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# Photon cascade luminescence in CaAl<sub>12</sub>O<sub>19</sub>:Pr, Cr

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#### Abstract

In this report, the  $Cr^{3+}$  ion was chosen as a co-dopant to modify the unpractical photon cascade emission properties of  $Pr^{3+}$ -doped  $CaAl_{12}O_{19}$  phosphors, which emit one near-UV photon from the  ${}^{1}S_{0}$  state followed by visible photons from the  ${}^{3}P_{0}$  state, into phosphors that emits two visible photons through energy transfer. The photon cascade emission process via energy transfer and the transfer mechanisms were systemically investigated by luminescence spectra and dynamics using synchrotron radiation as one of the excitation sources. The internal visible quantum efficiency of  $CaAl_{12}O_{19}$ :Pr, Cr was estimated and compared with  $CaAl_{12}O_{19}$ :Pr and the drawback to obtain the visible quantum efficiency higher than unit for  $CaAl_{12}O_{19}$ :Pr, Cr as a practical VUV phosphor was also discussed.  $\bigcirc$  2007 Elsevier Inc. All rights reserved.

Keywords: Photon cascade luminescence; Synchrotron radiation; Energy transfer

# 1. Introduction

The development of plasma display panels and mercuryfree fluorescent lamps in recent years made new demands for the efficient VUV-excited phosphors [1]. In these applications, the high energy of the VUV photons produced by the rare gas discharge make it possible to achieve two visible photon emissions for one VUV photon absorbed, namely a phosphor quantum efficiency (QE) higher than unit [2]. The successive emission of two photons, so-called photon cascade emission (PCE), was observed in  $Pr^{3+}$ -doped materials when the energy level of  ${}^{1}S_{0}$  ( $4f^{2}$ ) is located below the lowest 4f5d energy level [3–5]. Incident VUV photons are absorbed by  $Pr^{3+}$  from its ground state ( ${}^{3}H_{4}$ ) into the 4f5d configuration. After relaxation, the excitation decays to the  ${}^{1}S_{0}$  state. Then  ${}^{1}S_{0}$  is depopulated through a two-step cascade emission, involving transitions  ${}^{1}S_{0}-{}^{1}I_{6}$  (around 402 nm) followed by  ${}^{3}P_{0}-{}^{3}F_{J}$ ,  ${}^{3}H_{J}$  (480–700 nm). Thus a system with internal QE greater than unit can be achieved. But this two-photon luminescence is not monochromatic and the first step transition,  ${}^{1}S_{0}-{}^{1}I_{6}$ , is near the UV range, not suitable for practical application. Therefore, an appropriate co-dopant that can modify the unpractical PCE properties by converting the first step photon into proper visible photon through energy transfer (ET) could be a solution for this situation [6–11].

Oxide materials are usually better choices than fluoride materials for VUV phosphor because of its relatively easier preparation method and higher VUV absorption efficiency although most of the  $Pr^{3+}$ -based PCE hosts are fluorides [3,12].  $Pr^{3+}$ -based PCE in oxides was discovered several years ago in  $Pr^{3+}$ -doped  $SrAl_{12}O_{19}$  [13],  $LaMgB_5O_{10}$  [14], and  $LaB_3O_6$  [15], etc. In this present work,  $CaAl_{12}O_{19}$  (CAO) was selected as a host to incorporate  $Pr^{3+}$  and  $Cr^{3+}$  to investigate the possibility of using  $Cr^{3+}$  co-doping to modify the PCE properties of  $Pr^{3+}$ . CAO is also a host in

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which the lowest 4f5d level of  $Pr^{3+}$  is located above its  ${}^{1}S_{0}$  ( $4f^{2}$ ) level. The trivalent chromium,  $Cr^{3+}$ , is a promising candidate for this kind of co-dopant because  $Cr^{3+}$  has abundant energy levels in the range from UV to visible, and  $Cr^{3+}$  itself has efficient red emission in CAO host.

# 2. Experimental section

# 2.1. Sample preparation

Microcrystalline CAO:Pr, CAO:Cr and CAO:Pr, Cr phosphors were synthesized by high-temperature solidstate reaction method using CaCO<sub>3</sub> (99.99%),  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> (99.999%), Pr<sub>6</sub>O<sub>11</sub> (99.99%), MgO (99.999%) and Cr<sub>2</sub>O<sub>3</sub> (99.99%) (all from Beijing Fine Chemical Company) as raw materials. The choice of this type of Al<sub>2</sub>O<sub>3</sub> powder as a starting material is based on its high reactivity [16]. Powders of the raw materials were dried at 200 °C for 12 h in air to remove any water. Stoichiometric amounts of the starting materials above were weighed and then wetmixed in 2-propyl alcohol (>97%) for 5h in an agate container with agate balls on a planetary mill. After mixing, the 2-propyl alcohol was evaporated. The powder was dried in a stove for 1 day at 200 °C, and a small amount of H<sub>3</sub>BO<sub>3</sub> as a flux was added and then it was subsequently ground for 1h in an agate mortar. The powder was fired in a molybdenum crucible under CO reducing atmosphere, which was formed by activated carbon at high temperature. Reactions were performed in a vertical high-temperature tube furnace at 1550 °C for 10 h, and then quenched to room temperature. The final processes of grinding and firing were repeated two times. The heating rates of  $5 \,^{\circ}C/min$  were used.

The  $Pr^{3+}$  concentration of 1% (in mol) along with  $Cr^{3+}$  concentrations of 1%, 2%, 3%, 4%, 5%, 6%, 7% and 10% and the  $Cr^{3+}$  concentration of 1% along with  $Pr^{3+}$  concentrations of 1%, 3% and 5% were used in the preparation process. When  $Pr^{3+}$  is doped, equivalent amounts of Mg<sup>2+</sup> were co-doped, substituting for Al<sup>3+</sup> for charge compensation [17].

