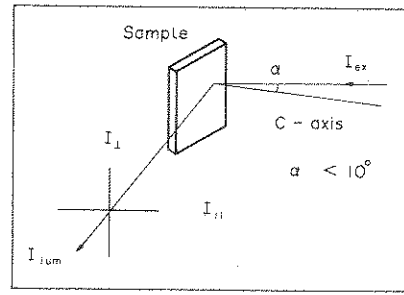


Fig. 3. The optical scattering plane of the experiment.

In experiments, we found that  $P$  has different values under different  $I_{ex}$  see Figs. 4 and 5.

From Figs. 4 and 5, some important points can be figured as follows:

(1) The near band-edge emission of GaN crystal wafers show polarization character, the preferential direction is  $C$ -axis.

(2)  $P$  values of  $I_1$  and  $I_3$  lines increase along with  $I_{ex}$  during the excitation range of 0-0.1  $MW\ cm^{-2}$ .

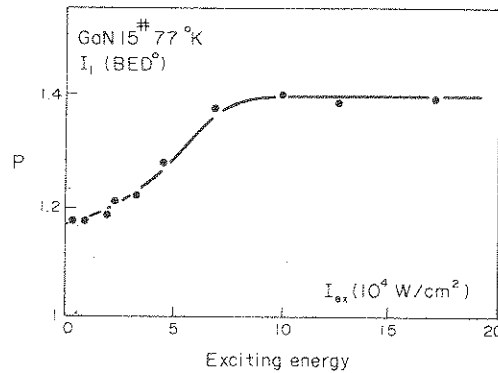


Fig. 4.  $P$  values of  $I_1$  line under various  $I_{ex}$ 's.

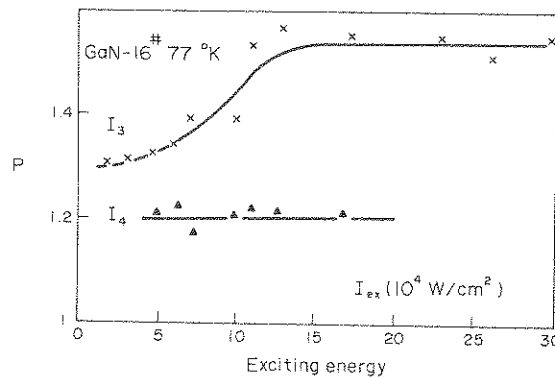


Fig. 5.  $P$  values of  $I_3$  under various  $I_{ex}$ 's.

(3) Wh  
escence pol  
phenomena

(4)  $P$  vs

4. AF

4.1. Dispers

The e  
associated  
dipole-dipo  
Waals Forc  
force. Whe  
transient d  
persion ef  
We only c  
and [5].

For e  
spherical-li  
to study  
interaction  
 $r_1$  and  $r_2$ ,  
induce a  
polarize  $p_2$   
 $p_1$  with mo

The in  
both  $p_1$  a  
detailed cal

$M = (2)^{1/2}$   
where,  $\epsilon$   
crystal,  $hw$   
for the n  
excitons (  
other kind

$R = r_2 -$

As we  
anisotropic  
as an uniso

$a = \epsilon_{\parallel} / \epsilon_{\perp}$   
where,  $\epsilon$   
crystal,  $||$   
and perper

If one  
valence ba  
be larger th

The  
electric di  
 $p$  not spher  
ponent of

$p_{\parallel} = aP_{\perp}$

(3) When  $I_{ex}$  is about  $0.1 \text{ MW cm}^{-2}$ , the luminescence polarizations of  $I_1$  and  $I_3$  lines show saturation phenomena.

(4)  $P$  value of  $I_4$  line do not change with  $I_{ex}$ .

#### 4. ANALYSIS OF EXPERIMENT RESULT

##### 4.1. Dispersion theory

The exciton has a polarization  $\mathbf{p} \cdot \exp(i\mathbf{K} \cdot \mathbf{R})$  associated with it. Like in neutral atom, the transient dipole-dipole interaction resulting in the Van der Waals Force which was known as Loudon dispersion force. When two excitons approach each other, the transient dipole-dipole interaction resulting the dispersion effect of exciton-exciton interaction also. We only cite some main ideas and formula from [4] and [5].

For example, we consider  $BED^0$  case,  $\mathbf{p}$  shows spherical-like distribution, hence  $BED^0$  is a good sample to study the dispersion effect of exciton-exciton interaction. Suppose there are two  $BED^0$ 's localized at  $\mathbf{r}_1$  and  $\mathbf{r}_2$ , labelled by  $\mathbf{p}_1$  and  $\mathbf{p}_2$  respectively,  $\mathbf{p}_1$  will induce a transient electrical field at  $\mathbf{r}_2$ , which will polarize  $\mathbf{p}_2$  or make  $\mathbf{p}_2$  larger, enlarged  $\mathbf{p}_2$  will repolarize  $\mathbf{p}_1$  with more power.