# 2.2. Characterizations

All the measurements were performed at room temperature. The powder diffraction data were obtained by X-ray diffraction (XRD) using a Cu target radiation resource ( $\lambda = 1.54078$  Å). The VUV excitation spectra in the region of 130–330 nm were measured at the VUV station of the BS-U10B beam-line in National Synchrotron Radiation Laboratory, Hefei, China. The typical spectral resolutions of the primary monochromator (1 m Seya-Namioka) and the secondary monochromator (Spectrapro-275) are 0.4 and 2 nm, respectively. The pressure in the vacuum chamber during the measurements was  $1 \times 10^{-4}$  Pa. The excitation and emission spectra were detected by a Hamamatsu H5920-01 photomultiplier. The excitation spectra were corrected for the photoflux of the excitation beam using the excitation spectrum of sodium salicylate as standard. Fluorescence and excitation spectra in the UV region were obtained by Hitachi F-4500 Fluorescence Spectrophotometer, which equipped with a continuous 150-W Xe-arc lamp. For comparison of different samples, the spectra were measured with the same instrument parameters (2.5 nm for the excitation slit, 2.5 nm for the emission slit and 700 V for the PMT voltage). The emission spectra have been corrected for the response of the detector. The fluorescence dynamics of  $Pr^{3+}$  and  $Cr^{3+}$  were detected with a Tektronix digital oscilloscope model TDS 3052. An optical parametric oscillator was used as the excitation source. It has a line width of  $0.2 \text{ cm}^{-1}$ , pulse duration of 10 ns and repetition frequency of 10 Hz.

# 3. Results and discussion

#### 3.1. Crystal structure

CAO adopts a hexagonal magnetoplumbite structure, crystallizing in space group  $P6_3/mmc$  [18]. The XRD patterns of the host CAO (a) as well as CAO:Pr (b) and CAO:Cr (c) samples, both with high dopant concentration, are shown in Fig. 1. The *d*-spacing (*d*, crystal plane spacing) of some peaks is presented. First, they are all in good agreement with JCPDS No. 84-1613, and no additional phase is observed. Second, relative to the host

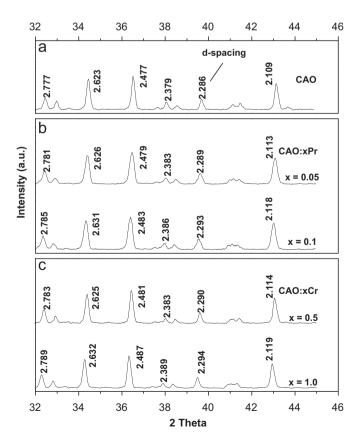


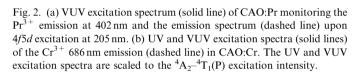
Fig. 1. XRD patterns of CAO (a), CAO:Pr (b) and CAO:Cr (c). The *d*-spacing of some peaks is given in this figure.

CAO, the *d* of each peak increases with increasing  $Pr^{3+}$ and  $Cr^{3+}$  concentrations. According to Bragg's Law,  $n\lambda = 2d \sin \theta$ , the increase of *d* results from the fact that the ion size of doped ions is larger than the replaced ions in a crystal. For CAO:Pr, the ion sizes of  $Pr^{3+}$  (~126.6 pm; all radii taken from Ref. [19]) and Ca<sup>2+</sup> ions (~126 pm) are about equal. Thus, the increase of *d* may result from the codoped big Mg<sup>2+</sup> ions (71 pm, 4-coord.) substituting for the small Al<sup>3+</sup> (53 pm, 4-coord.) in the spinel block, as they do in SrAl<sub>12</sub>O<sub>19</sub>. For CAO:Cr, the ion size of Cr<sup>3+</sup> ions (75.5 pm, 6-coord.) is larger than that of Al<sup>3+</sup> (67.5 pm, 6coord.) and much smaller than that of Ca<sup>2+</sup> ions (~126 pm). Then the increase of *d* is attributed to the fact that Cr<sup>3+</sup> substitutes for Al<sup>3+</sup> site in the host.

The ET efficiency of the Forster-Dexter type depends on the spectral overlap between Pr<sup>3+</sup> emission and coactivator absorption as well as on their separation [20,21]. Both strongly depend on the type of host lattice. Wang et al. [17] reported the observation of ET between  $Pr^{3+}$  and  $Er^{3+}$  in CAO. However, both rare-earth ions replace  $Ca^{2+}$  sites in the host. Although the dopant concentrations are relatively high, the large molecule that contains only one Ca makes big separation between the donor and acceptor, leading to a small ET rate. In the CAO unit cell, the  $Ca^{2+}$  ion is surrounded by  $Al^{3+}$  ions and the distance of Ca-Ca (~10.95 Å, evaluated from the date in Ref. [18]) is much larger than the average separation of Ca–Al ( $\sim$ 4.64 Å). In this work, Cr<sup>3+</sup> replaces  $Al^{3+}$  in the host. The average D–A distance for  $Cr^{3+}$  codoping is shorter than that for  $RE^{3+}$  co-doping for the same doping concentration. According to Dexter's theory, the ET efficiency depends on the average D-A separation in the host [21]. The shorter D-A distance may benefit the ET between  $Pr^{3+}$  and  $Cr^{3+}$ .

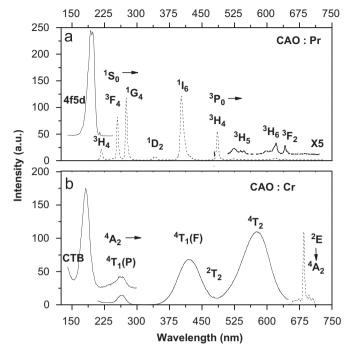
#### 3.2. Spectral overlap and possibility of PCE in CAO: Pr, Cr

The VUV excitation and emission spectrum of CAO:1% Pr is shown in Fig. 2(a). The bands in the VUV excitation spectrum are the absorptions of  $Pr^{3+}$  4f5d states. Upon 205 nm excitation of the 4f5d states, the emission lines of  $Pr^{3+}$  at 214, 254, 275, 341, 402 and 485 nm are assigned to  ${}^{1}S_{0} - {}^{3}H_{4}$ ,  ${}^{3}F_{4}$ ,  ${}^{1}G_{4}$ ,  ${}^{1}D_{2}$ ,  ${}^{1}I_{6}$  and  ${}^{3}P_{0} - {}^{3}H_{4}$  transitions, respectively, and the emissions of  ${}^{1}S_{0}-{}^{1}I_{6}$  and  ${}^{3}P_{0}-{}^{3}H_{4}$ constitute the two-step PCE process [13–15]. The UV and VUV excitation and emission spectra of CAO:1% Cr are shown in Fig. 2(b). The broad band dominated at 184 nm is ascribed to the  $O^{2-}-Cr^{3+}$  related charge transfer band (CTB) [22]. In the UV excitation spectrum, the three bands at 575, 419 and 264 nm belong to the spin-allowed transitions from the  ${}^{4}A_{2}$  to the  ${}^{4}T_{2}$ ,  ${}^{4}T_{1}(F)$  and  ${}^{4}T_{1}(P)$ states of Cr<sup>3+</sup>, respectively [23]. The emission of CAO:Cr consists of a  ${}^{2}E{-}^{4}A_{2}$  zero-phonon line peaking at 686 nm with some vibronic sidebands [23]. The comparison of the emission spectrum of CAO:Pr and the excitation spectrum of CAO:Cr reveals that the two-step  $Pr^{3+}$  cascade emissions  ${}^{1}S_{0}$  +  ${}^{1}I_{6}$  at 402 nm and  ${}^{3}P_{0}$  +  ${}^{3}H_{4}$  at 485 nm overlap



 $Cr^{3\,+}$  excitations  ${}^{4}A_{2} {}^{-4}T_{1}(F)$  and  ${}^{4}A_{2} {}^{-4}T_{2}$  states, respectively. According to Dexter's theory [21], in  $Pr^{3\,+} {}^{-}Cr^{3\,+}$  codoped CAO system, PCE could be achieved by ETs from  $Pr^{3\,+} \, {}^{1}S_{0}$  and  ${}^{3}P_{0}$  states to  $Cr^{3\,+}$  under these resonant conditions, i.e., the successive emissions of  $Pr^{3\,+} \, {}^{1}S_{0}$  and  ${}^{3}P_{0}$  states are both possible to be converted into the luminescence of  $Cr^{3\,+}$ , and then the unpractical PCE properties of  $Pr^{3\,+}$  can be modified.

Part of the energy-level scheme for the Pr<sup>3+</sup>-Cr<sup>3+</sup> system in CAO, showing the possibility of using  $Cr^{3+}$  codoping to modify the PCE properties of Pr<sup>3+</sup> via a twostep ET, is presented in Fig. 3. Firstly, upon excitation to the lowest 4f5d states of  $Pr^{3+}$ , part of the excitation energy is transferred to  $Cr^{3+}$  by cross-relaxation, exciting  $Cr^{3+}$  to the  ${}^{4}T_{1}(F)$  state and bringing  $Pr^{3+}$  to the  ${}^{1}I_{6}$  level (denoted by CR<sub>i</sub>). Secondly, after the electrons quickly relax from  ${}^{1}I_{6}$ down to  ${}^{3}P_{J}$  [24], the remaining excitation also can be transferred to a high-energy state of Cr<sup>3+</sup> (denoted by  $ET_{p}$ ). Each step can result in a red emission due to the  $Cr^{3+2}E^{-4}A_2$  transition. It should be noted that  $CR_i$  can depopulate the  $Pr^{3+1}S_0$  state, feed the high-energy states of  $Cr^{3+}$  and simultaneously populate the <sup>1</sup>I<sub>6</sub> level of  $Pr^{3+}$ . Consequently, an *increase* of the relative emission intensity of  ${}^{3}P_{0}$  to  ${}^{1}S_{0}$  is expected in CAO:Pr, Cr compared to that in CAO:Pr if CR<sub>i</sub> occurs. The occurrence of CR<sub>i</sub> can therefore be evaluated by comparing the emission spectra upon  $Pr^{3+}$ 4f5d states excitation in samples with and without  $Cr^{3+}$ co-doping.



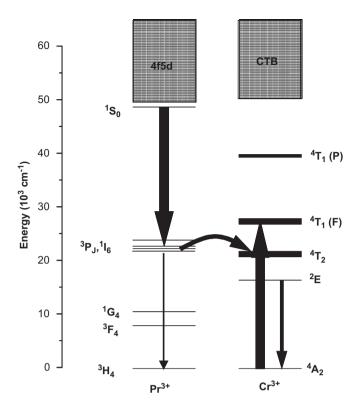


Fig. 3. Energy level diagram of the  $Pr^{3+}$ - $Cr^{3+}$  system in CAO, showing the possibility of using  $Cr^{3+}$  co-doping to modify the PCE properties of  $Pr^{3+}$  via ET.

In addition, there are also spectral overlaps between  ${}^{1}S_{0}{}^{-3}F_{4}$ ,  ${}^{1}G_{4}$   $Pr^{3+}$  emissions and the  ${}^{4}A_{2}{}^{-4}T_{1}(P)$   $Cr^{3+}$  absorption, as shown in Fig. 2. Thus the emission energies of  $Pr^{3+}{}^{1}S_{0}{}^{-3}F_{4}$ ,  ${}^{1}G_{4}$  also could be transferred to  $Cr^{3+}$  through cross-relaxations (denoted by  $CR_{f}$  and  $CR_{g}$ , respectively). However, after the electrons relax from  ${}^{1}S_{0}$  down to  ${}^{3}F_{4}$  or  ${}^{1}G_{4}$  through cross-relaxations, the remaining energy could not be transferred to  $Cr^{3+}$  and also no visible emissions could be yielded. But the contribution to this transfer is equivalent to the direct ET of all excitation energy from  $Pr^{3+}$   ${}^{1}S_{0}$  state to a high  $Cr^{3+}$  state (denoted by  $ET_{S}$ ), and also could result in a red photon on  $Cr^{3+}$ .

# 3.3. Spectroscopic investigation of PCE via ET in CAO:Pr, Cr

Fig. 4 presents the UV (a) and VUV (b) excitation spectra of the  $Cr^{3+}$  emission at 686 nm in CAO:1% Cr,  $x^{9/6}$ Pr (x = 0, 1, 3, 5). The peaks of  $Pr^{3+} {}^{3}H_{4} - {}^{3}P_{0}$  (485 nm),  ${}^{3}P_{1}$ (465 nm),  ${}^{3}P_{2}$  (445 nm), belong to spin forbidden transitions, appear in the UV excitation spectra of  $Cr^{3+}$  emission and grow up with increasing x, indicating the occurrence of ET from  $Pr^{3+} {}^{3}P_{J}$  to  $Cr^{3+}$ . In the VUV excitation spectra, the additional contributions locating on the right shoulder of the  $O^{2-}-Cr^{3+}$ -related CTB are attributed to the absorptions of the  $Pr^{3+} 4f5d$  states. The peak at 214 nm is attributed to the transition of  $Pr^{3+} {}^{3}H_{4}-{}^{1}S_{0}$ . They all enhance as x increases, implying that the  $Cr^{3+}$  emission in

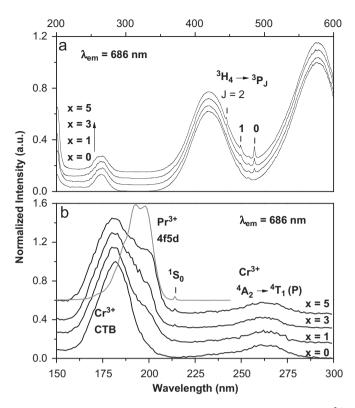


Fig. 4. Normalized UV (a) and VUV (b) excitation spectra of the  $Cr^{3+}$  686 nm emission in CAO:1% Cr, x% Pr (x = 0, 1, 3, 5). The spectra have been offset vertically for clarity.