The interaction is supposed fast enough and then, both  $\mathbf{p}_1$  and  $\mathbf{p}_2$  get an increased quantity  $M$ . The detailed calculation shows that:

$$M = (2)^{1/2} |\mathbf{p}|^3 / 3\epsilon R^3 \hbar \omega_0, \quad (2)$$

where,  $\epsilon$  stands for the dielectrical function of GaN crystal,  $\hbar \omega_0$  stands for the energy of  $BED^0$ ,  $R$  stands for the nearest distance between  $BED^0$  and other excitons (including free exciton,  $BED^0$ ,  $BEA^0$ , or other kind of bound excitons):

$$\mathbf{R} = \mathbf{r}_2 - \mathbf{r}_1.$$

As we know, GaN is an uniaxial crystal, it has an unisotropic crystal field. We define a parameter "a" as an unisotropic parameter:

$$a = \epsilon_{\parallel} / \epsilon_{\perp} > 1, \quad (3)$$

where,  $\epsilon$  stands for the dielectric function of GaN crystal, " $\parallel$ " and " $\perp$ " stand for the direction parallel and perpendicular to  $C$ -axis.

If one allows for the unisotropic structive effects of valence band in uniaxial crystals, the value of "a" would be larger than the value calculated by formulae (3).

The unisotropic crystal field should affect the electric distribution, make the transient dipole moment  $\mathbf{p}$  not spherical but elliptical, that is, the parallel component of  $\mathbf{p}$  would be larger than the perpendicular one:

$$p_{\parallel} = aP_{\perp} > p_{\perp}. \quad (4)$$

According to formula (2), (3) and (4), one can deduce a relation:

$$M_{\parallel} = a^4 M_{\perp} > M_{\perp}, \quad (5)$$

where,  $M_{\parallel}$  and  $M_{\perp}$  stand for the induced transient dipole moment parallel and perpendicular to  $C$ -axis, respectively.

Formulae (5) show that, in uniaxial crystal, such as GaN, the dispersion effect has the unisotropic character.

Allowing for Fermi relation between dipole moment and luminescence intensity, from formulae (1), can get the following relation:

$$P = I_{\parallel} / I_{\perp} = (P_{\parallel} + M_{\parallel})^2 / (P_{\perp} + M_{\perp})^2, \quad (6)$$

where,  $I_{\parallel}$  and  $I_{\perp}$  are the luminescence intensities parallel and perpendicular to  $C$ -axis.

Approximately, consider the optical absorbtion process as a single molecular approach, write down the relation between  $I_{ex}$  and the density  $N$  of  $BED^0$ , and the relation between  $N$  and the nearest distance  $R$ :

$$I_{ex} \cdot f / \hbar \omega \cdot De f = N / \tau, \quad (7)$$

$$R^{-3} = 4\pi N / 3, \quad (8)$$

where  $f$ : the oscillator strength of  $BED$ ,  $\tau$ : the lifetime of  $BED^0$ ,  $De f$ : the effective absorbtion depth of GaN crystal wafers,  $\hbar \omega$ : exciting photon energy.

From formula (3), (6), (7) and (8), one can get a relation:

$$P = (A + B \cdot I_{ex})^2, \quad (9)$$

where,  $A$ : a constant relevant to the initial polarization of  $BED^0$ ,  $B$ : a constant relevant to the dispersion effect of  $BED^0$  by another  $BED^0$  or other excitons.

Detailed deducement shows that:

$$A = a, \quad (10)$$

$$B = 4\pi \cdot a \cdot f \cdot \tau \cdot |\mathbf{p}|^2 / 9\epsilon \hbar \omega_0 \cdot \hbar \omega \cdot De f. \quad (11)$$

Take  $BED^0$  as a sample in GaN crystal, unisotropic parameter  $a \approx 1$ , oscillator strength  $f \approx 1$ , lifetime  $\tau \approx 10^{-9}$  second, transient dipole moment  $|\mathbf{p}| \approx 17 \text{ e}\text{\AA}$  (the radius of exciton in GaN is about  $17 \text{ \AA}$ ), dielectric costands  $\epsilon \approx 6\epsilon_0$ , the energy of  $BED^0$   $\hbar \omega_0 \approx 3.400 \text{ eV}$ , exciting photon energy  $\hbar \omega \approx 4.023 \text{ eV}$ , the effective absorbtion depth  $De f \approx 1 \mu\text{m}$ , one can calculate the values of  $A$  and  $B$ :

$$A \approx 1 \quad (12)$$

$$B = 10^{-6} (\text{cm}^2 \text{ W}^{-1}) \quad (13)$$

##### 4.2 Experiment result analysis

Figures 5 and 6 show the relation between  $(P)^{1/2}$  and  $I_{ex}$ 's.