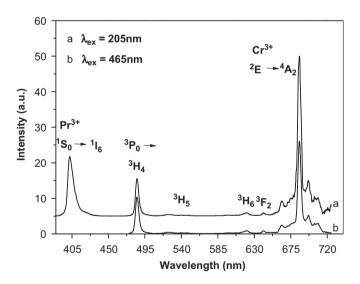


Fig. 5. Emission spectra of CAO:1% Pr, 5%Cr upon the lowest 4/5d excitation at 205 nm (a) and under  ${}^{3}P_{1}$  excitation at 465 nm (b). Two emission spectra are scaled to the  ${}^{3}P_{0}-{}^{3}H_{4}$  emission intensity.

the co-doped samples could be excited through the ET from  $Pr^{3\,+\,\,1}S_0$  to  $Cr^{3\,+}.$ 

The emission spectra of the typical sample of CAO:1% Pr, 5%  $Cr^{3+}$  upon excitation in the lowest 4*f*5*d* state (205 nm) and  ${}^{3}P_{1}$  level (465 nm) of  $Pr^{3+}$  are depicted in Fig. 5. The spectra are scaled to the emissions from  $Pr^{3+}$   ${}^{3}P_{0}$  and the contribution of  $Cr^{3+}$  emissions by direct

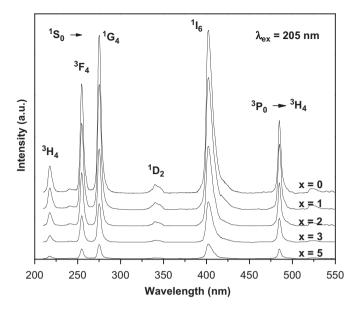


Fig. 6. Emission spectra of CAO:1% Pr, x% Cr (x = 0, 1, 2, 3, 5) upon 205 nm excitation. The spectra have been offset vertically for clarity.

excitation at 205 and 465 nm, respectively, has been subtracted by using the spectra of singly doped Cr sample. Under 465 nm excitation, the appearance of  $Cr^{3+}$  emission is in agreement with the existence of ET from  $Pr^{3+} {}^{3}P_{J}$  to  $Cr^{3+}$ . The relative emission intensity of  $Cr^{3+}$  to  $Pr^{3+} {}^{3}P_{0}$  is much higher upon 205 nm excitation compared to that upon 465 nm excitation. This observation substantiates that  ${}^{1}S_{0}$  can transfer part of excitation energy to  $Cr^{3+}$  in addition to  ${}^{3}P_{J}$  upon  $Pr^{3+} 4f5d$  excitation.

The emission spectra of  $Pr^{3+}$  in CAO:1% Pr, x% Cr (x = 0, 1, 2, 3, 5) upon 205 nm excitation are displayed in Fig. 6. The PCE process of  $Pr^{3+}$ ,  ${}^{1}S_{0}{}^{-1}I_{6}$  (402 nm) and  ${}^{3}P_{0}$ - ${}^{3}H_{4}$  (485 nm), is observed [13–15]. First, the intensities of the  ${}^{1}S_{0}$  emissions decrease greatly as x increases, which is consistent with the presence of ET from the  $Pr^{3+1}S_0$  state to  $Cr^{3+}$ . Second, it can be carefully observed that the relative intensities of the  ${}^{3}P_{0}$  to  ${}^{1}S_{0}$  emissions are changed with x while those of different  ${}^{1}S_{0}$  emissions are not. The decreasing rate of the  ${}^{3}P_{0}-{}^{3}H_{4}$  emission is slower than those of <sup>1</sup>S<sub>0</sub> emissions with increasing x. For example, at x = 0the  ${}^{3}P_{0}-{}^{3}H_{4}$  emission intensity is weaker than that of  ${}^{1}S_{0}$   $-{}^{3}F_{4}$ , but when x increases to 5, the intensities of the two emission lines are about equal. Generally, upon the lowest 4f5d state excitation, the population of  ${}^{3}P_{0}$  comes from the  ${}^{1}S_{0}-{}^{1}I_{6}$  transition in the singly  $Pr^{3+}$ -doped sample, i.e., the  ${}^{1}S_{0}-{}^{1}I_{6}$  emission intensity can be taken as a measure of the initial  ${}^{3}P_{0}$  population [24]. The changes of the relative emission intensity of  ${}^{3}P_{0}$  to  ${}^{1}S_{0}$  with x can therefore indicate the influence of Cr<sup>3+</sup> co-doping on the population of  ${}^{3}P_{0}$ . Two approaches could influence the relative intensity of  ${}^{3}P_{0}$  to  ${}^{1}S_{0}$  in  $Pr^{3+}$  and  $Cr^{3+}$  co-doped samples: one is CR<sub>i</sub>, as discussed before; the other is ET<sub>p</sub>. Actually, there is a competition between  $CR_i$  (increasing the  ${}^{3}P_0$ population for higher relative intensity) and ET<sub>p</sub> (decreasing the  ${}^{3}P_{0}$  population for lower relative intensity).

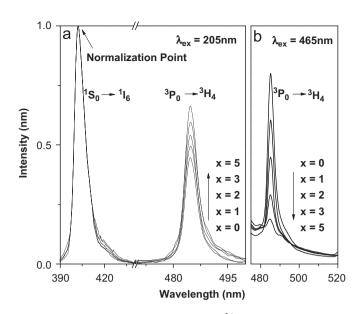


Fig. 7. (a) Normalized emission spectra of  $Pr^{3+}$  in CAO:1% Pr, x% Cr (x = 0, 1, 2, 3, 5), excited at 205 nm. (b) Emission spectra of  $Pr^{3+} {}^{3}P_{0}{}^{-3}H_{4}$  transition in CAO:1% Pr, x% Cr (x = 0, 1, 2, 3, 5), excited at 465 nm.

In Fig. 7, the emission spectra of  $Pr^{3+}$  in CAO:1% Pr, x% Cr (x = 0, 1, 2, 3, 5) upon 205 nm excitation are normalized and compared with those under  ${}^{3}P_{1}$  excitation by 465 nm. First, under  ${}^{3}P_{1}$  excitation the  ${}^{3}P_{0}$  emission decreases with increasing x, which is in accord with the occurrence of ET from the  ${}^{3}P_{0}$  to  $Cr^{3+}$ . Second, the expected increase (see Section 3.2) in the relative emission intensity of  ${}^{3}P_{0}$  to  ${}^{1}S_{0}$  is observed clearly as x increases upon 205 nm excitation, though the ET from  ${}^{3}P_{0}$  to Cr<sup>3+</sup> can simultaneously depopulate the  ${}^{3}P_{0}$  level resulting in the decreasing relative intensity. This observation evidences the existence and the efficiency of CR<sub>i</sub> in the ET from  $Pr^{3+1}S_0$ to Cr<sup>3+</sup>. In one word, upon VUV excitation of the lowest 4f5d state of  $Pr^{3+}$ , PCE via ET, CR<sub>i</sub> followed by ET<sub>p</sub>, takes place. If this ET process is efficient enough, the unpractical PCE of Pr3+ in CaAl12O19 will be modified into a two-red-photon luminescence of Cr<sup>3+</sup> with high quantum yield.

# 3.4. Dynamic processes and mechanisms of ET from $Pr^{3+}$ to $Cr^{3+}$

The typical decay profiles of the  $Pr^{3+} {}^{3}P_{0}-{}^{3}H_{4}$  emission in CAO:1% Pr, x% Cr (x = 0, 1, 3, 5, 7) are plotted in Fig. 8. It can be seen that in the single  $Pr^{3+}$ -doped sample the fluorescence decays strictly obey the exponential rule as expected (only radiative decay). In the  $Pr^{3+}$  and  $Cr^{3+}$  codoped sample, when the  $Cr^{3+}$  concentration is increased, the decay curve becomes more and more rapid and nonexponential, which can be explained by the introduction of extra decay pathways due to the  $Cr^{3+}$  co-doping: ET from  $Pr^{3+} {}^{3}P_{0}$  to  $Cr^{3+}$  enhances the  ${}^{3}P_{0}$  decay rate [25]. The non-exponential behavior can also be explained as follows. In the concentration range studied in this work the  $Cr^{3+}$ ions are randomly distributed around the  $Pr^{3+}$  lattice sites.

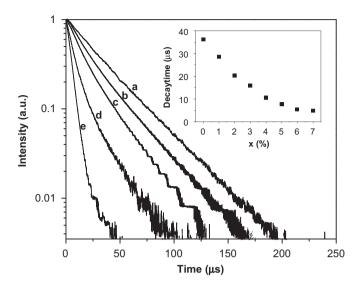


Fig. 8. Typical fluorescence decay curves of the  ${}^{3}P_{0}$  emission in CAO:1% Pr, x% Cr, (a) x = 0, (b) x = 1, (c) x = 3, (d) x = 5, (e) x = 7 at 465 nm excitation. Inset: Cr<sup>3+</sup> concentration dependence of decay time of the  ${}^{3}P_{0}$  emission.

The environment of every  $Pr^{3+}$  ion is different, leading to a variety of transfer rates, that is, the instantaneous average ET rate varies with time. And then, the luminescent decay curve deviates from an exponential function [26].

The difference in lifetime between samples with and without activator ions is a useful way of characterizing the ET process between sensitizer and activator ions [26]. Since the decay of  $Pr^{3+}$  ions in the presence of  $Cr^{3+}$  ions is non-exponential, the "1/e-decay time" has no physical meaning for multi-exponential decay curves. Instead, according to Inokuti–Hirayama model [27], the lifetime of a non-exponential decay curve can be defined by

$$\tau = \frac{1}{I_0} \int_0^\infty I(t) \,\mathrm{d}t,\tag{1}$$

where  $I_0$  is the intensity at t = 0. Thus  $\tau$  is the mean decay time, which can be obtained by integrating the decay curve over time after normalization. At x = 0,  $\tau_0$  is about 36 µs, which is consistent with that yielded by a monoexponential fit. In the inset of Fig. 8, the  $\tau$  is plotted versus  $Cr^{3+}$ concentration.

Now we will focus on the microscopic mechanism of ET from  $Pr^{3+}$  to  $Cr^{3+}$ . The microscopic mechanism of ET was first explained by Forster and Dexter [20,21]. Since there are favorable spectra overlaps of  $Pr^{3+}$  emissions and  $Cr^{3+}$  absorptions, both radiative and nonradiative transfer could be involved in the ET process.

For radiative transfer, photons emitted by donors are reabsorbed by acceptors. The pattern of donor fluorescence depends on the acceptor concentration, but the donor lifetime does not change with that [28]. As shown in Fig. 2, the spectra overlaps between various  ${}^{1}S_{0}$  emission lines of  $Pr^{3+}$  and the absorptions of  $Cr^{3+}$  are all different. However, no obvious changes can be observed for the relative branching ratios of the  ${}^{1}S_{0}$  emissions with or without  $Cr^{3+}$  co-doping (see Fig. 6). In addition, in our experiments the decay time of  $Pr^{3+} {}^{3}P_{0}$  is dependent strongly on the concentration of  $Cr^{3+}$  (see Fig. 8). The results indicate that the ET in these materials is essentially a non-radiative process.

For non-radiative transfer, the transfer mechanisms, exchange (ex) and/or multipolar interactions, differ from one another in the dependence of the transfer rate on  $R_{DA}$ , the average distance of donor and acceptor [21,28]. According to Van Uitert formula [29]

$$C_0 = V(4\pi R_0^3/3)^{-1},$$
(2)

where  $C_0$  is the critical concentration of acceptor, at which the emission intensity or decay time of the donor is half of that without it.  $R_0$  is the critical distance with which the ET rate is equal to the radiative decay rate from the excited donor, and V is the volume of the unit cell of CAO. By taking the experimental and analytic values of  $C_0$  and V, about 2% for the transfer form  $Pr^{3+3}P_0$  to  $Cr^{3+}$  (see Fig. 8) and 585.83 Å [18], respectively, into the formula,  $R_0$ is found to be about 19 Å, which is much larger than the typical critical distance for ex interaction (<5Å) [21]. It indicates that the mechanism of ex interaction plays no role in the ET process. The multipolar character of any ET process has not only an influence on the time decay of donor luminescence but also on the concentration dependence of the macroscopic ET rate  $(P_{DA})$ . Neglecting the diffusion of excitation energy between donors, based on Dexter's ET formula of multipolar interaction the following relation can be obtained [21]:

$$P_{\rm DA} \propto \frac{1}{R_{\rm DA}^n} \propto x^{n/3},\tag{3}$$

where  $R_{DA}$  also is the average D–A distance, x the ion concentration and n = 6, 8 and 10, corresponding to dipole–dipole (d–d), dipole–quadrupole (d–q), and quadrupole–quadrupole (q–q) interactions, respectively. Thus, the dependence of the ET rate on ion concentration strongly depends on the dominant multipolar mechanism.