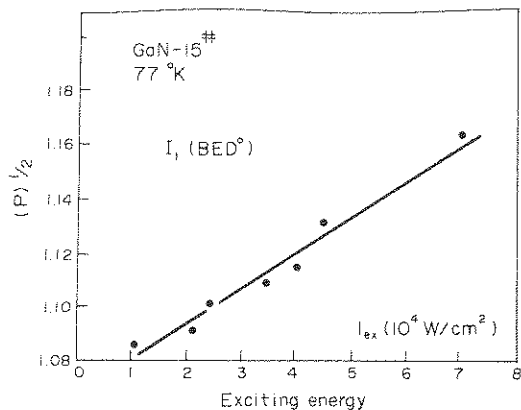


Fig. 6.  $(P)^{1/2} - I_{\text{ex}}$  relation of  $I_1$  line.

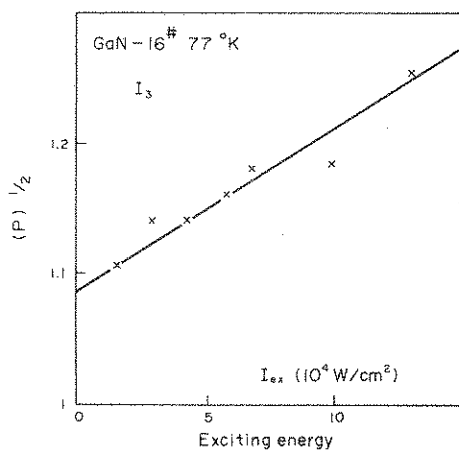


Fig. 7.  $(P)^{1/2} - I_{\text{ex}}$  relation of  $I_3$  line.

From Fig. 6 one can know that, for  $I_1$  line,  $A \approx 1.07$ ,  $B \approx 1.30 \cdot 10^{-6} \text{ (cm}^2 \text{ W}^{-1})$ . From Fig. 7 one can know that for line  $I_3$ ,  $A \approx 1.09$ ,  $B \approx 1.20 \cdot 10^{-6} \text{ (cm}^2 \text{ W}^{-1})$ . All of the experimental values can suit well the theoretical calculating values.

When  $I_{\text{ex}}$  is over about  $0.1 \text{ MW cm}^{-2}$ , the free exciton density will be about  $10^{18} \text{ cm}^{-3}$ , various kinds of bound centers are occupied by excitons or in another words, the bound excitons are saturated. After that,

when  $I_{\text{ex}}$  increases further, the distance of the nearest neighbors does not apparently shorten. This is the reason of the saturation phenomena in luminescence polarization of  $I_1$  and  $I_3$  lines appeared in Figs. 4 and 5.

Since  $I_4$  line is not relevant to excitons, the dispersion concept does not suit it, and it just shows the initial polarization property caused by the uniaxial crystal field (both the dielectric function and the band structure effects) of GaN crystal wafers.

## 5. CONCLUSIONS

From the above analyses, one can make some conclusions as follows:

The near band-edge emissions of uniaxial crystal GaN including  $I_1$ ,  $I_3$  and  $I_4$  show initial polarization properties,  $C$ -axis is the preferential direction.

The luminescence polarizations of emission lines relevant to bound excitons increase quadratically with  $I_{\text{ex}}$  in the excitation range of  $0-0.1 \text{ MW cm}^{-2}$ . Meanwhile, polarization of  $I_4$  line does not change with  $I_{\text{ex}}$ . These experimental results give support to the dispersion theory of exciton-exciton interaction strongly.

Because the density of bound excitons is limited by the bound centers, when  $I_{\text{ex}}$  is about  $0.1 \text{ MW cm}^{-2}$ , the saturation phenomena of luminescence polarization of bound excitons appeared.

## REFERENCES

1. R. Dingle, D.D. Sell, S.E. Stokowski & M. Ilegems, *Phys Rev B* **44**, 1211 (1971).
2. J.I. Pankove, L.E. Berkeyheiser, H.P. Maruska & J. Wittke, *Solid State Commun.* **8**, 1051 (1970).
3. R. Dai, S. Fu, J. Xie, G. Hu, H. Schrey & C. Klingshirn, *J. Phys C* **15**, 393 (1982).
4. Q. Bao, R. Dai & X. Xu, *J. Phys, Colloque C 7-221*, supplement au n° 10 Tome 46, October (1985).
5. Q. Bao, R. Dai & X. Xu, *The dispersion between bound excitons in uniaxial crystals*, abstract see *The Fifth Chinese Conference on Semiconductor Physics*, p. 230, published in China, 3-6 December, (1985).
6. H.P. Maruska & J.J. Thietjen, *Appl. Phys. Lett.* **15**, 327, (1969).

SINCE TH  
small norm  
magnetocor  
from the po  
ation of the  
are now ob  
narrow cha  
[6, 7], the  
inelastic sc  
in small sy  
the recen  
techniques.

The ef  
ference du  
disordered.  
In the sma  
interferenc  
the conduc  
the magnit  
universal c  
degree of  
temperatur  
coherence  
ture, the ir  
various ph  
scattering,