In addition, the macroscopic ET rate  $P_{DA}$  as a function of ion concentration can be evaluated from the lifetime measurements of the donor state since

$$P_{\rm DA} = \frac{1}{\tau} - \frac{1}{\tau_0},$$
 (4)

 $\tau_0$  and  $\tau$  are the decay times of the donor emission in the singly and co-doped samples, respectively [30].

Using Eqs. (1), (3) and (4) and Reisfeld's approximation the nature of interaction in this transfer process can be decided by plotting the following relation [30]:

$$\frac{I_0}{I} \propto x^{n/3}$$
 or  $\frac{\tau_0}{\tau} \propto x^{n/3}$ , (5)

where  $I_0$  and I are the luminescence intensities of  $Pr^{3+}$  with and without the presence of  $Cr^{3+}$  and n = 6, 8 and 10 again stands for d–d, d–q, and q–q interaction mechanisms. The  $\tau_0/\tau - x^{n/3}$  plots are depicted in Fig. 9 and when

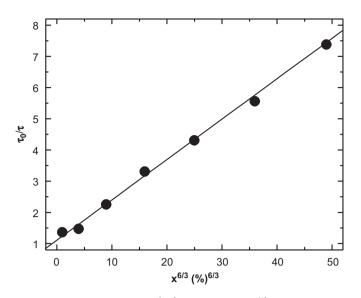


Fig. 9. Dependence of  $\tau_0/\tau$  of  $Pr^{3+3}P_0$  emissions on  $x^{6/3}$  for CAO:1% Pr,  $x^{6/3}$  Cr (x = 1-7). The solid line is a linear fit curve.

n = 6 it shows linear relation. We can then conclude that the electric d-d interaction mechanism is predominantly responsible for the ET between  $Pr^{3+}$  and  $Cr^{3+}$  ions in the co-doped CAO:Pr, Cr samples (at least in the concentration range studied in this work).

# 3.5. Visible QE for CAO: Pr and CAO: Pr, Cr

For single  $Pr^{3+}$  activated CAO the  ${}^{3}P_{0}$  state is the intermediate state yielding the second photon in the cascade emission process,  ${}^{1}S_{0}-{}^{1}I_{6}$  followed by  ${}^{3}P_{0}-{}^{3}H_{4}$ . Taking the  ${}^{1}S_{0}-{}^{1}I_{6}$  fluorescence intensity as a measure of the initial  ${}^{3}P_{0}$  population, the QE for  ${}^{3}P_{0}$  yielding the second step emission,  $\eta_p$ , can be written as  $\eta_p = R/\beta$ , where R is the intensity ratio of the  ${}^{3}P_{0}-{}^{3}H_{4}$  emission to the  ${}^{1}S_{0}-{}^{1}I_{6}$  emission and  $\beta$  is the branch ratio of  ${}^{3}P_{0}-{}^{3}H_{4}$ transition to all  ${}^{3}P_{0}$  transitions. For CAO:1% Pr, R and  $\beta$ are 0.326 and 0.412, respectively, and then  $\eta_p$  is about 0.79 [24].  $\eta_p$  decreases with increasing  $Pr^{3+}$  concentration and is significantly less than unity even at low concentration (0.5%) [24]. The total visible QE for  $Pr^{3+}$  singly doped CAO,  $\eta_{TP}$ , upon the lowest 4f5d state excitation can be written as  $\eta_{TP} = \alpha (1 + \eta_p \beta)$ , where  $\alpha$  (~0.49) is the branch ratio of  ${}^{1}S_{0}$ - ${}^{1}I_{6}$  transition to all  ${}^{1}S_{0}$  transitions and can be obtained from the corrected luminescence spectra in Fig. 2(a). For CAO:1% Pr,  $\eta_{TP}$  is about 65%. If we exclude the deep violet  ${}^{1}S_{0}-{}^{1}I_{6}$  emission, which has a poor luminous efficiency, the  $\eta_{TP}$  is only about 16%. Anyway, the total visible QE for CAO:1% Pr is far lower than unit.

For  $Pr^{3+}$  and  $Cr^{3+}$  co-doped CAO, the ET efficiency of  $CR_i$ ,  $\eta_{CR_i}$  and of the sum from  ${}^{1}S_0$  to  $Cr^{3+}$ ,  $\eta_{Sum}$ , in the first step can be expressed, respectively, by

$$\eta_{\rm CR_i} = \frac{W_{\rm CR_i}}{W_{\rm Sum} + \gamma_{\rm S}/\alpha},\tag{6}$$

$$\eta_{\rm Sum} = \frac{W_{\rm Sum}}{W_{\rm Sum} + \gamma_{\rm S}/\alpha},\tag{7}$$

where  $\gamma_{\rm S}$  is the rate of the  ${}^{1}{\rm S_{0}}{}^{-1}{\rm I_{6}}$  transition,  $W_{\rm CR_{i}}$  and  $W_{\rm Sum}$  are the ET rates of CR<sub>i</sub> and the sum from  ${}^{1}{\rm S_{0}}$  to Cr<sup>3+</sup> in the first step, respectively, and  $\alpha$  again is the branch ratio of  ${}^{1}{\rm S_{0}}{}^{-1}{\rm I_{6}}$  transition to all  ${}^{1}{\rm S_{0}}$  transitions.

In continuous excitation upon the lowest 4/5d state of  $Pr^{3+}$ , the populations of the  ${}^{1}S_{0}$  ( $n_{S}$ ) and  ${}^{3}P_{0}$  ( $n_{P}$ ) states satisfy the equation  $[\gamma_{S} + W_{CR_{i}}]n_{S} = n_{P}/\tau$ , and then,  $W_{CR_{i}}$  can be expressed by

$$W_{\rm CR_i} = \left(\frac{R\tau_0}{R_0\tau} - 1\right)\gamma_{\rm S},\tag{8}$$

where *R* and  $R_0$  (~0.326) denote the intensity ratio of the  ${}^{3}P_0 - {}^{3}H_4$  emission to the  ${}^{1}S_0 - {}^{1}I_6$  emission with and without  $Cr^{3+}$  co-doping, respectively.

The absorption of  $Pr^{3+}$  at the excitation wavelength (about 200 nm, see Fig. 2) is dominant relative to that of  $Cr^{3+}$ . If we assume that the decrease of the emission intensity of  $Pr^{3+} {}^{1}S_{0}$  is only owed to the ET from  $Pr^{3+} {}^{1}S_{0}$ to  $Cr^{3+}$ ,  $W_{Sum}$  can be estimated based on the intensity decrease of the  ${}^{1}S_{0}$  emissions with the increase of x, as shown in Fig. 6. In continuous excitation, one has

$$W_{\rm Sum} = \left(\frac{I_{\rm S_0}}{I_{\rm S}} - 1\right) \frac{\gamma_{\rm S}}{\alpha},\tag{9}$$

where  $I_{\rm S}$  is the integral intensity of  ${}^{1}{\rm S}_{0}{-}^{1}{\rm I}_{6}$  transition and  $I_{\rm s_{0}}$  the integral intensity for x = 0.

On the other hand, from the luminescence decay curves in Fig. 8 the direct ET efficiency from  $Pr^{3+} {}^{3}P_{0}$  to  $Cr^{3+}$ ,  $\eta_{ET_{p}}$ , can be determined, which is defined as the ratio of  $Pr^{3+}$  ions that depopulate by ET to  $Cr^{3+}$  ions to the total number of  $Pr^{3+}$  ions excited. By dividing the integrated intensity of the decay curves of the CAO:1% Pr, x% Cr samples to the integrated intensity of the CAO:1% Pr curve the transfer efficiency is obtained as a function of the  $Cr^{3+}$ concentration,

$$\eta_{\rm ET_p} = 1 - \frac{\int I_{x\% \rm Cr} \, \mathrm{d}t}{\int I_{0\% \rm Cr} \, \mathrm{d}t} \quad \text{or} \quad \eta_{\rm ET_p} = 1 - \frac{\tau}{\tau_0},\tag{10}$$

where *I* denotes intensity and  $x^{0}$  Cr stands for the Cr<sup>3+</sup> concentration.

At room temperature, the  ${}^{3}P_{1,2}$  states are all the thermalized levels of  ${}^{3}P_{0}$  and have the same luminescent dynamics [24]. Thus, they are all involved in the ET process and have the same transfer efficiency.

If we take the blue  ${}^{3}P_{0}{}^{-3}H_{4}$  emission of  $Pr^{3+}$  into account and exclude the deep violet  ${}^{1}S_{0}{}^{-1}I_{6}$  emission, the total visible QE for  $Pr^{3+}$  and  $Cr^{3+}$  co-doped CAO upon excitation in the lowest 4f5d state of  $Pr^{3+}$  can be determined using the following equation:

$$\eta_{\rm TPC} = \eta_{\rm Sum} + [\eta_{\rm CR_i} + (1 - \eta_{\rm Sum})\alpha][\eta_{\rm ET_p} + (1 - \eta_{\rm ET_p})\eta_{\rm p}\beta].$$
(11)

Using Eqs. (6)–(11) and the experimental data presented in Fig. 8,  $\eta_{CR_i}$ ,  $\eta_{Sum}$ ,  $\eta_{ET_p}$  and  $\eta_{TPC}$  can be evaluated and all

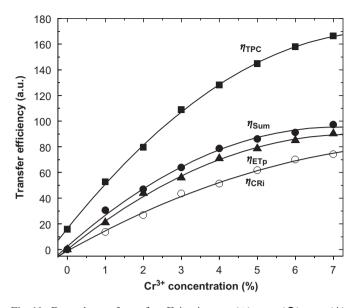


Fig. 10. Dependence of transfer efficiencies  $\eta_{CR_i}$  ( $\bigcirc$ ),  $\eta_{Sum}$  ( $\bullet$ ),  $\eta_{ET_p}$  ( $\blacktriangle$ ) and visible QE  $\eta_{TPC}$  ( $\blacksquare$ ) for CAO:1% Pr, x% Cr (x = 0-7) on Cr<sup>3+</sup> concentrations. The curves are drawn as a guide to the eye.

plotted versus  $Cr^{3+}$  concentration in Fig. 10. It can be seen that the transfer efficiencies increase rapidly with increasing  $Cr^{3+}$  content. The difference between  $\eta_{Sum}$  and  $\eta_{CR_i}$ ,  $\eta_{Sum}-\eta_{CR_i}$ , is smaller than  $\eta_{CR_i}$ , indicating that the  $CR_i$  is the main ET process from  $Pr^{3+}$   $^1S_0$  to  $Cr^{3+}$ . This is consistent with the spectral overlap between emissions of  $Pr^{3+}$  and absorptions of  $Cr^{3+}$ . According to Dexter's theory [21], the ET rate depends on the overlap integral between the emission line-shape function of the sensitizer  $(Pr^{3+})$  and the absorption line-shape function of the sensitizer ( $Pr^{3+}$ ) and the absorption line-shape function of the activator ( $Cr^{3+}$ ). The larger this spectra overlap, the more efficient the transfer process will be. As presented in Fig. 2, the spectral overlaps of the  ${}^{1}S_{0}-{}^{1}I_{6}$  emission of  $Pr^{3+}$  with the excitation of  $Cr^{3+}$  are larger than other  ${}^{1}S_{0}$  emissions of  $Pr^{3+}$  with  $Cr^{3+}$ .

Generally, for the ET between donor  $(Pr^{3+})$  and acceptor  $(Cr^{3+})$  ions, the higher acceptor dopant concentration will theoretically result in the higher trapping probability and then the higher ET efficiency. As shown in Fig. 10, the transfer efficiencies,  $\eta_{\text{Sum}}$  and  $\eta_{\text{ET}_{p}}$ , get closer and closer to 100% with the increase of  $Cr^{3+}$  concentration. We can assume that  $\eta_{Sum}$  and  $\eta_{ET_p}$  could approximately be equal to 1 if x is high enough, i.e., the  ${}^{1}S_{0}$  and  ${}^{3}P_{0}$ states could transfer all of their energies to  $Cr^{3+}$ . And then, following Eq. (11), the maximal visible QE  $\eta_{\text{TPC}} \approx 1 + \eta_{\text{CR}}$ . According to Fig. 10, when x > 5,  $\eta_{CR_i} > 70\% \eta_{Sum}$ , that is, more than 70% energy was transferred to Cr<sup>3+</sup> through  $CR_i$  in the transfers from  ${}^{1}S_0$  to  $Cr^{3+}$  ( $CR_i$ ,  $CR_f$ ,  $CR_g$  and ETs). Thus the maximal  $\eta_{\text{TPC}}$  could reach more than 170%. The visible OE is much higher than unity and may seem exciting. But unfortunately, it cannot be achieved. Firstly, in a practical VUV phosphor based on the  $Pr^{3+}-Cr^{3+}$  pair, the  $Pr^{3+}$  ion and not the  $Cr^{3+}$  should absorb the VUV emission from the Xe discharge (located

between 149 and 173 nm) of the eventual application. As shown in Fig. 2, it becomes evident that  $Cr^{3+}$  ions will be involved in the absorption just as well as  $Pr^{3+}$  ions in the VUV region. Direct  $Cr^{3+}$  excitation will result in a normal one-photon emission process, which lowers the total QE of the two-photon-luminescence. Secondly,  $\eta_{TPC}$  is dependent on the dopant concentrations of  $Pr^{3+}$  and  $Cr^{3+}$  and their concentration ratios. The dopant concentration of Pr<sup>3+</sup> must be high enough that can ensure that phosphor has a strong absorption or a big absorption cross-section in the VUV region. But higher concentration wants higher trapping probability and too high concentration will bring out concentration quenching. The critical quenching concentration of  $Pr^{3+}$  due to the cross relaxation of  ${}^{3}P_{0}$ is more than 5% in CAO (this work). For the dopant concentration of Cr<sup>3+</sup>, too high concentration will result in the direct excitation of Cr<sup>3+</sup> instead of Pr<sup>3+</sup> and also the occurrence of concentration quenching. Thus, the realization of the maximum  $\eta_{\text{TPC}}$  is dependent on the optimal excitation wavelength and the optimum concentrations of Pr<sup>3+</sup> and Cr<sup>3+</sup> and their concentration ratios. In our present work, the series of CAO:1% Pr, x% Cr (x = 1-10) samples were chosen and the excitation of the lowest 4f5dstate of  $Pr^{3+}$  at about 200 nm was selected, where the absorption of Cr<sup>3+</sup> is very weak and is ignored in this work.

As shown in Fig. 11, the dependence of  $Cr^{3+}$  emission intensities on  $Cr^{3+}$  concentration in CAO:1% Pr, x% Cr (x = 1-10) upon  $Pr^{3+}$  excitation at 205 nm and under direct  $Cr^{3+}$  excitation at 550 nm are presented. The emission intensities at x = 1 in the two samples have been normalized. Under different excitations, both emission intensities approach maximum at  $Cr^{3+}$  content about 5%, then they decrease. From curve (a), the critical quenching concentration of  $Cr^{3+}$  can be determined to be about 5%

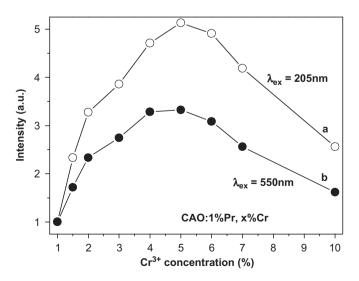


Fig. 11. Dependence of emission intensity of  $Cr^{3+}$  on the  $Cr^{3+}$  concentration in CAO:1% Pr, x% Cr (x = 1-10) under 205 nm (a) and under 550 nm excitations (b). The emission intensities at x = 1 in the two samples have been normalized.

in CAO. With the increasing  $Cr^{3+}$  content, for the climbing phase the emission intensities upon  $Pr^{3+}$  excitation increase faster than that under  $Cr^{3+}$  excitation, which shows that the ET from  $Pr^{3+}$  to  $Cr^{3+}$  increases the luminescence output of  $Cr^{3+}$ . However, upon  $Pr^{3+}$  excitation at  $Cr^{3+}$  concentration higher than 5%, although the ET efficiency will continue to increase, as discussed above, the actual luminescence output of the  $Cr^{3+}$  ions will decrease in the same way due to the concentration quenching of  $Cr^{3+}$ . When the  $Pr^{3+}$  concentration is fixed at 1%, the optimum concentrations for  $Cr^{3+}$  is about 5%. As shown in Fig. 10, for x = 5,  $\eta_{CR_i} = 61\%$ ,  $\eta_{Sum} = 86\%$ ,  $\eta_{ET_p} = 78\%$  and  $\eta_{TPC} = 143\%$  are obtained. But considering the  $Cr^{3+}$  ions will compete with the  $Pr^{3+}$  ions under the radiation from the Xe discharge, we believe that the actual visible QE as a practical VUV phosphor will be depressed greatly.

#### 4. Conclusions

The  $Cr^{3\,+}$  ion was chosen as a co-dopant to modify the unpractical PCE properties of  $Pr^{3\,+}$  in  $CaAl_{12}O_{19}$  phosphors. There exists a favorable spectra overlap between the emission spectra of the Pr<sup>3+</sup> and the excitation spectra of the  $Cr^{3+}$  in CAO, which promotes a two-step ET from  $Pr^{3+}$  to  $Cr^{3+}$ , converting the photon from  $Pr^{3+}$   ${}^{1}S_{0}$  in the unpractical UV or near-UV region into the red Cr<sup>3+</sup> emission through cross-relaxations, and subsequently, photon from  $Pr^{3+} {}^{3}P_{0}$  also into the red  $Cr^{3+}$  emission through direct ET. The Dexter model was applied to the analysis of the concentration dependence of the ET rate from  $Pr^{3+} {}^{3}P_0$  to  $Cr^{3+}$ , which indicated that the d-d interaction mechanism is mainly responsible for the transfer. Upon excitation into the lowest 4f5d state of  $Pr^{3+}$ , the two-step ET between  $Pr^{3+}$  and  $Cr^{3+}$  is efficient and a visible QE higher than 100% can be achieved, but considering the  $Cr^{3+}$  ions will compete with the  $Pr^{3+}$  ions under the radiation from the Xe discharge, we believe that the actual visible QE as a practical VUV phosphor will be depressed greatly.

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